

# Today

- $\ln(x)$  as inverse function for  $e^x$ .
- Derivative of  $\ln(x)$ .



What is the definition of the inverse function of  $f(x)$ ?

- (A) The function  $g(x)$  for which  $g(f(x))=x$ .
- (B) The function whose graph is the mirror image of graph of  $f(x)$  in the line  $y=x$ .
- (C)  $1/f(x)$
- (D)  $-f(x)$



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What is the domain of

$$f(x) = e^x?$$

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(B) All  $x > 0$ .

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Let  $f(x)=e^x$ . Define  $\ln(x)$   
to be  $f^{-1}(x)$ .

Which of the following is false?

(A) If  $a=e^b$  and  $c=e^d$  then  $\ln(a/c) = b-d$ .

(B) If  $a=e^b$  and  $c=e^d$  then  $\ln(a-c) = b/d$ .

(C) If  $c=a^d$  then  $\ln(c) = d \ln(a)$ .

(D) If  $a=e^b$  and  $c=a^d$  then  $\ln(c) = bd$ .

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$$f(x) = \ln(x)$$

$$\longrightarrow f'(x) = 1/x$$

• Solve for  $y'$ :  $y' = e^{-y} = 1/x$