

# Today

- Reminders:

- Assignment 4a on Tues 7am,

- Assignment 4b on Fri 5pm,

- Midterm 1 on Tues 6pm.

- S.101 – HENN 200,

- S.103 – Last name A-K: BUCH A203

- S.103 – Last name L-Z: BUCH A103



# Today

- Questions about previous material
- Concavity and inflection points



# Concave up/down

- We say a function is **concave up** on some interval if  $f'(x)$  is increasing on that interval.

When  $f''(x)$  exists, same as  $f''(x) > 0$ .

- We say a function is **concave down** on some interval if  $f'(x)$  is decreasing on that interval.

When  $f''(x)$  exists, same as  $f''(x) < 0$ .



# Inflection points

• An **inflection point** of  $f(x)$  is a point at which the **concavity changes** from up to down or down to up.

• A point **a** is an **inflection point** of a function  $f(x)$  provided that **a** is a **local minimum or a local maximum of  $f'(x)$** .

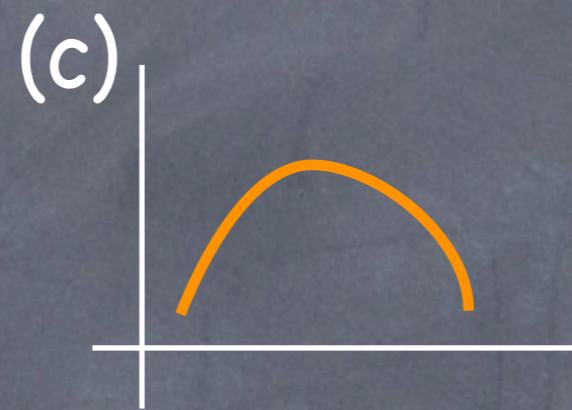
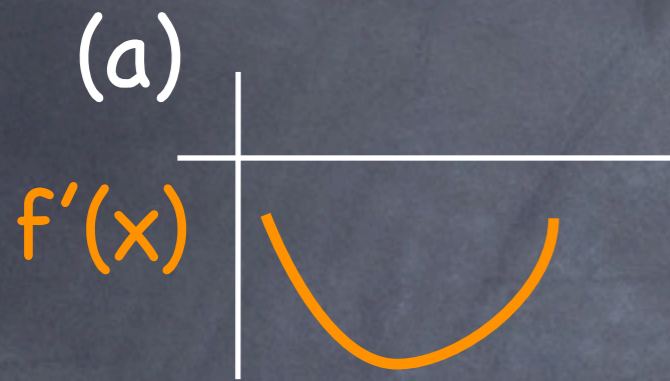
better!!



• Don't think about inflection points in terms of  $f''(x)$ !



# Match $f'(x)$ to $f(x)$



(A) 1d, 2b, 3a, 4c

(C) 1b, 2d, 3c, 4a

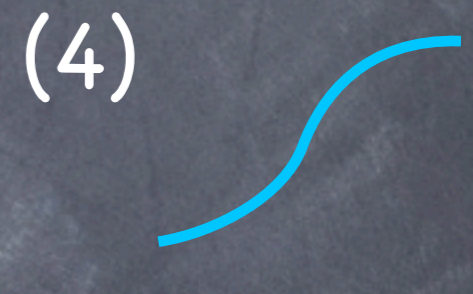
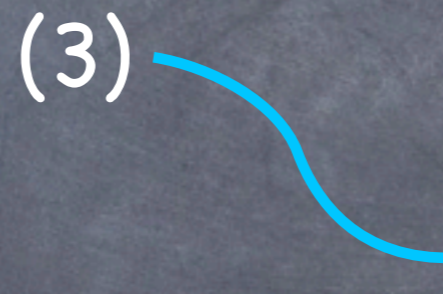
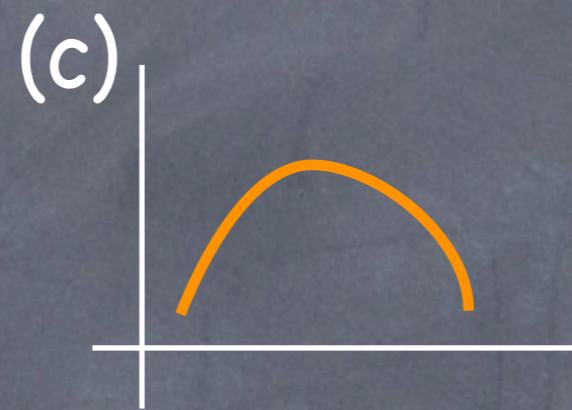
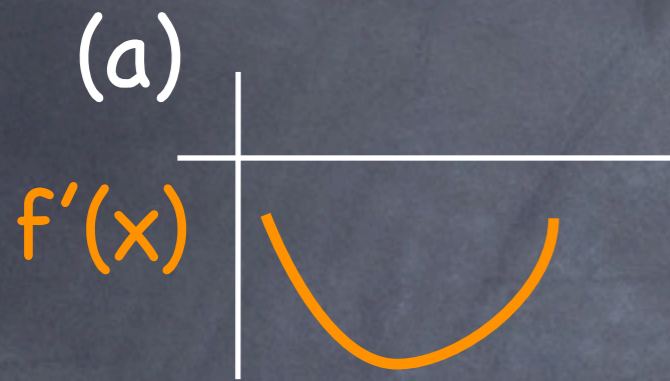
(B) 1b, 2d, 3a, 4c

(D) 1c, 2a, 3d, 4b

(E) Don't know.



# Match $f'(x)$ to $f(x)$



(A) 1d, 2b, 3a, 4c

(C) 1b, 2d, 3c, 4a

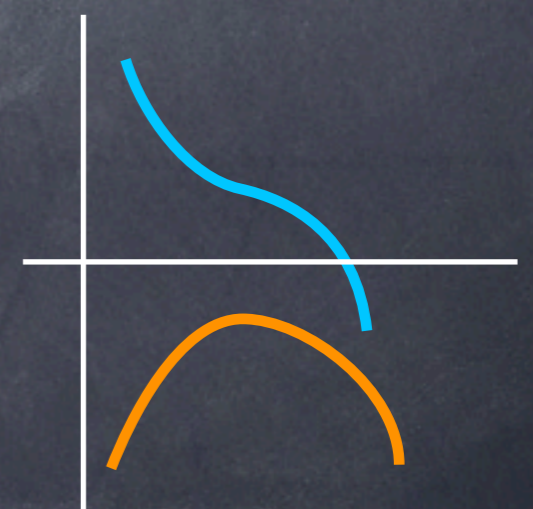
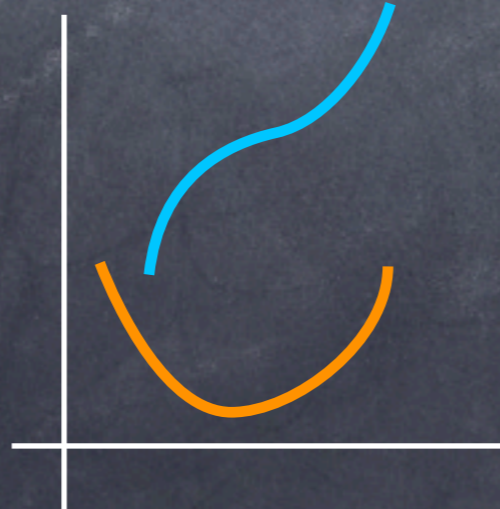
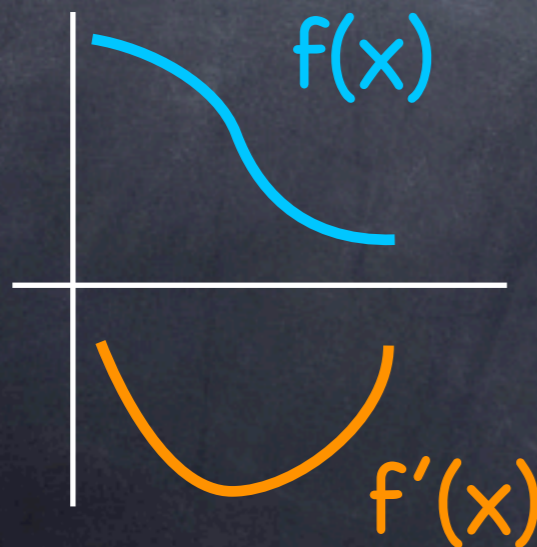
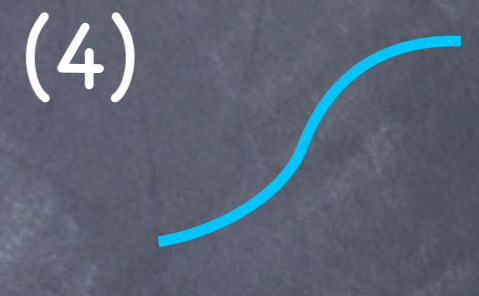
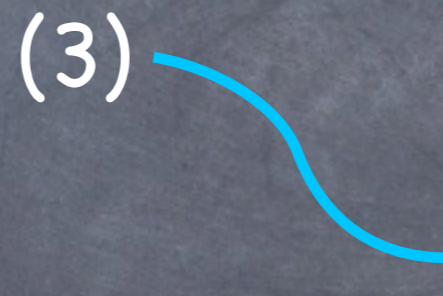
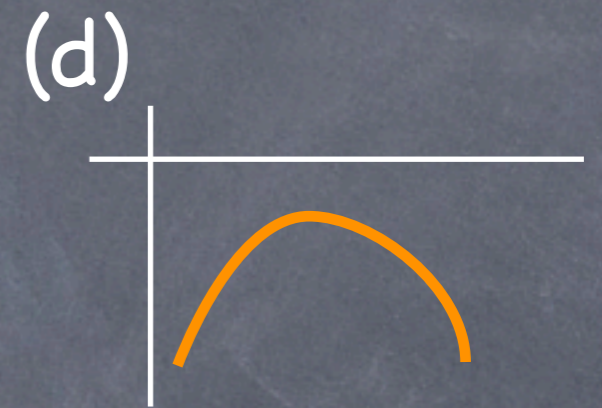
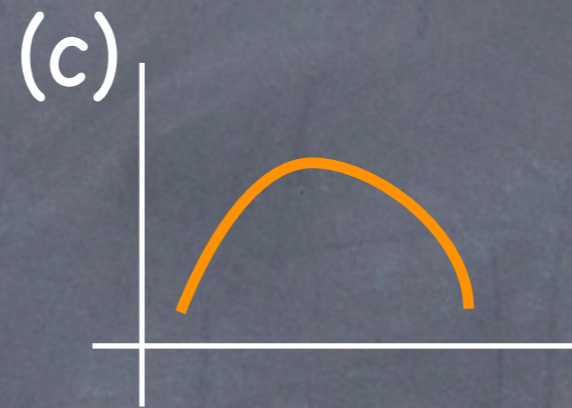
(B) 1b, 2d, 3a, 4c

(D) 1c, 2a, 3d, 4b

(E) Don't know.



# Match $f'(x)$ to $f(x)$





If you want to find a min/max of  $f'(x)$ , look for points at which. . .

- (A)  $f'(x) = 0$ .       $\rightarrow$  potential extremum of  $f(x)$
- (B)  $f'(x) = 0$  and  $f''(x) \neq 0$ .       $\rightarrow$  extremum of  $f(x)$
- (C)  $f''(x) = 0$ .       $\rightarrow$  potential extremum of  $f'(x)$
- (D)  $f''(x) = 0$  and  $f'''(x) \neq 0$ .       $\rightarrow$  extremum of  $f'(x)$
- (E) Don't know.



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- (E) Don't know.

This is "SDT" where the function considered is  $f'$  instead of  $f$ ! Would usually use "FDT".



# Potential IPs

- A potential IP is a point  $a$  at which  $f''(a)=0$  because that MIGHT be a min/max of  $f'(x)$ .
- If  $f''(x)$  changes sign at a potential IP of  $f(x)$ , then it is an IP of  $f(x)$  because it's an extrema of  $f'(x)$ .
- If  $f''(x)$  does not change sign at a potential IP of  $f(x)$ , then the potential IP is not an IP of  $f(x)$ !



# Summary

- Use  $f'(x)$  to determine intervals of **increase/decrease** of  $f(x)$ .
- Solve  $f'(x)=0$  to find **potential extrema** ( $x=a$ ). Check that  $f'(x)$  **changes sign** at  $a$  (FDT) or that  $f''(a) \neq 0$  (SDT) to make sure.
- Use  $f''(x)$  to determine intervals of **concave up/down**.
- Solve  $f''(x)=0$  to find **potential inflection points** ( $x=a$ ). Check that  $f''(x)$  **changes sign** at  $a$  ("FDT" or that  $f'''(a) \neq 0$  ("SDT")) to make sure.