

Chain ruleRelated rates examples

# Choose $f(t_p) = t_p^2$ Find $t_p$ that maximizes $R_{avg} = nt_p^2 / (nt_p + t_0)$

(A)  $t_p = -2nt_0$ (B)  $t_p = 0$ (C) Never leave. "maximum"  $t_p$ 



Think and/or sketch before you calculate.

If f(x) = 2x+3 and g(x) = -4x+2, (A) h(x) = f(g(x)) = -8x+7(B) h(x) = f(g(x)) = -8x-10(C)  $h(x) = f(g(x)) = -8x^2-8x+6$ (D) h(x) = f(g(x)) = -8x+5

If f(x) = 2x+3 and g(x) = -4x+2, (A) h(x) = f(g(x)) = -8x+7(B) h(x) = f(g(x)) = -8x-10(C)  $h(x) = f(g(x)) = -8x^2-8x+6$ (D) h(x) = f(g(x)) = -8x+5

If h(x)= f(g(x)), then
(A) h'(x) = f'(x)g'(x)
(B) h'(x) = f'(x)g(x) + f(x)g'(x)
(C) h'(x) = f'(g'(x))
(D) h'(x) = f'(g(x))g'(x)

If h(x)= f(g(x)), then
(A) h'(x) = f'(x)g'(x)
(B) h'(x) = f'(x)g(x) + f(x)g'(x)
(C) h'(x) = f'(g'(x))
(D) h'(x) = f'(g(x))g'(x)

For f(x) = 2x+3 and g(x) = -4x+2,If h(x) = f(g(x)), then h'(x) = -8! But... (A) h'(x) = f'(x)g'(x) ----- h'(x) = 2(-4)(B)  $h'(x) = f'(x)g(x) + f(x)g'(x) ---> \begin{bmatrix} h'(x) = 2(-4x+2) \\ + (2x+3)(-4) \end{bmatrix}$ (C) h'(x) = f'(g'(x)) -----> h'(x) = 2(D) h'(x) = f'(g(x))g'(x) -----> h'(x) = 2(-4)

Come up with an f and g that violate (A)!

#### Related rates

Quantity 1 depends on quantity 2 and quantity 2 depends on a third quantity (e.g. time):  $Q_1(Q_2(t))$ 

Given the rate of change of one of them, find the rate of change of the other.

Which is the relevant equation relating the quantities (not rates of change yet)?

(A)  $V = 4/3 \pi r^3$ (B)  $V' = 4 \pi r^2 k$ (C)  $V' = 4 \pi k^2$ (D)  $V = 4/3 \pi k^3$ 

Which is the relevant equation relating the quantities (not rates of change yet)?

#### (A) V = $4/3 \pi r^3$

(B) V' =  $4 \pi r^2 k$ (C) V' =  $4 \pi k^2$ (D) V =  $4/3 \pi k^3$ 

Which is the relevant equation relating the rates of change?

(A)  $V = 4/3 \pi r^3$ (B)  $V' = 4 \pi r^2 k$ (C)  $V' = 4 \pi k^2$ (D)  $V = 4/3 \pi k^3$ 

Which is the relevant equation relating the rates of change?

(A)  $V = 4/3 \pi r^3$ (B)  $V' = 4 \pi r^2 k$ (C)  $V' = 4 \pi k^2$ (D)  $V = 4/3 \pi k^3$ 

(A)  $V' = 4 \pi k$ (B)  $V' = 4 \pi k^2$ (C)  $V' = 4/3 \pi$ (D)  $V' = 4/3 \pi k^3$ 

#### (A) $V' = 4 \pi k$

(B) V' =  $4 \pi k^2$ (C) V' =  $4/3 \pi$ (D) V' =  $4/3 \pi k^3$  Water is leaking out of a conical cup of height H and radius R. Find the rate of change of the height of water in the cup when the cup is full, if the volume is decreasing at a constant rate, k.

Which is the relevant equation relating the quantities (not rates of change yet)?

(A)  $V = 1/3 \pi R^2 H$ (B)  $V = 1/3 \pi (R^2/H^2) h$ (C)  $V = 1/3 \pi (R^2/H^2) h^3$ (D)  $V = 1/3 \pi r^2 h$ 



Water is leaking out of a conical cup of height H and radius R. Find the rate of change of the height of water in the cup when the cup is full, if the volume is decreasing at a constant rate, k.

Which is the relevant equation relating the quantities (not rates of change yet)?

(A) V =  $1/3 \pi R^2 H$ (B) V =  $1/3 \pi (R^2/H^2) h$ (C) V =  $1/3 \pi (R^2/H^2) h^3$ (D) V =  $1/3 \pi r^2 h$ 



Continued next lecture...