

# Today

- Midterm comments
- Trig review
- Rhythmic processes



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- Marks should appear on Connect over the weekend. Midterms available for pickup starting Tuesday (10am-11:30, 12-2)



# Trig review

- The SI convention for the units used for angles is radians, not degrees. Although degrees date back thousands of years they are less convenient, for example, in calculating the arclength:

$$s = r\theta \text{ or } s = \pi r\theta/360 ?$$



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- Unless you're looking at a map.
- Or baking.



# Trig review

$$\sin(2\pi/3) =$$

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(B)  $-\frac{\sqrt{3}}{2}$

(C)  $\frac{1}{2}$

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(A)  $\cos(\arctan(\sqrt{3})) = 1/2$

(B)  $\sin(\arccos(1/2)) = \sqrt{3}/2$

(C)  $\arctan(1) = \pi/4$

(D)  $\arcsin(1/2) = \pi/3$

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# Trig review

Which is true for all  $x$  and  $y$ ?

(A)  $\sin(x+y) = \sin(x)\cos(y) + \sin(y)\cos(x)$

(B)  $\sin(x+y) = \sin(x)\sin(y) + \cos(x)\cos(y)$

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- The **phase shift** is the angle when  $t=0$  (e.g.  $\sin(2t+\pi/4)$ ).
- The **time-shift** is the time at which the argument of the trig function is 0.



# Trig review

What is the period of  $h(t) = 8 - 6\sin(4t+1)$ ?

(A) 4

(B) 1

(C)  $1/4$

(D)  $2\pi$

(E)  $\pi/2$



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Period of  $\sin(x)$  is  $2\pi$  so...

- When is  $(4t+1)=0$ ?
- When is  $(4t+1)=2\pi$ ?
- Difference between these  $t$  values is the period.
- (Same as  $4t=2\pi$ .)



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(D) 6

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•  $h(t)$  goes from a low of  $8-6$  to a high of  $8+6$  so the amplitude is 6.



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- Rewrite as  $h(t) = 8 - 6\sin(4(t+1/4))$  to see  $h(t)$  is a sin shifted by  $1/4$ .
- By some definitions, time-shift is  $-1/4$ .