

Today

- Quiz 2
- Minima, maxima and inflection points
- Graphing

If you want to find a min/max of $f'(x)$, look for points at which. . .

- (A) $f'(x) = 0$. \rightarrow potential extremum of $f(x)$
- (B) $f'(x) = 0$ and $f''(x) \neq 0$. \rightarrow extremum of $f(x)$
- (C) $f''(x) = 0$. \rightarrow potential extremum of $f'(x)$
- (D) $f''(x) = 0$ and $f'''(x) \neq 0$. \rightarrow extremum of $f'(x)$
- (E) Don't know.

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This is "SDT" where the function considered is f' instead of f ! Would usually use "FDT".

Potential IPs

- A potential IP is a point a at which $f''(a)=0$ because that MIGHT be a min/max of $f'(x)$.
- If $f''(x)$ changes sign at a potential IP of $f(x)$, then it is an IP of $f(x)$ because it's an extrema of $f'(x)$.
- If $f''(x)$ does not change sign at a potential IP of $f(x)$, then the potential IP is not an IP of $f(x)$!

Summary

- Use $f'(x)$ to determine intervals of **increase/decrease** of $f(x)$.
- Solve $f'(x)=0$ to find **potential extrema** ($x=a$).
Check that $f'(x)$ **changes sign** at a (FDT) or that $f''(a) \neq 0$ (SDT) to make sure.
- Use $f''(x)$ to determine intervals of **concave up/down**.
- Solve $f''(x)=0$ to find **potential inflection points** ($x=a$). Check that $f''(x)$ **changes sign** at a ("FDT") or that $f'''(a) \neq 0$ ("SDT") to make sure.

Does $f(x) = x^4$ have an inflection point?

(A) $f'(0) = 0$ so yes.

(B) $f''(0) = 0$ so yes.

(C) $f'''(0) = 0$ so no.

(D) $f''(0) = 0$ and $f''(x) > 0$ for all $x \neq 0$ so no.

(E) Don't know.

Does $f(x) = x^4$ have an inflection point?

(A) $f'(0) = 0$ so yes.

(B) $f''(0) = 0$ so yes.

(C) $f'''(0) = 0$ so no. ← "Second DT" applied to $f'(x)$
- fails so no conclusion.

(D) $f''(0) = 0$ and $f''(x) > 0$ for all $x \neq 0$ so no.

$$f''(x) = 12x^2$$

(E) Don't know.

Not sure about (C)? Try this for $f(x) = x^5$.