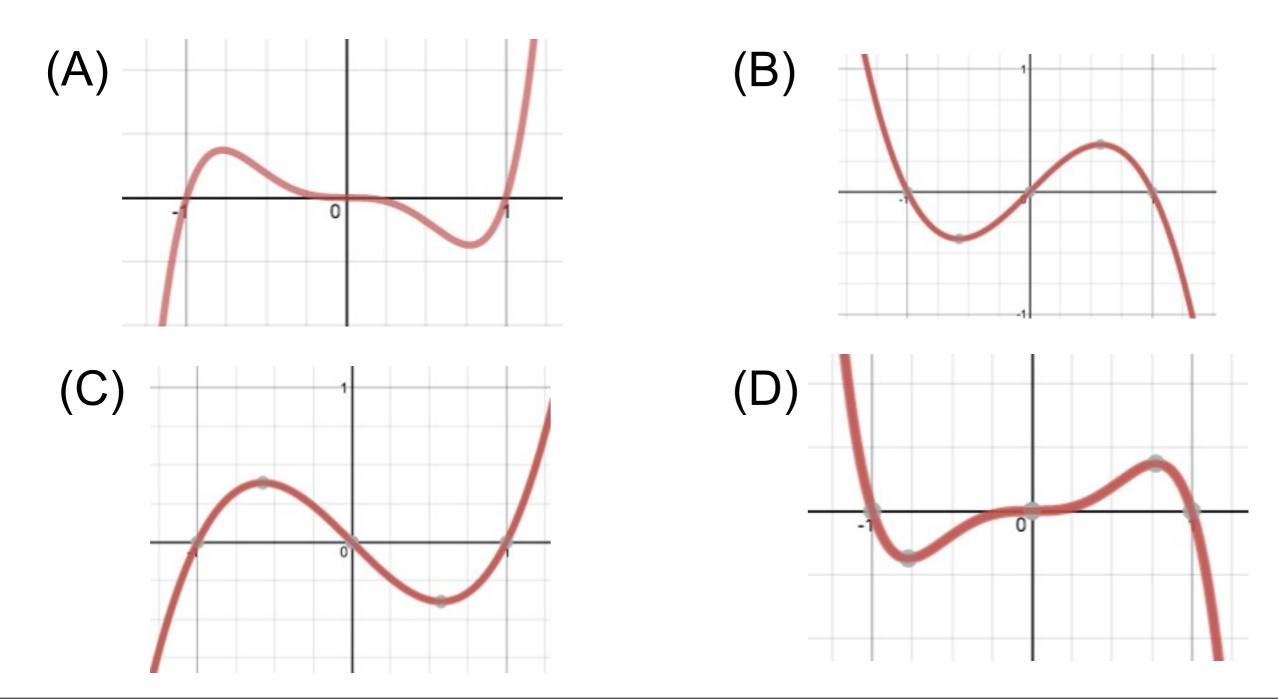
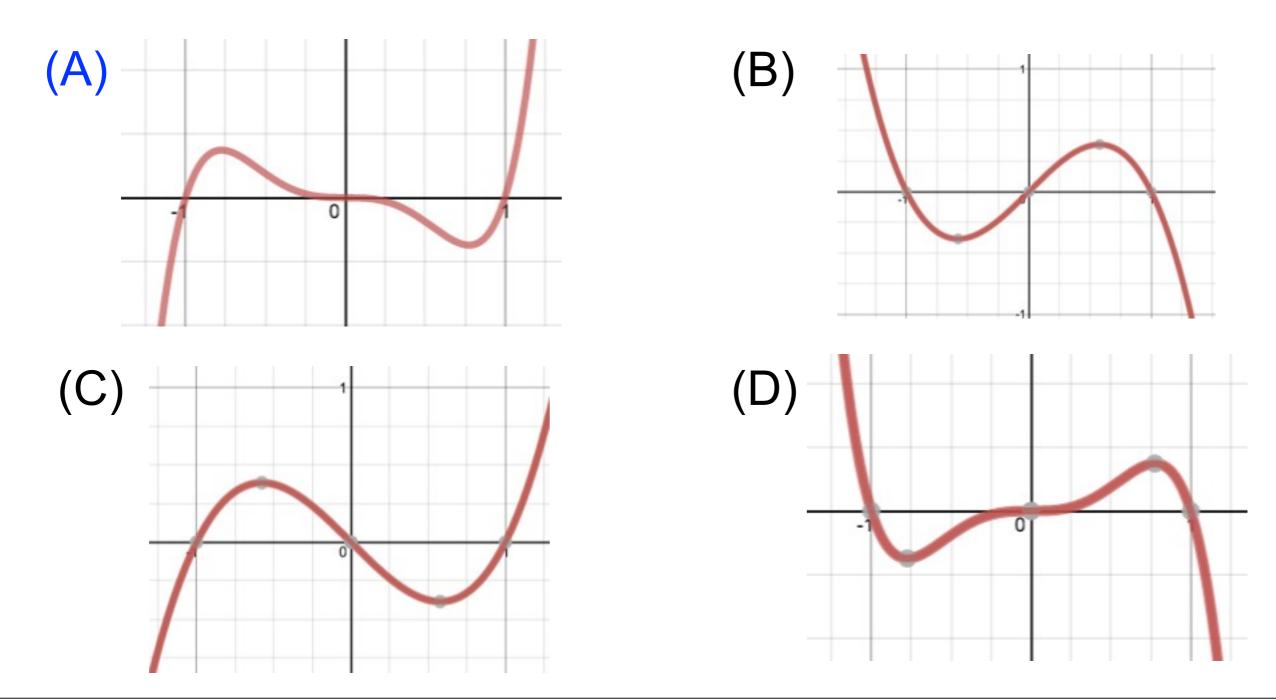
Today...

- Clicker questions on graphing simple polynomials.
- Hill functions.
- Introduction to the derivative (if there's time).

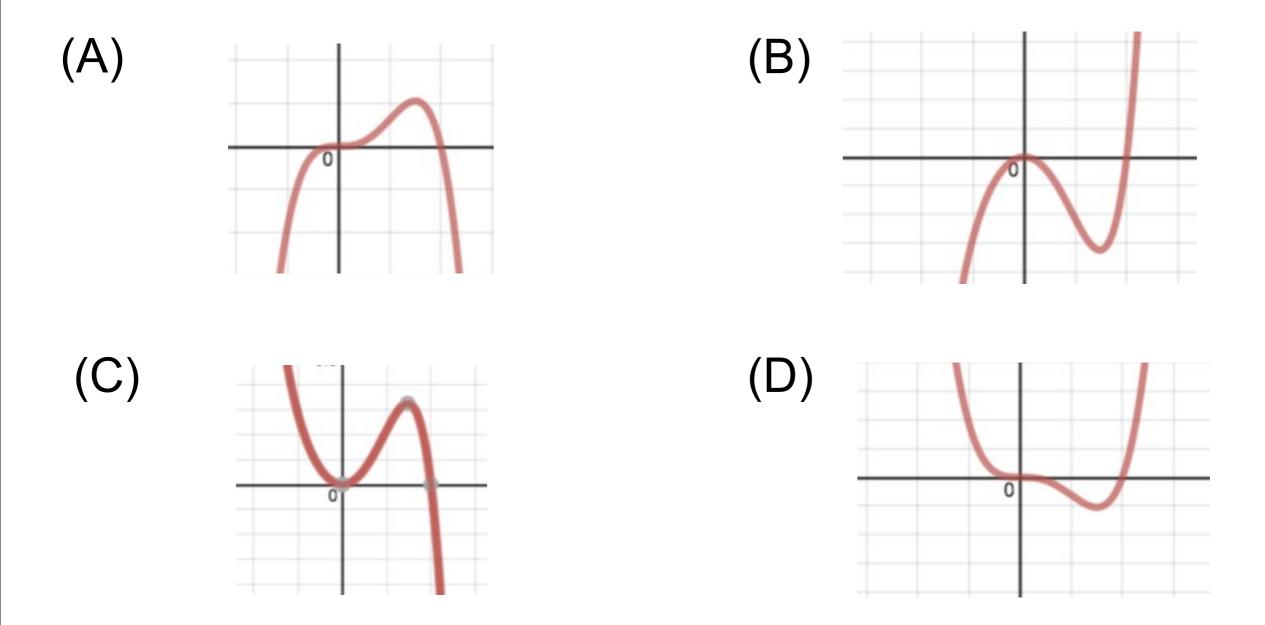
Which is the graph of the function $f(x) = x^5 - x^3$?



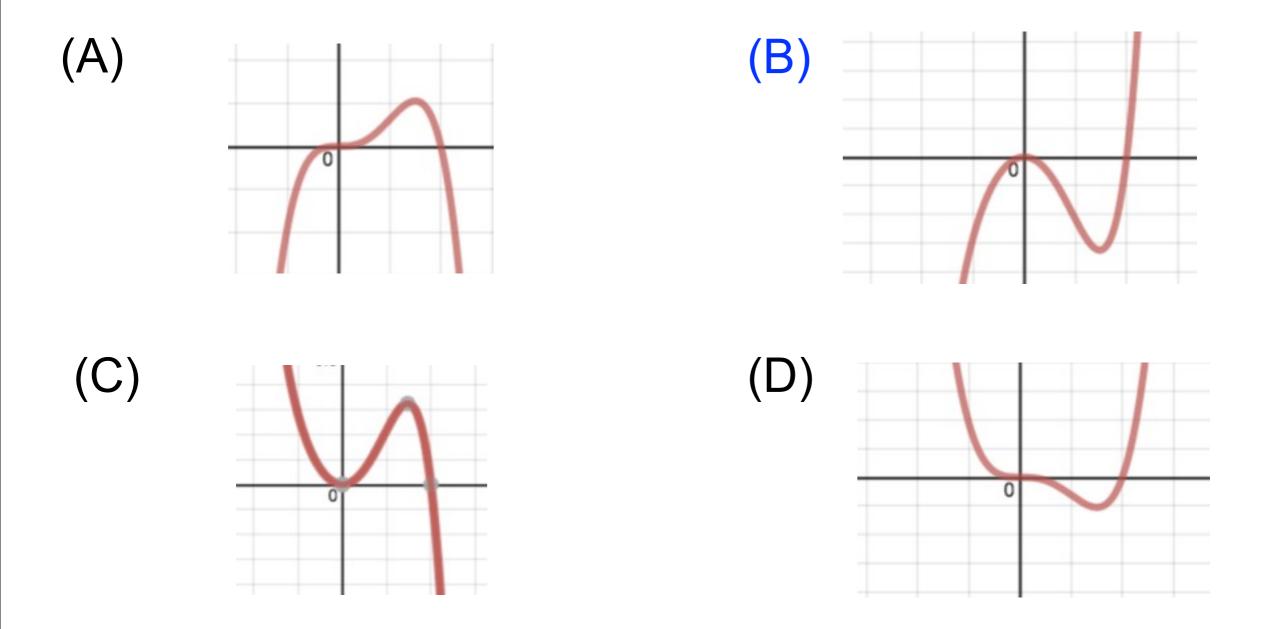
Which is the graph of the function $f(x) = x^5 - x^3$?



Which is the graph of the function $g(x) = x^5 - x^2$?



Which is the graph of the function $g(x) = x^5 - x^2$?



Hill functions

$$f(x) = \frac{ax^n}{b^n + x^n}$$

A useful function for studying saturating phenomena.

Hill functions

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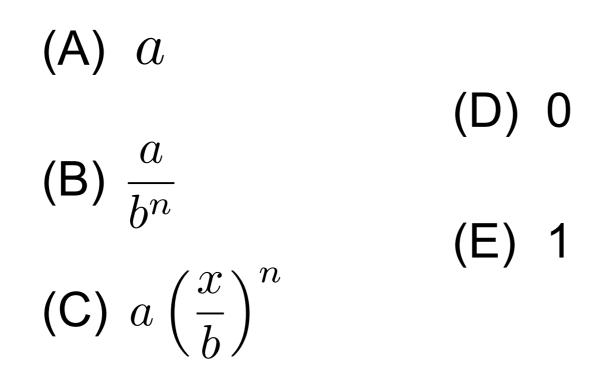
- A useful function for studying saturating phenomena.
- Important functions in biochemistry Michaelis-Menten kinetics

Hill functions

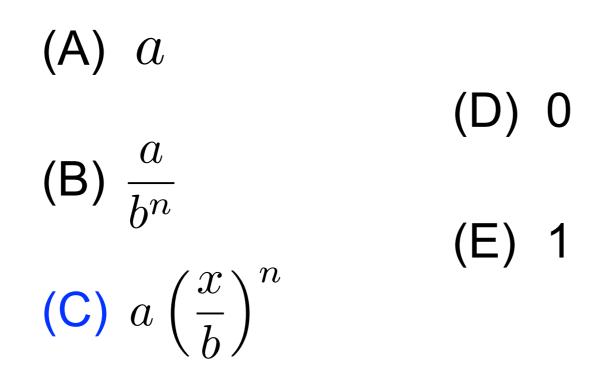
$$f(x) = \frac{ax^n}{b^n + x^n}$$

- A useful function for studying saturating phenomena.
- Important functions in biochemistry Michaelis-Menten kinetics
- We will see these several times this semester.

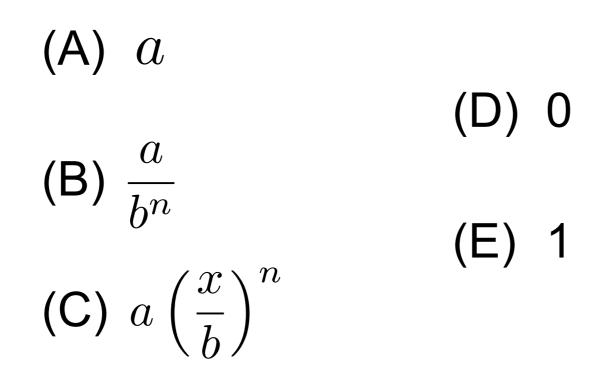
When
$$|\mathbf{x}| \ll \mathbf{b}$$
, then $f(x) = \frac{ax^n}{b^n + x^n}$



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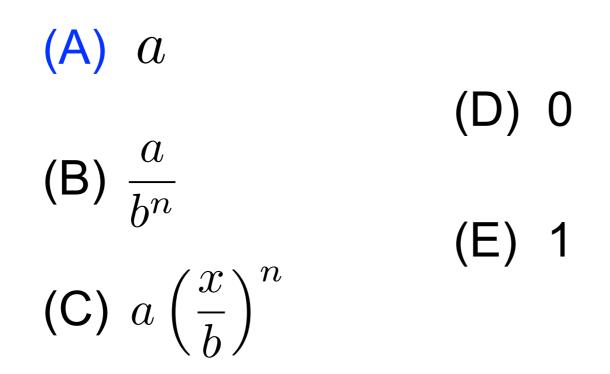


When x >> b, then
$$f(x) = \frac{ax^n}{b^n + x^n}$$

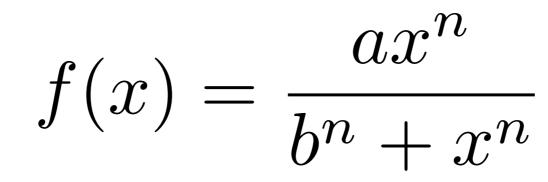


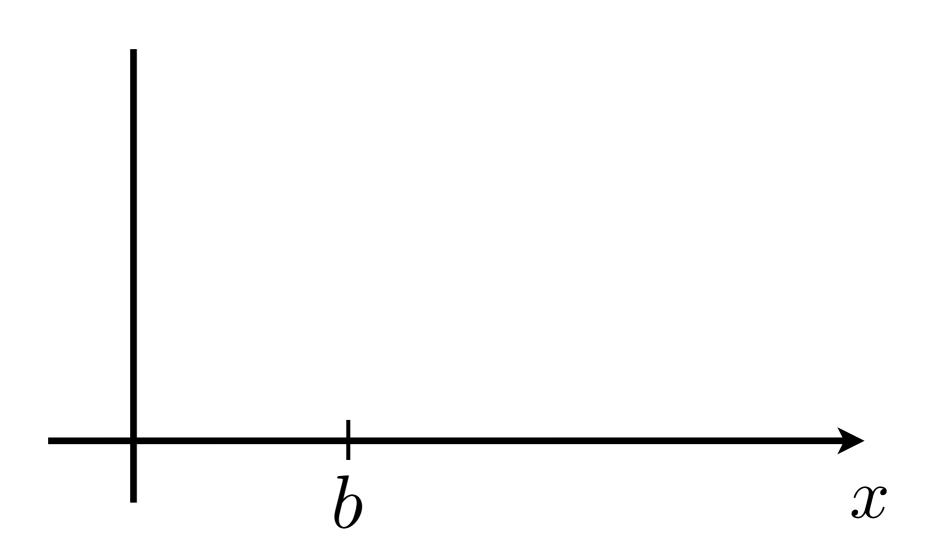
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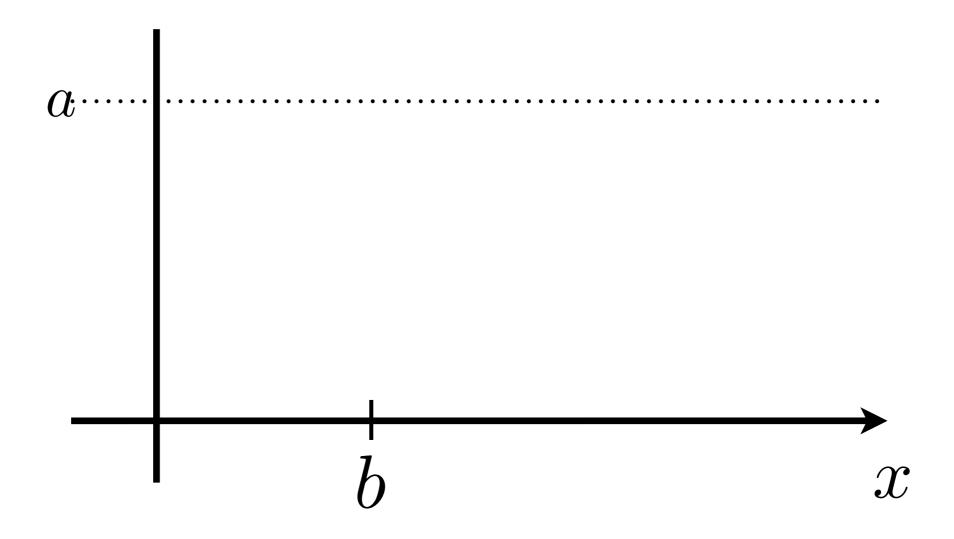


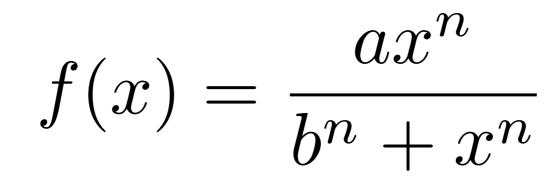
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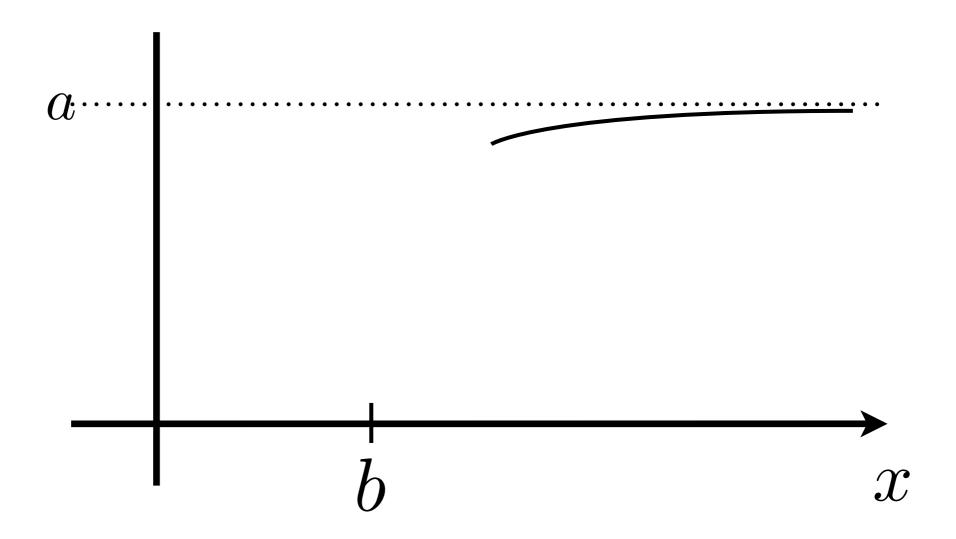


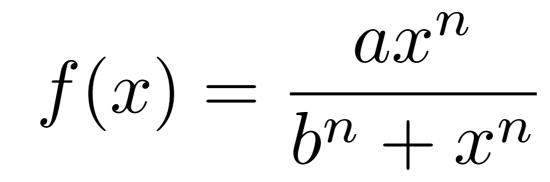


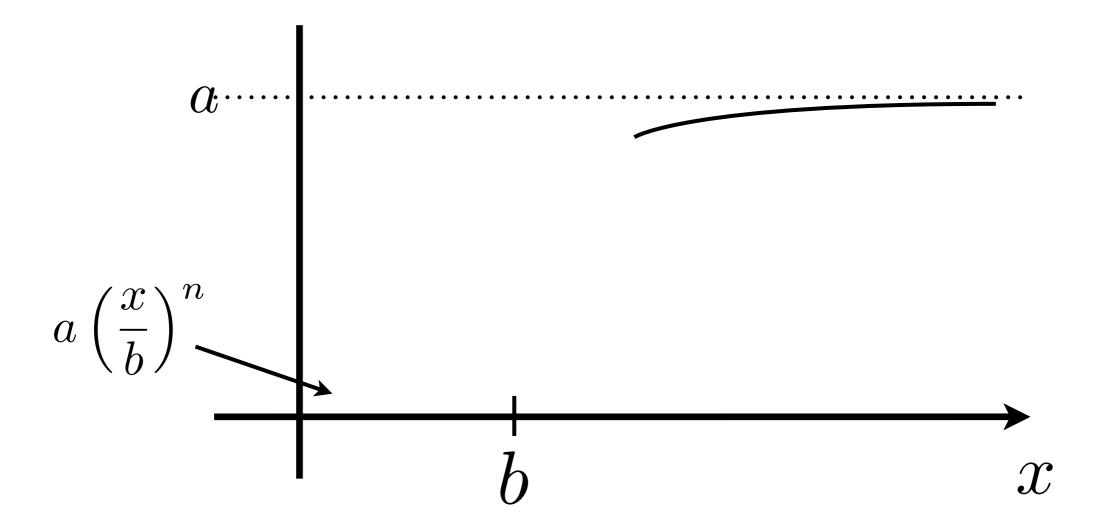
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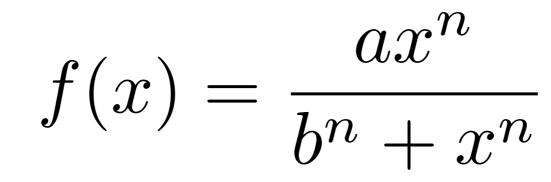


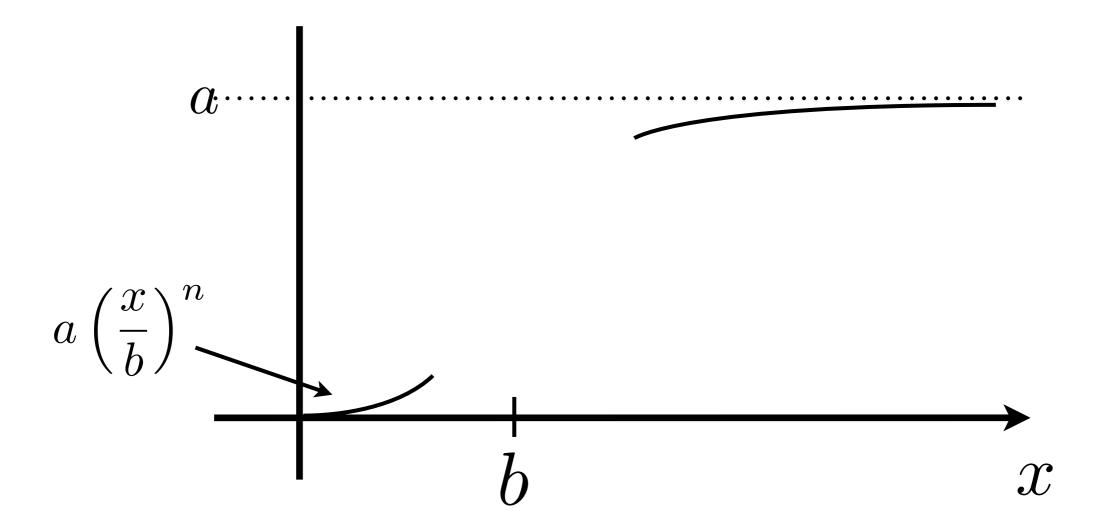


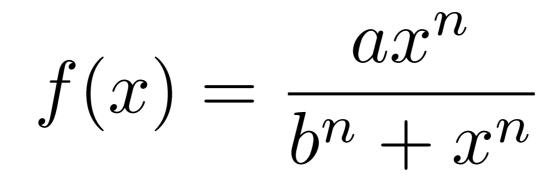


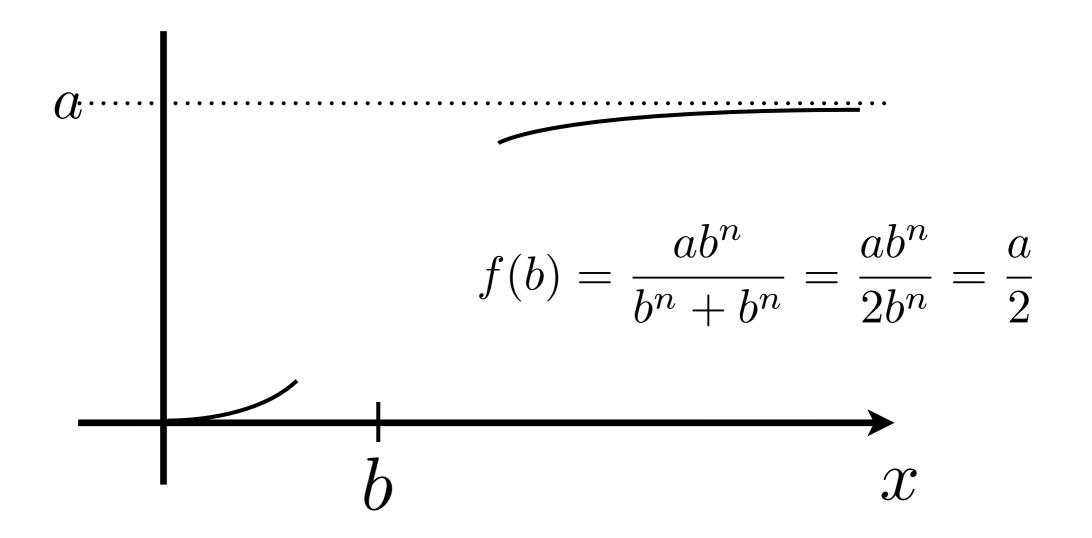


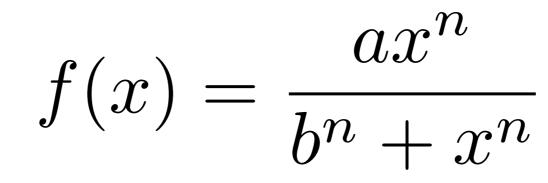


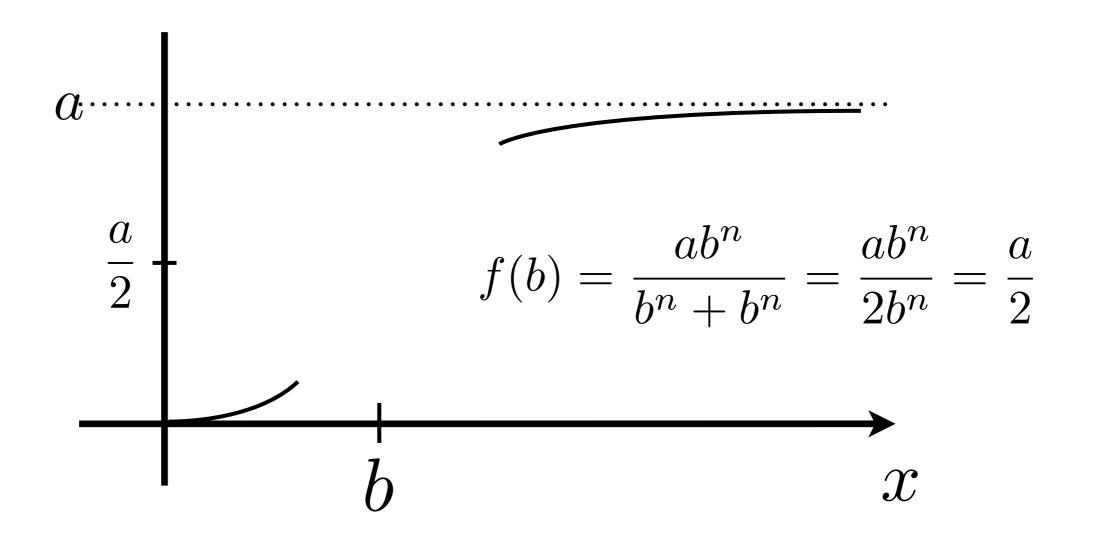


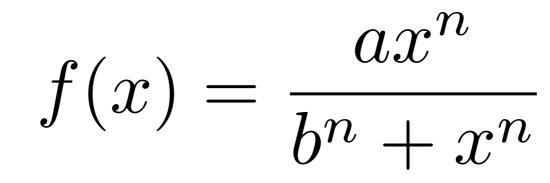


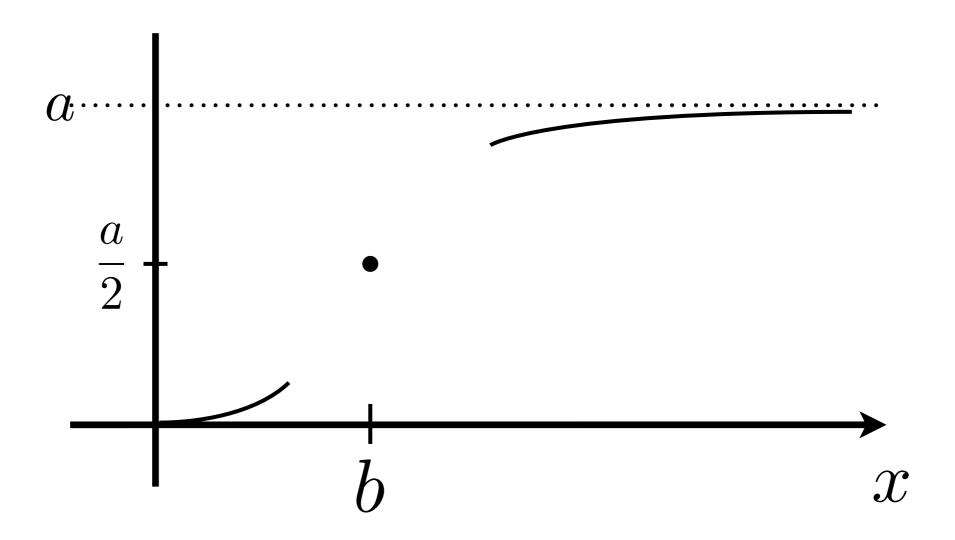


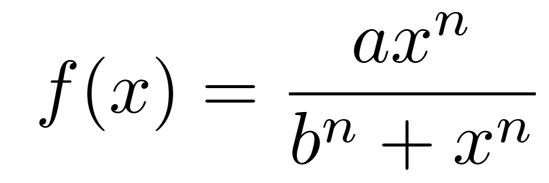


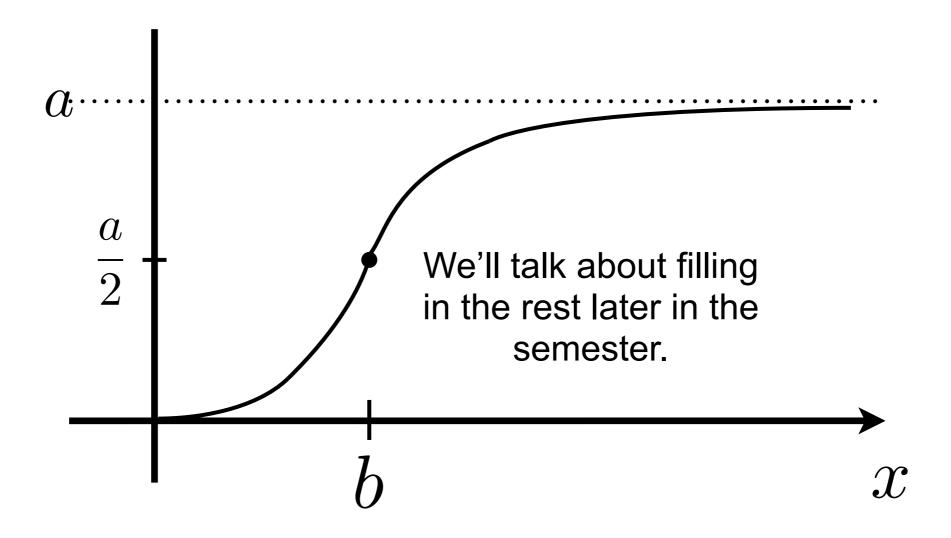






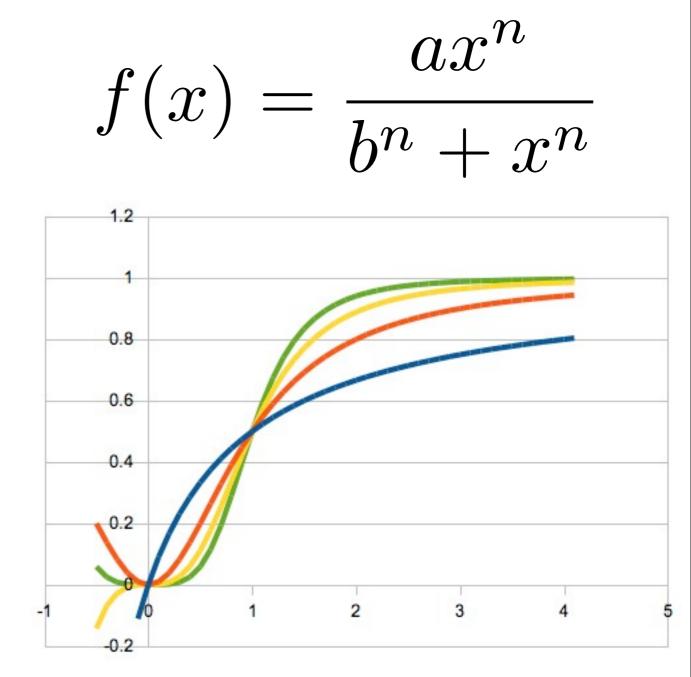






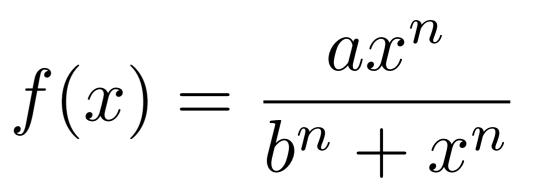
Comparing Hill functions with different n values

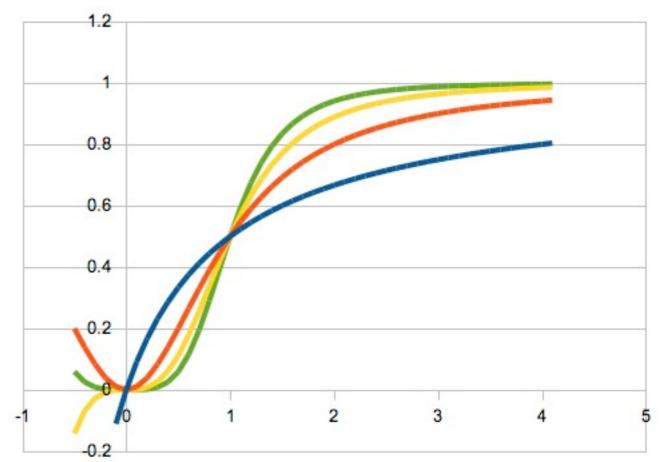
- (A) Green: n=2, yellow: n=3, red: n=4, blue: n=5.
- (B) Green: n=4, yellow: n=3, red: n=2, blue: n=1.
- (C) Green: n=5, yellow: n=4, red: n=3, blue: n=2.
- (D) Either (B) or (C) (not enough info).



Comparing Hill functions with different n values

- (A) Green: n=2, yellow: n=3, red: n=4, blue: n=5.
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What is the slope of the line connecting the points?

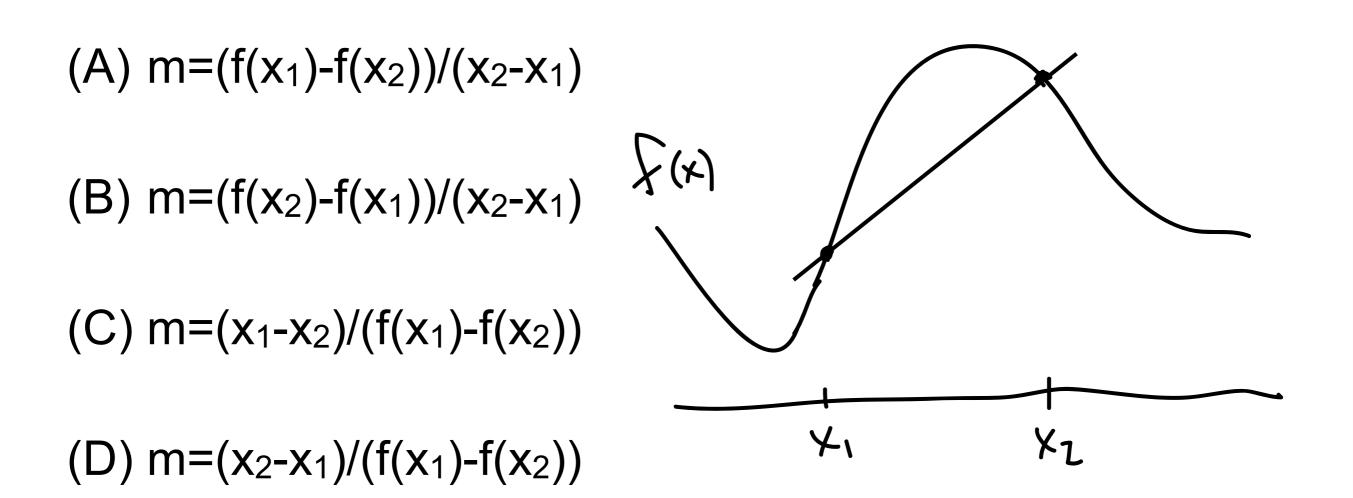
(A) $m=(x_1-x_2)/(y_1-y_2)$ (B) $m=(x_2-x_1)/(y_1-y_2)$ (C) $m=(y_1-y_2)/(x_1-x_2)$ (x_1,y_1) (D) $m=(y_2-y_1)/(x_2-x_1)$

What is the slope of the line connecting the points?

(A) $m=(x_1-x_2)/(y_1-y_2)$ (B) $m=(x_2-x_1)/(y_1-y_2)$ (C) $m=(y_1-y_2)/(x_1-x_2)$ (x_1, y_1)

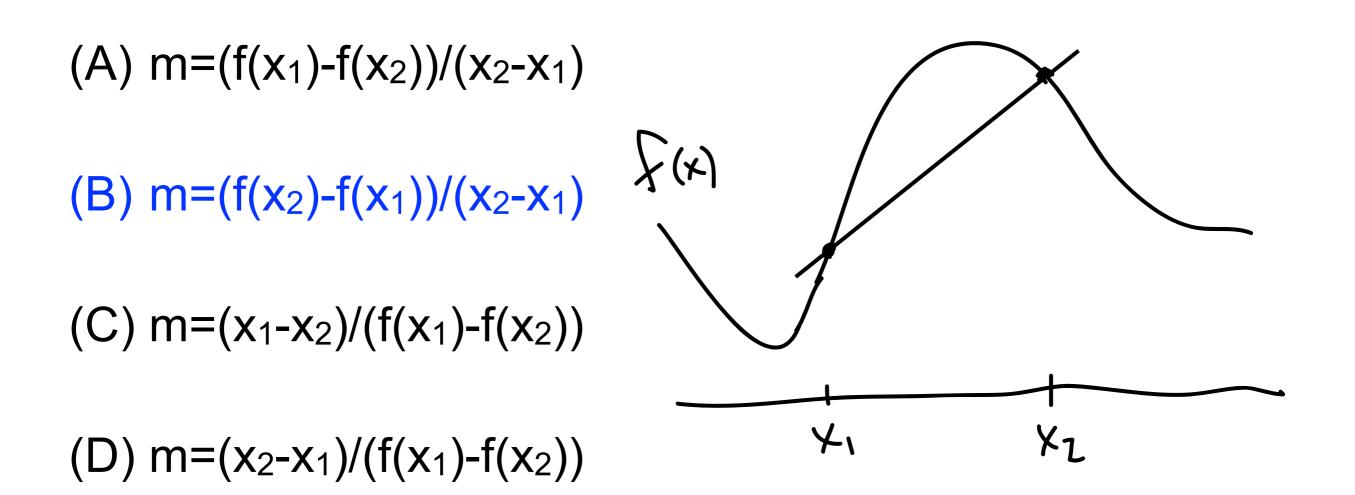
(D) $m=(y_2-y_1)/(x_2-x_1)$

What is the slope of the secant line to the graph of f(x)?

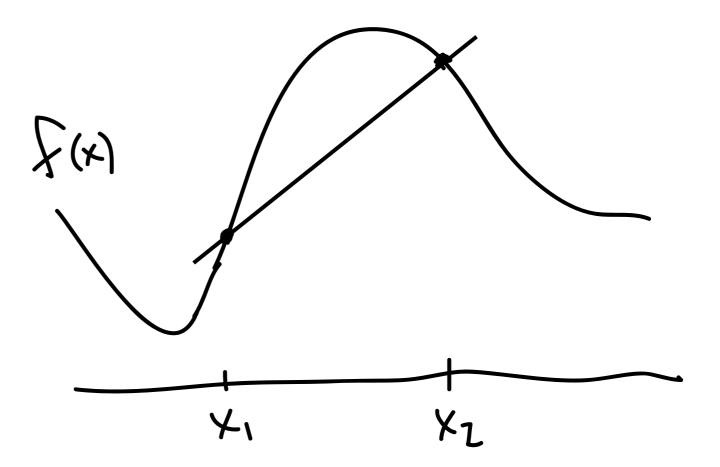


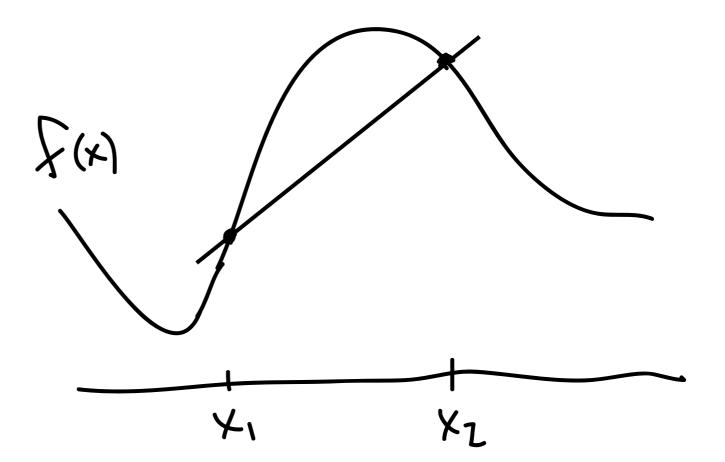
Slope of secant line = average rate of change from x_1 to x_2 .

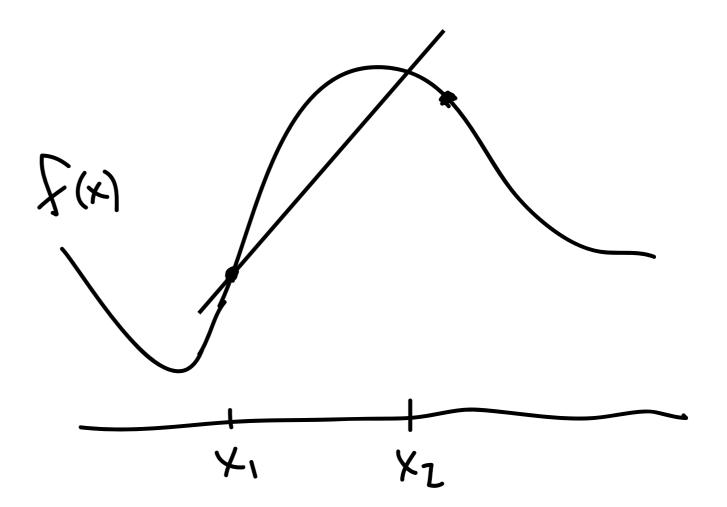
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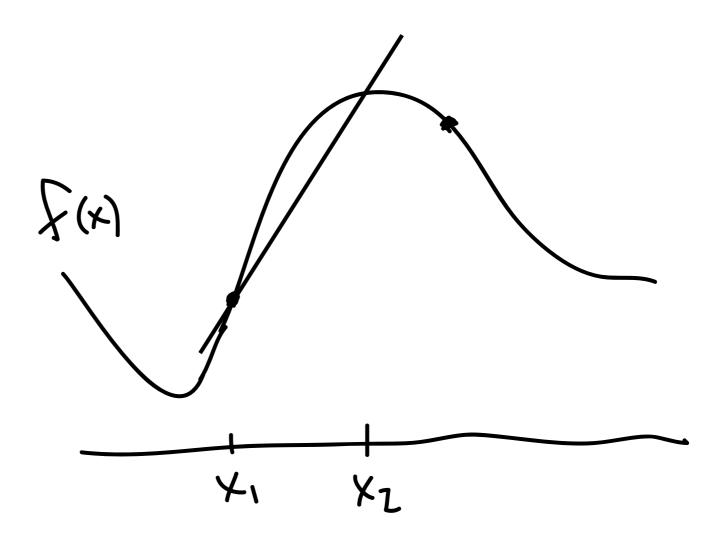


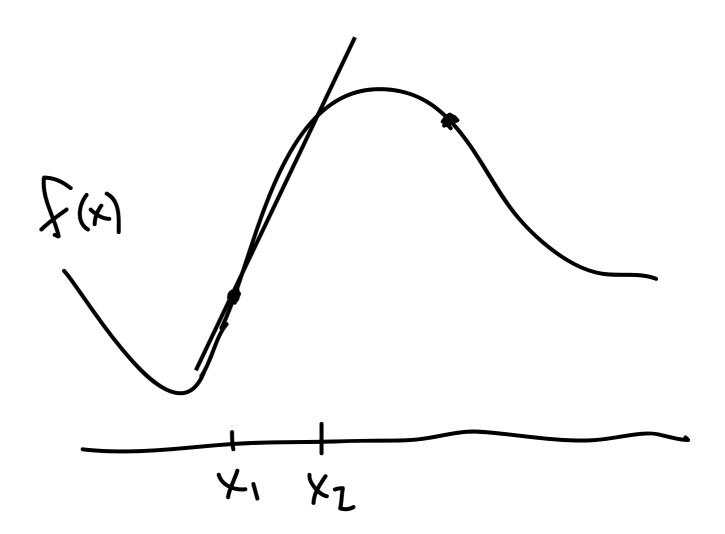
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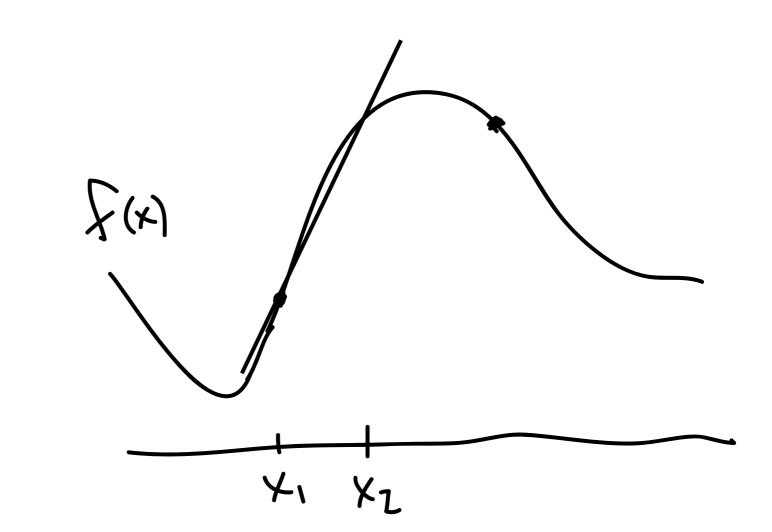








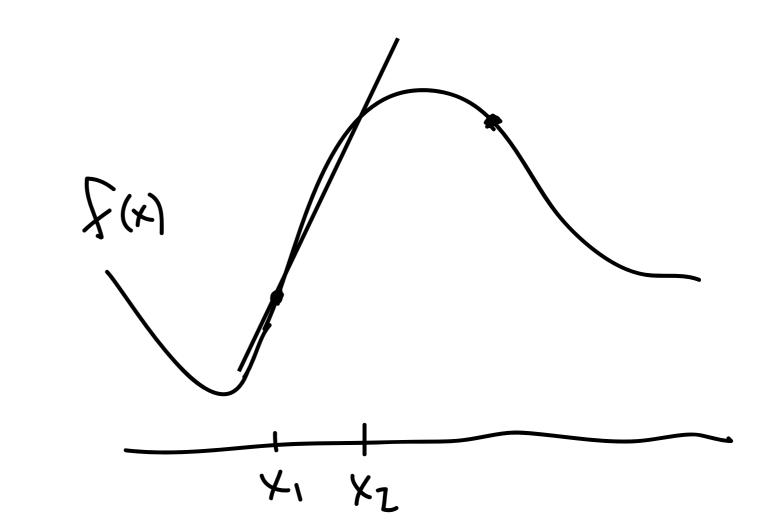
Take a point x_2 so that the secant line is closer to the "secant line" AT x_1 .



Alternate notation: let $x_2 = x_1 + h$ so that

$$m = \frac{f(x_2) - f(x_1)}{x_2 - x_1}$$

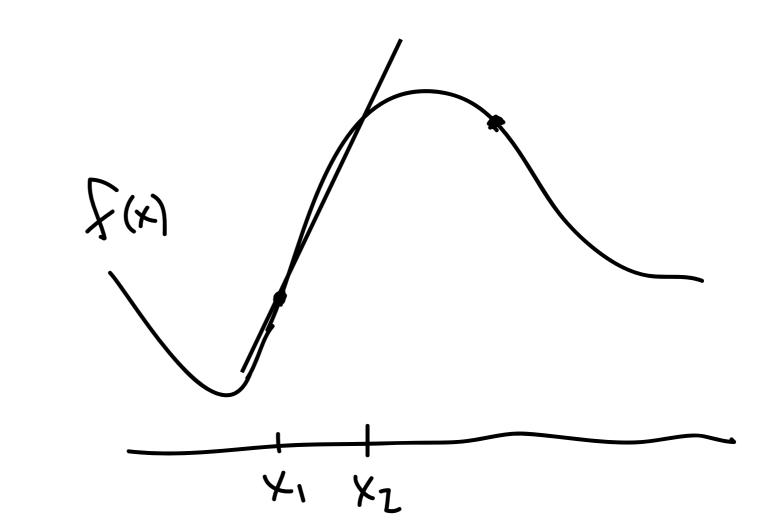
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Alternate notation: let $x_2 = x_1 + h$ so that

$$m = \frac{f(x_2) - f(x_1)}{x_2 - x_1} = \frac{f(x_1 + h) - f(x_1)}{x_1 + h - x_1}$$

Take a point x_2 so that the secant line is closer to the "secant line" AT x_1 .



Alternate notation: let $x_2 = x_1 + h$ so that

$$m = \frac{f(x_2) - f(x_1)}{x_2 - x_1} = \frac{f(x_1 + h) - f(x_1)}{h}$$

If we take h values closer and closer to 0...

- The secant line approaches the tangent line.
- The slope of the secant line approaches the slope of the tangent line.
- We call the resulting slope the derivative at x₁.
- We now have to learn how to take limits!

slope at
$$x_1 = f'(x_1) = \lim_{h \to 0} \frac{f(x_1 + h) - f(x_1)}{h}$$