

Assignment 1 - what does your score mean?
Calculating the derivative from the definition.
Limits and continuity examples.
Reminders- OSH 2 Monday! WW2 Thurs 7AM!

Assignment 1 results and interpretation

Average across all sections: 68%

- Below 50% 88 out of 676 students (13%).
- Above 85% 162 out of 676 students (24%)
- Roughly the stats for the final marks in 102.
- If you didn't pass, think seriously about switching – talk to me if you need advice.
- If you didn't get 100% fill in your gaps asap!

A WeBWorK limit example

Guess the value of the limit (if it exists) by evaluating the function at values close to where the limit is to be done. If it does not exist, enter DNE below.



Go over f'(2) where f(x) = 1/x on the board.

Limits $f(x) \longrightarrow f(x) \longrightarrow$

Which of the following are true? (B) 2, 5

- 1. $\lim_{x \to a} f(x) = f(a)$ 4. $\lim_{x \to a} f(x)$ exists. (C) 3
- 2. $\lim_{x \to b} f(x) = f(b)$ 5. $\lim_{x \to b} f(x)$ exists. (D) 4
- 3. $\lim_{x \to c} f(x)$ does not exist. (E) 5

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Left and right limits

 The right limit at a - plug in x values approaching a from above (x>a):

$$\lim_{x \to a^+} f(x)$$

 The left limit at a - plug in x values approaching a from below (x<a):

$$\lim_{x \to a^{-}} f(x)$$

 \bullet When these exist and are equal, $\lim_{x \to a} f(x)$ exists

$$\lim_{x \to a} f(x) = \lim_{x \to a^+} f(x) = \lim_{x \to a^-} f(x).$$

Limits



(A)
$$\lim_{x \to a} f(x) = 2$$

(B) $\lim_{x \to b^{-}} f(x) = 3$
(C) $\lim_{x \to a} f(x) = 3$

(D) $\lim_{x \to b} f(x) = 3$

(E) $\lim_{x \to b^+} f(x)$ does not exist

Limits



(A)
$$\lim_{x \to a} f(x) = 2$$

(B) $\lim_{x \to b^{-}} f(x) = 3$
(C) $\lim_{x \to a} f(x) = 3$

(D)
$$\lim_{x \to b} f(x) = 3$$

(E) $\lim_{x \to b^+} f(x)$ does not exist

Continuity

When $\lim_{x\to a} f(x)$ exists and $\lim_{x\to a} f(x) = f(a)$ we say that f(x) is continuous at x=a.



f(x) is continuous at all x except at x=a and x=b.

Continuous functions

- Examples of categories of continuous functions:
 - Polynomials
 - Exponentials
 - sin, cos
- These are all continuous for all real x.
- Desmos example...

Ensuring continuity

For what value of a is the following function continuous?

$$f(x) = \begin{cases} 4 - a^2 + 3x & x < 1 \\ x^2 + ax & x \ge 1 \end{cases}$$

(A) a = 3(B) a = -3(C) a = 0(D) a = 1(E) Don't know.

Ensuring continuity

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Types of limits we'll talk about

- Points of continuity: $\lim_{x \to a} f(x) = f(a)$
- Hole-in-the-graph (like derivative limit)
- Limits at $\pm\infty$ (horizontal asymptotes)



(A) 3 (B) -3 (C) Not defined. (D) ∞

(E) Don't know.



(A) 3 (B) -3 (C) Not defined. Limit at a point of continuity. (D) ∞ (E) Don't know.



(A) 0

(B) ∞

(C) 1

(D) 4

(E) Don't know.



Is
$$\lim_{x \to 2} \frac{x^2 - 4}{x - 2}$$
 actually the

derivative of some function?

(for you to think about)

What is
$$\lim_{x \to \infty} \frac{5x^3 + 3x^2 - x + 1}{2x^4 - x^2 + 2}$$
?

(A) 0

$$\frac{5x^3 + 3x^2 - x + 1}{2x^4 - x^2 + 2} \approx \frac{5x^3}{2x^4} = \frac{5}{2x}$$
(B) ∞

(C) 5/2

Use asymptotics to simplify top and bottom.

(D) 1/2

(E) Don't know.

What is
$$\lim_{x \to \infty} \frac{5x^3 + 3x^2 - x + 1}{2x^4 - x^2 + 2}$$
?

(B) ∞

(C) 5/2

(D) 1/2

(E) Don't know.

Friday, September 12, 2014