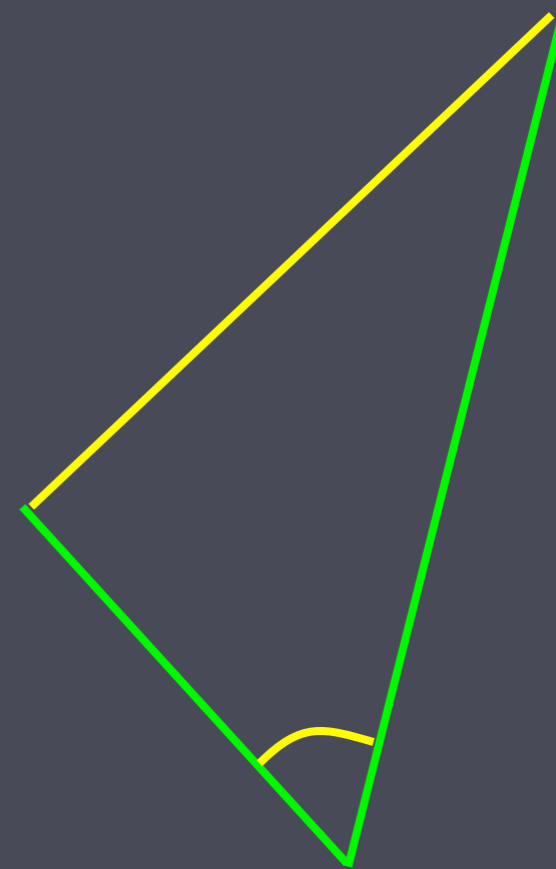


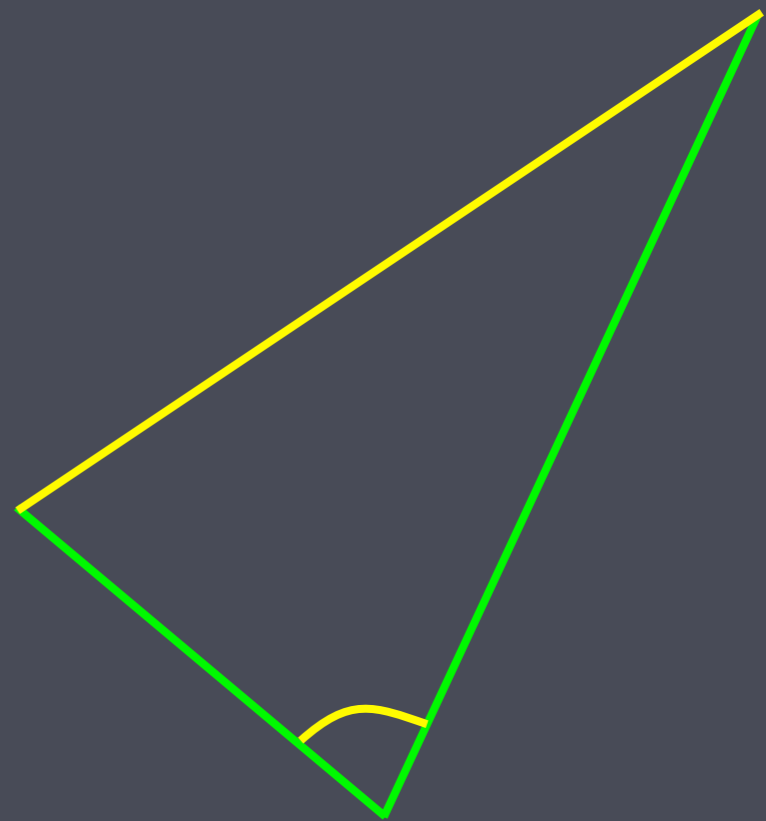
Today

- Inverse trig review
- Derivatives of inverse (trig) functions
- Office hours next week: MWTh 1:30–3:30

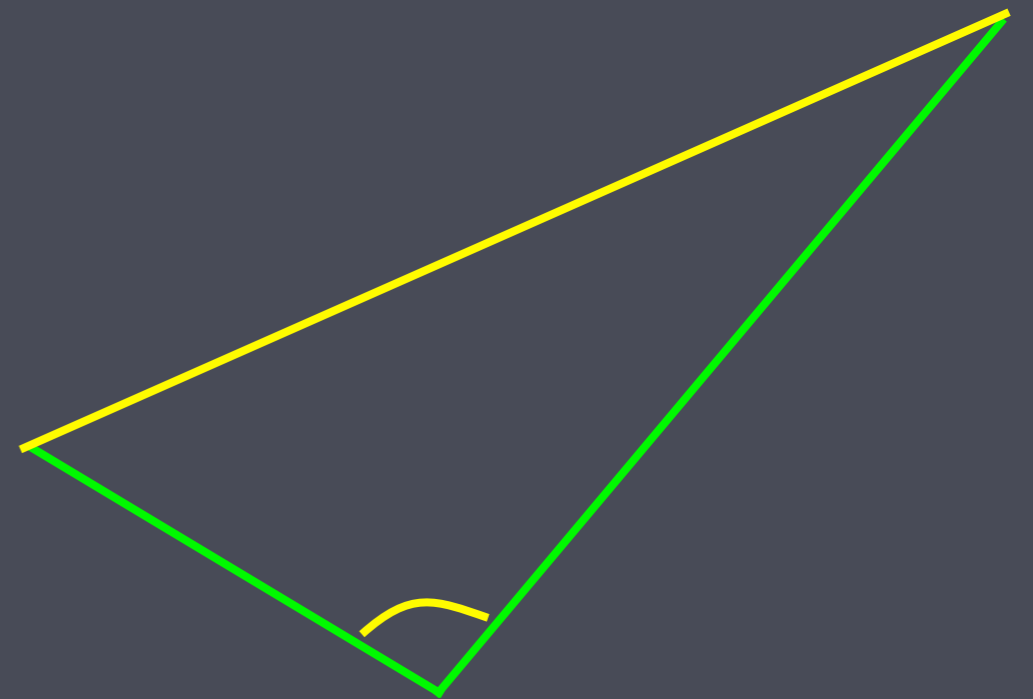
Triangle with two sides of fixed length, angle between them changes.



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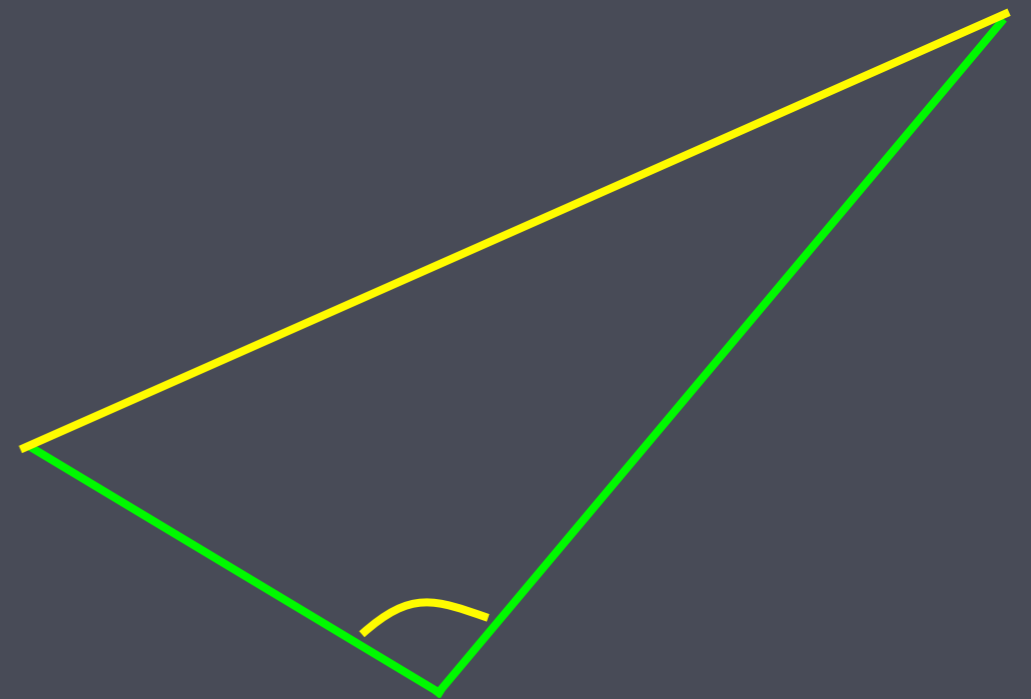
Relate the two changing quantities:

(A) $a^2 = b^2 + c^2$

(B) $a^2 = b^2 + c^2 - 2bc \cos(\theta)$

(C) $a/\sin(A) = b/\sin(B)$

(D) $\sin(\theta) = a/b$



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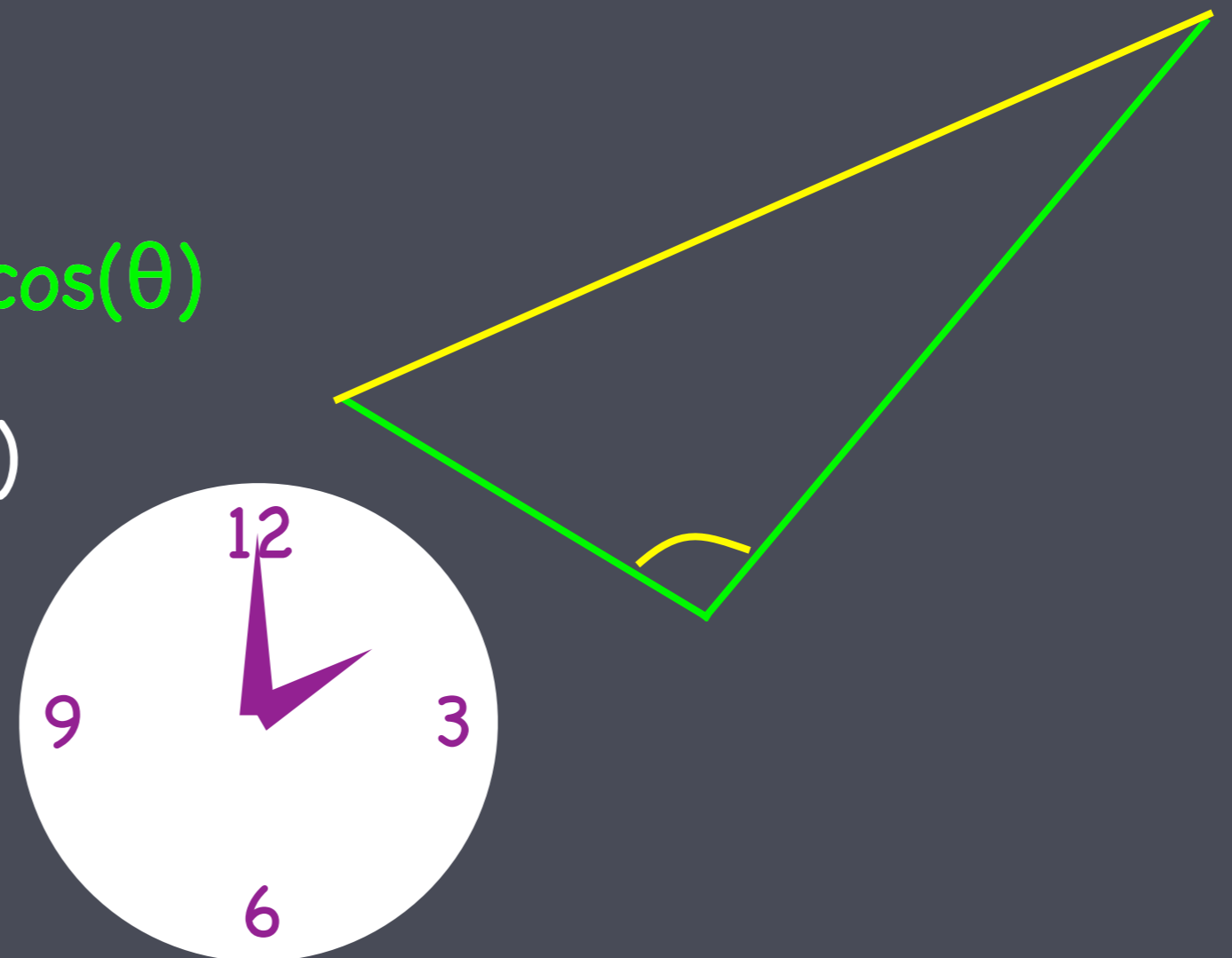
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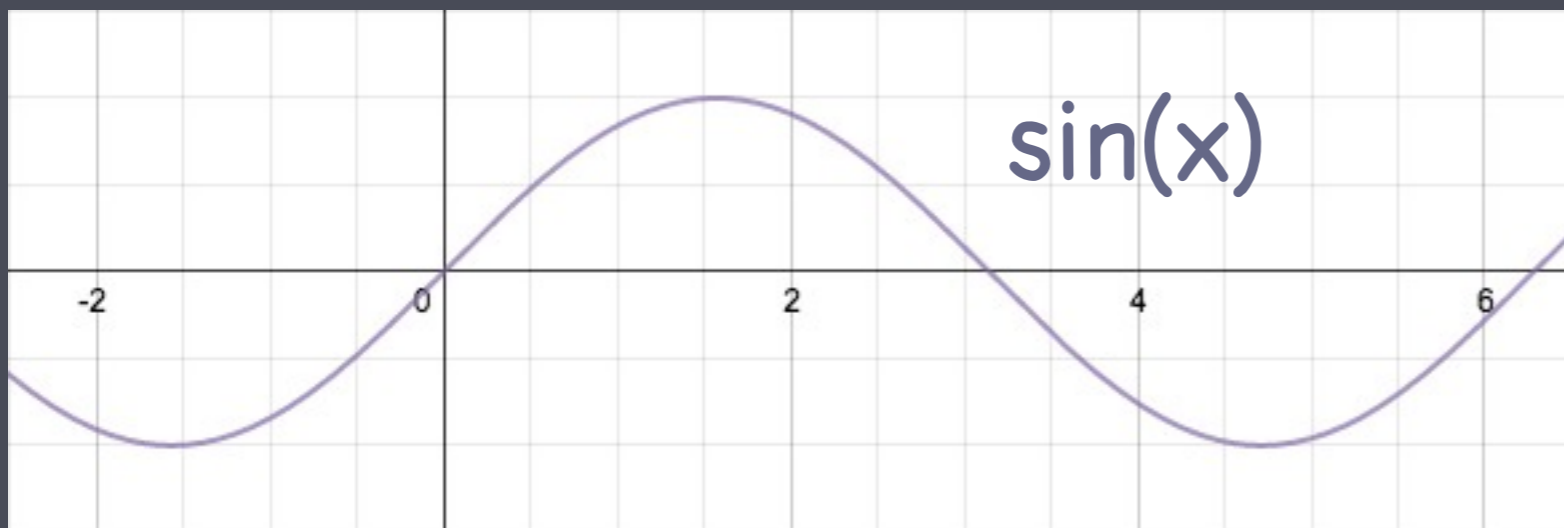
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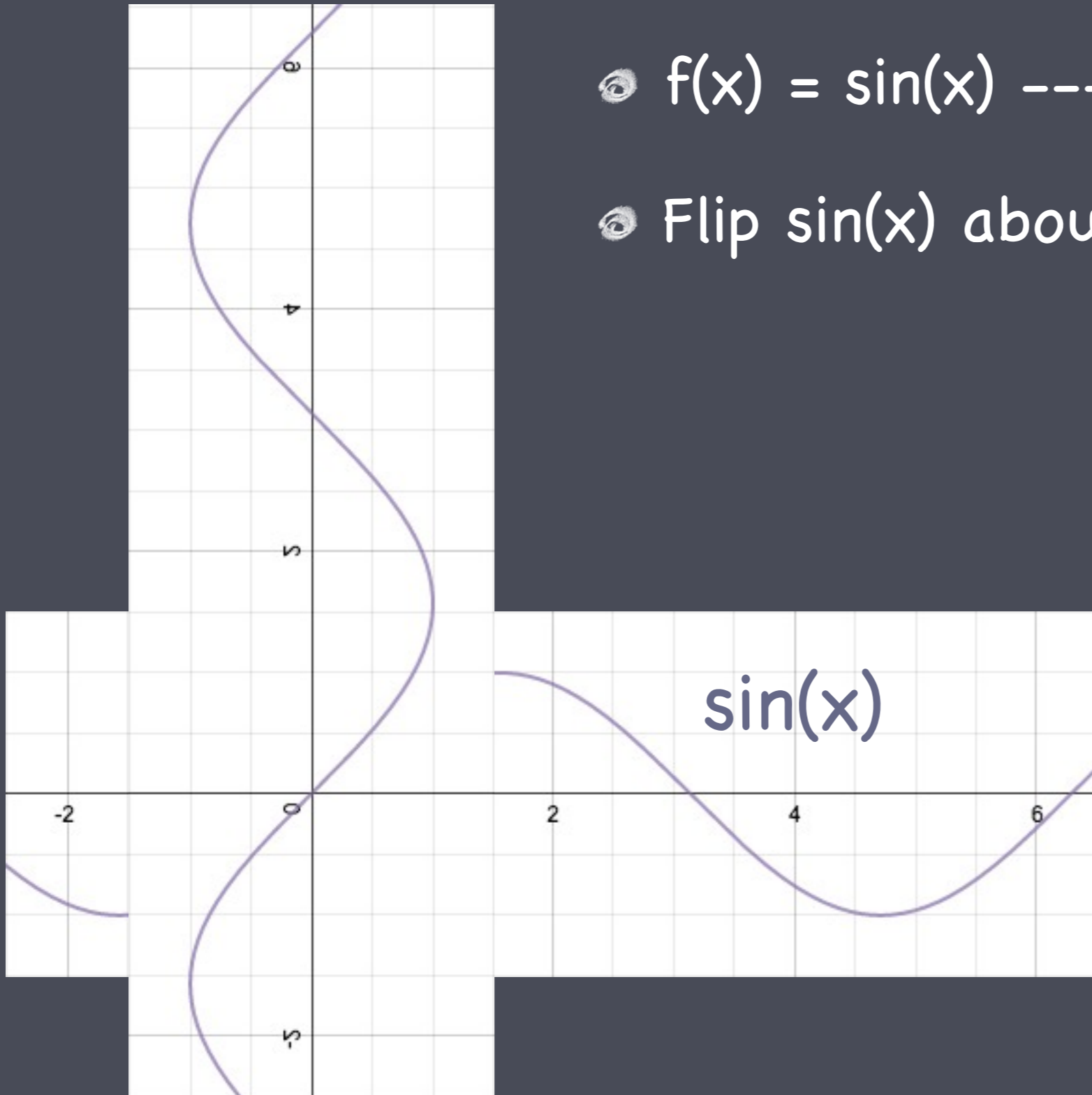
Inverse trig

• $f(x) = \sin(x) \rightarrow f^{-1}(x) = \arcsin(x)$



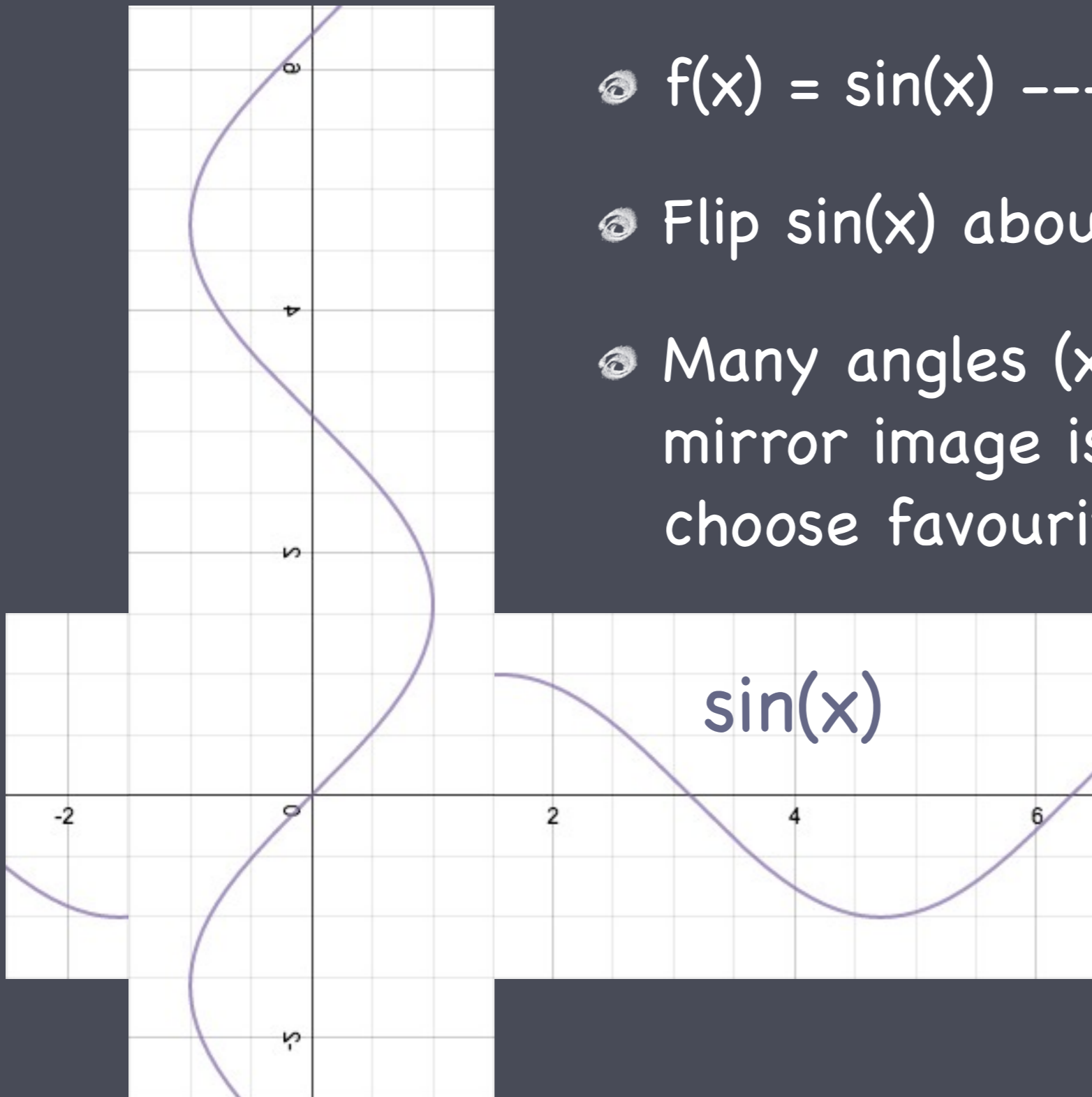
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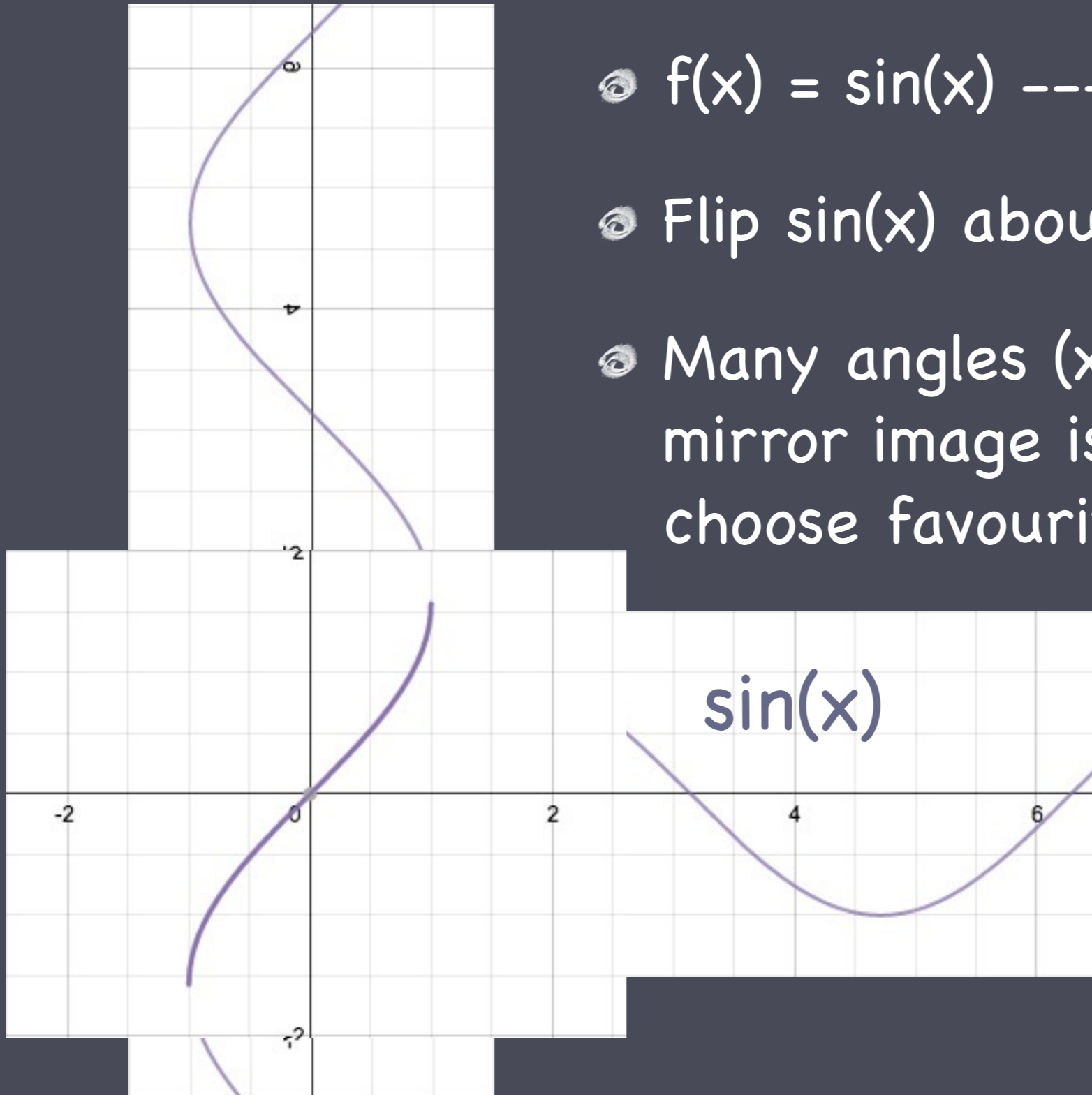
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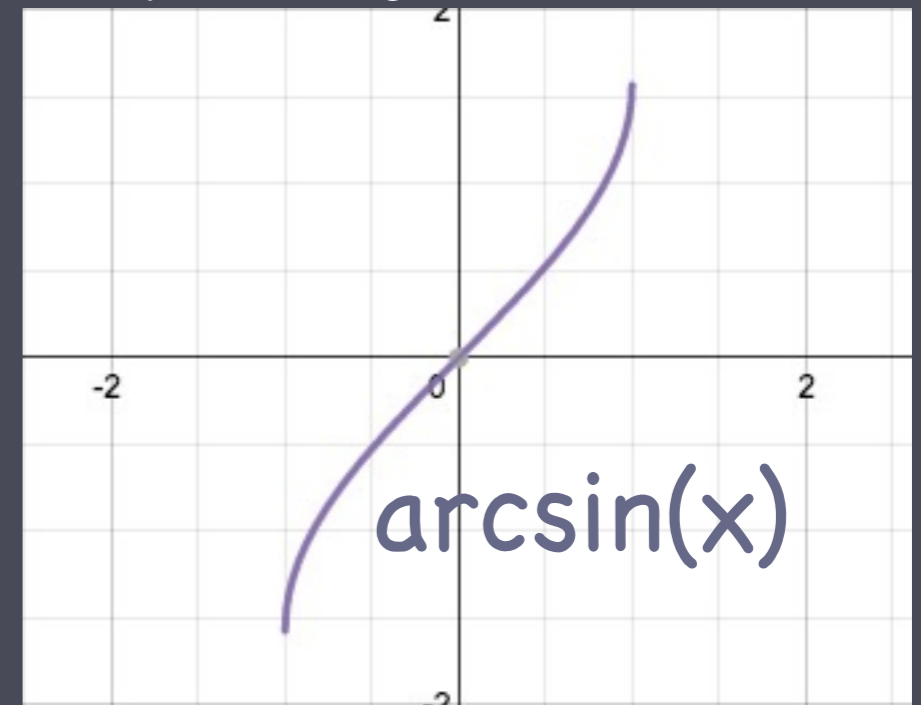
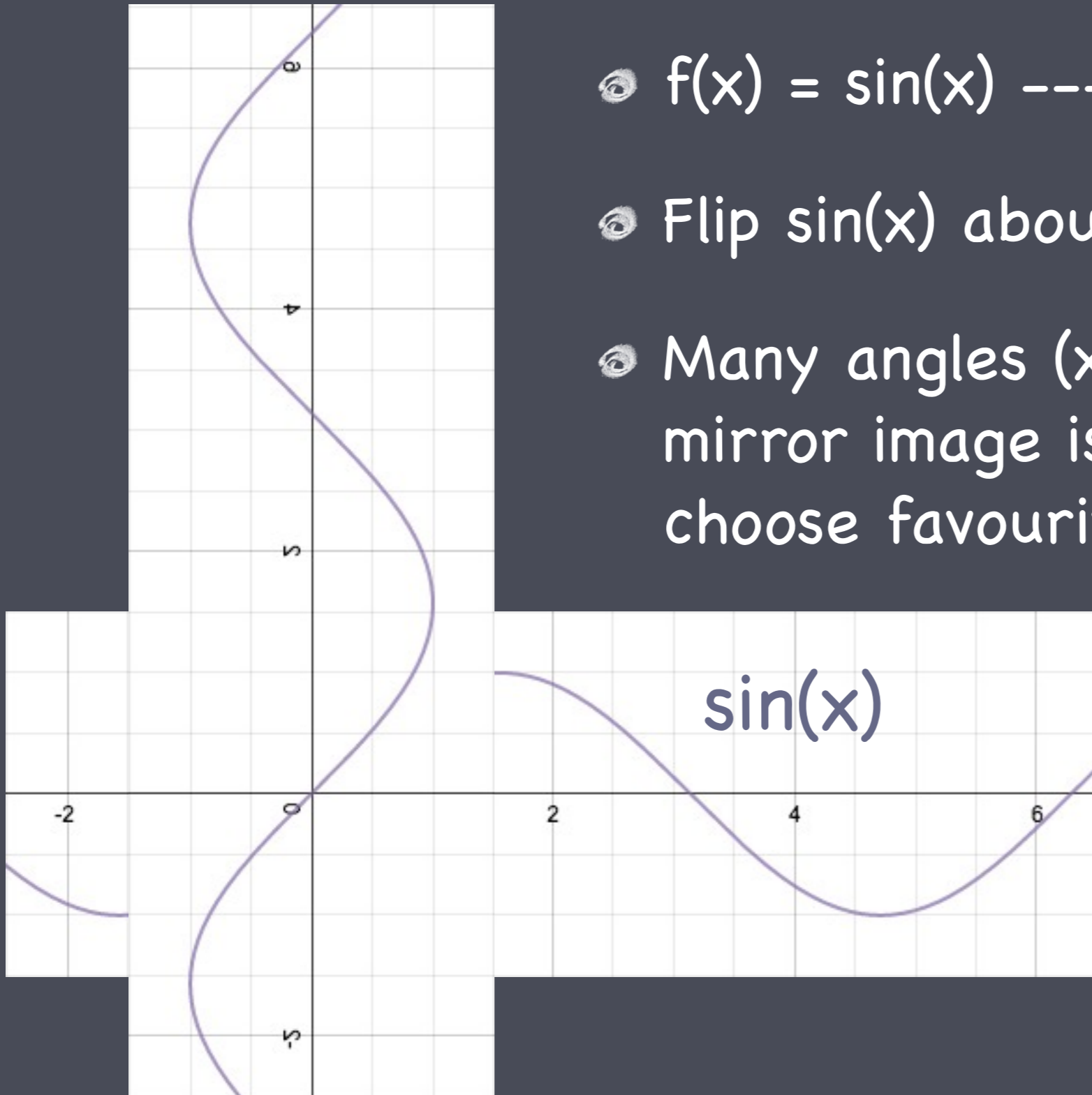
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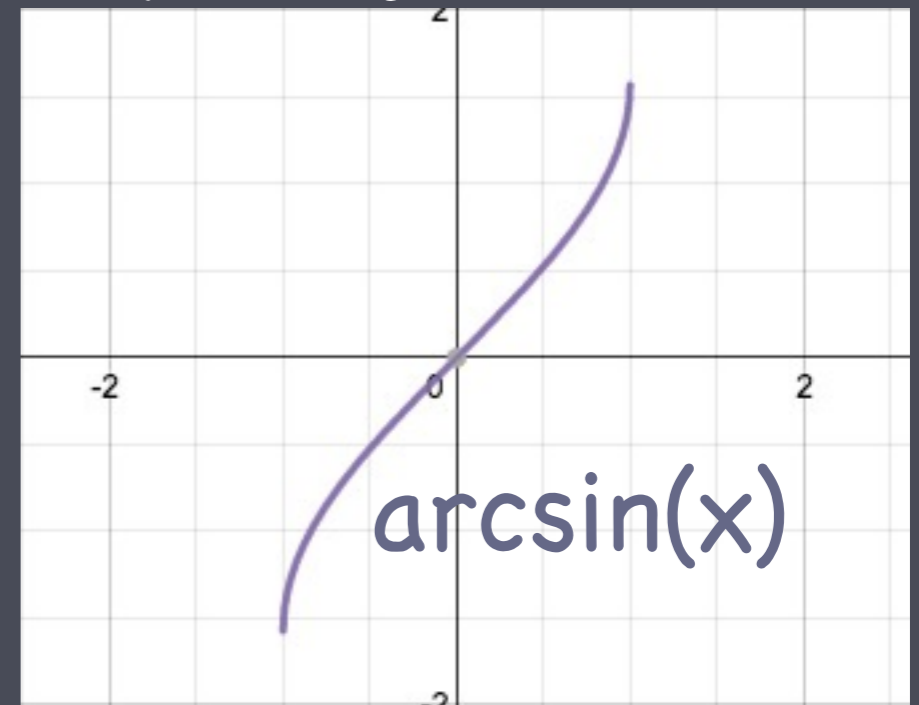
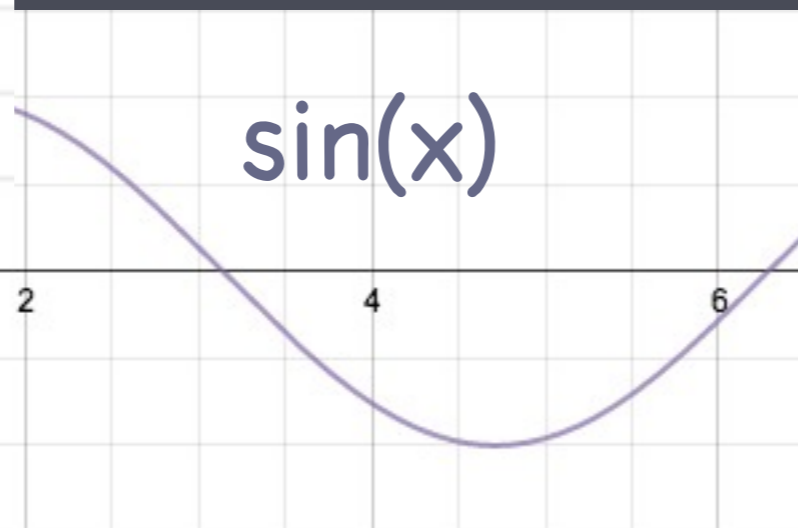
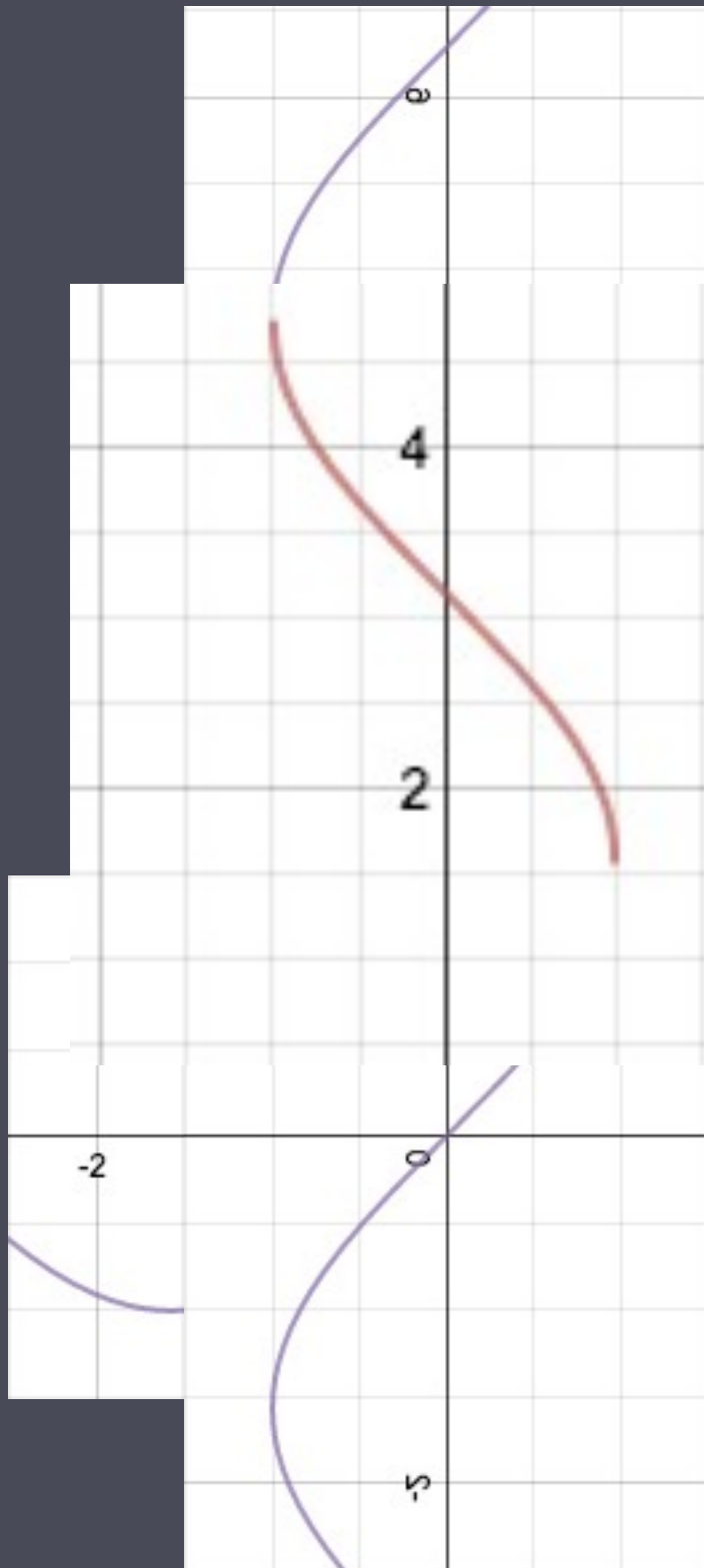
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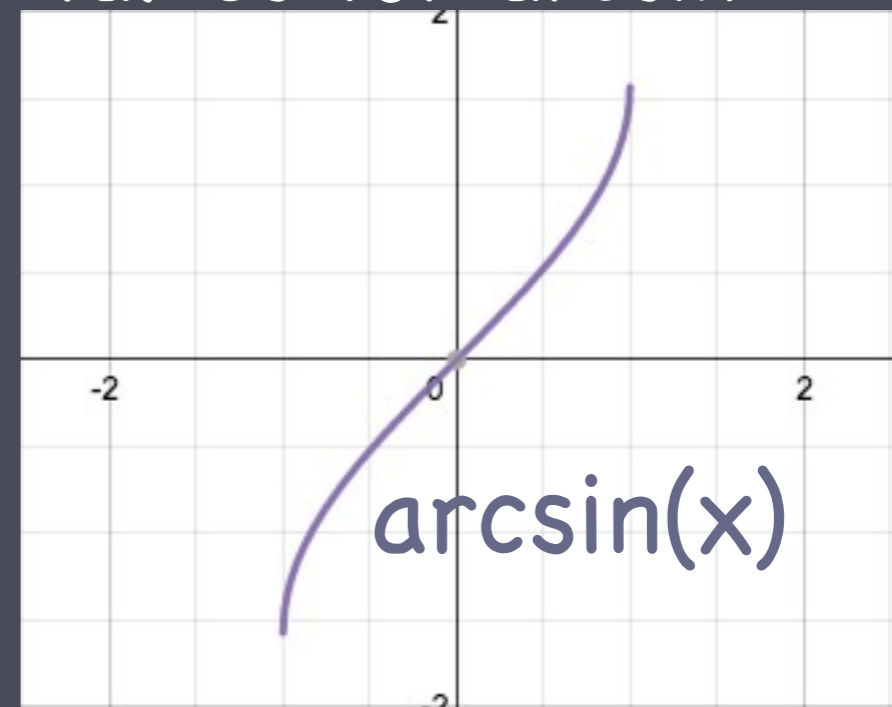
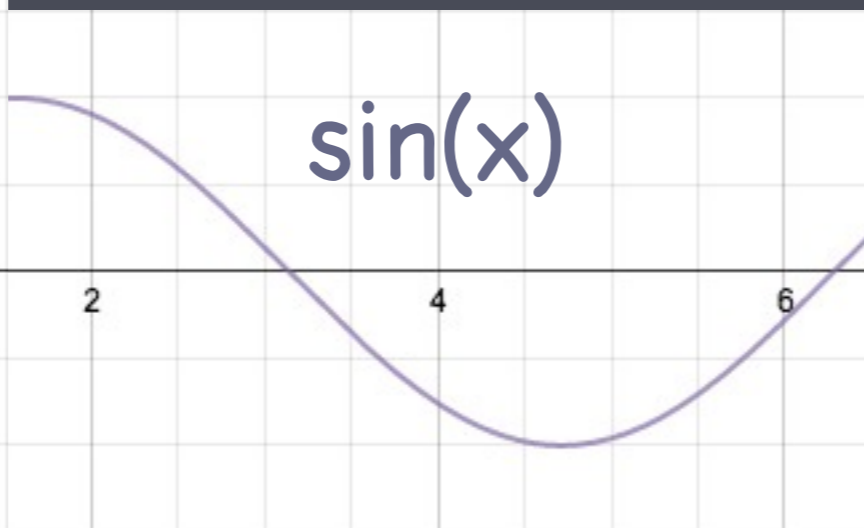
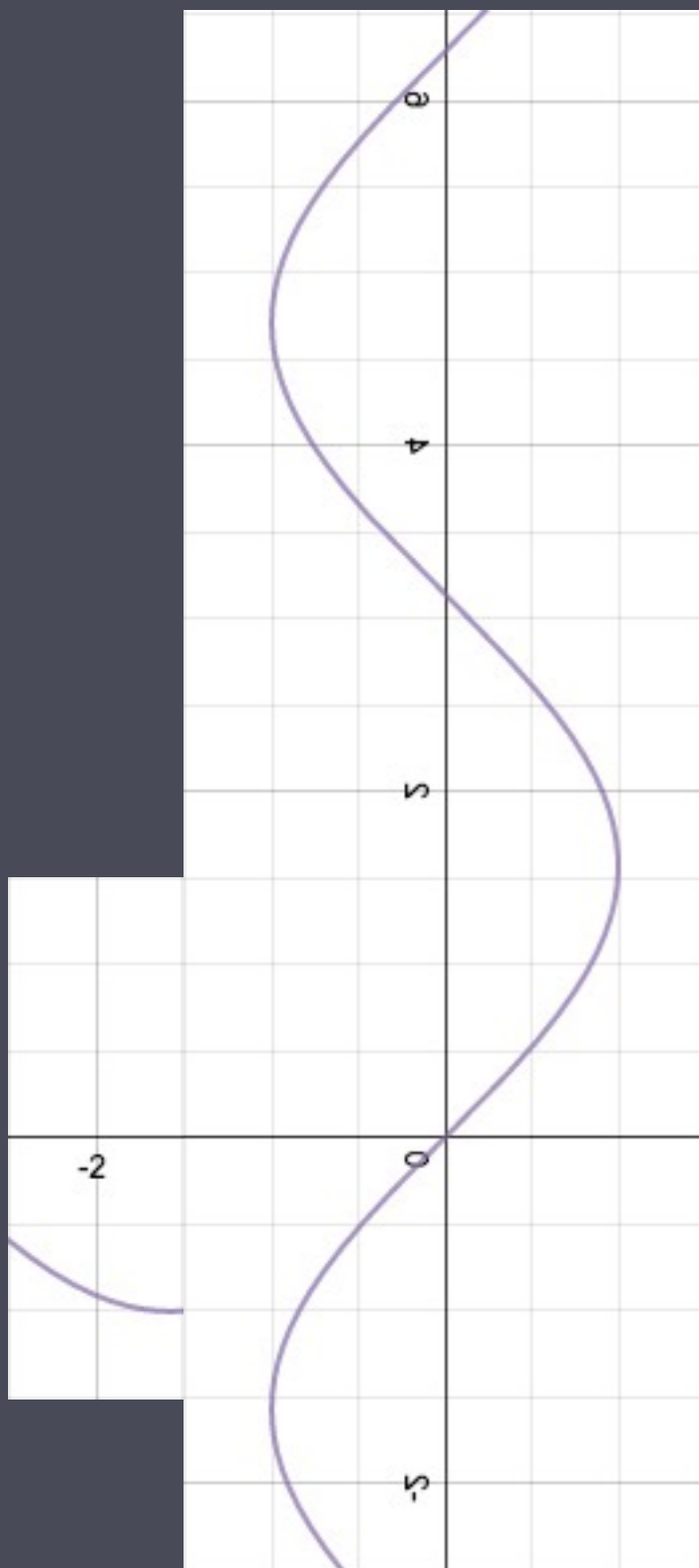
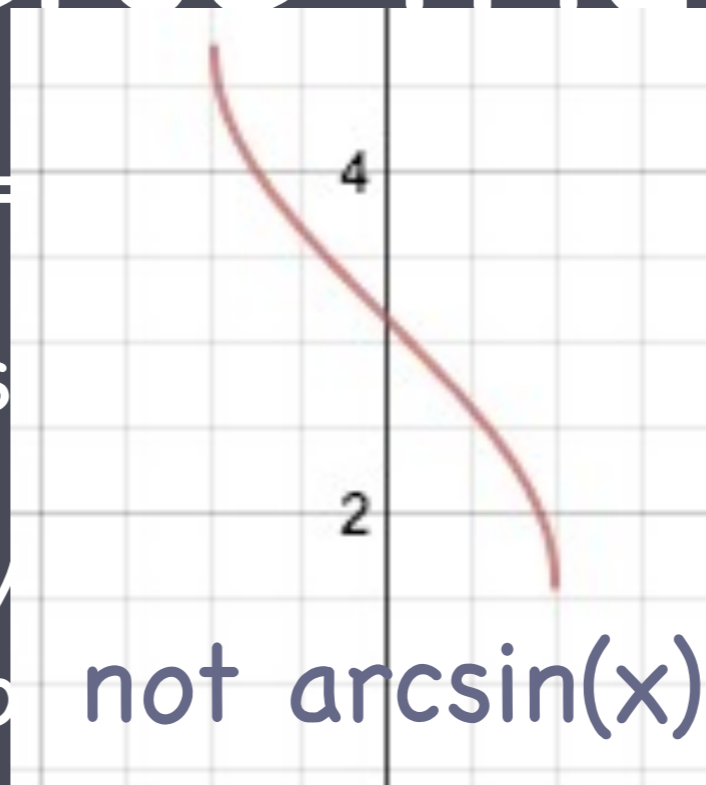


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The domain of arcsin is...

(A) $(-\pi/2, \pi/2)$

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(C) $[0, \pi]$

(D) $(-1, 1)$

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The range for $\arcsin(x)$ is...

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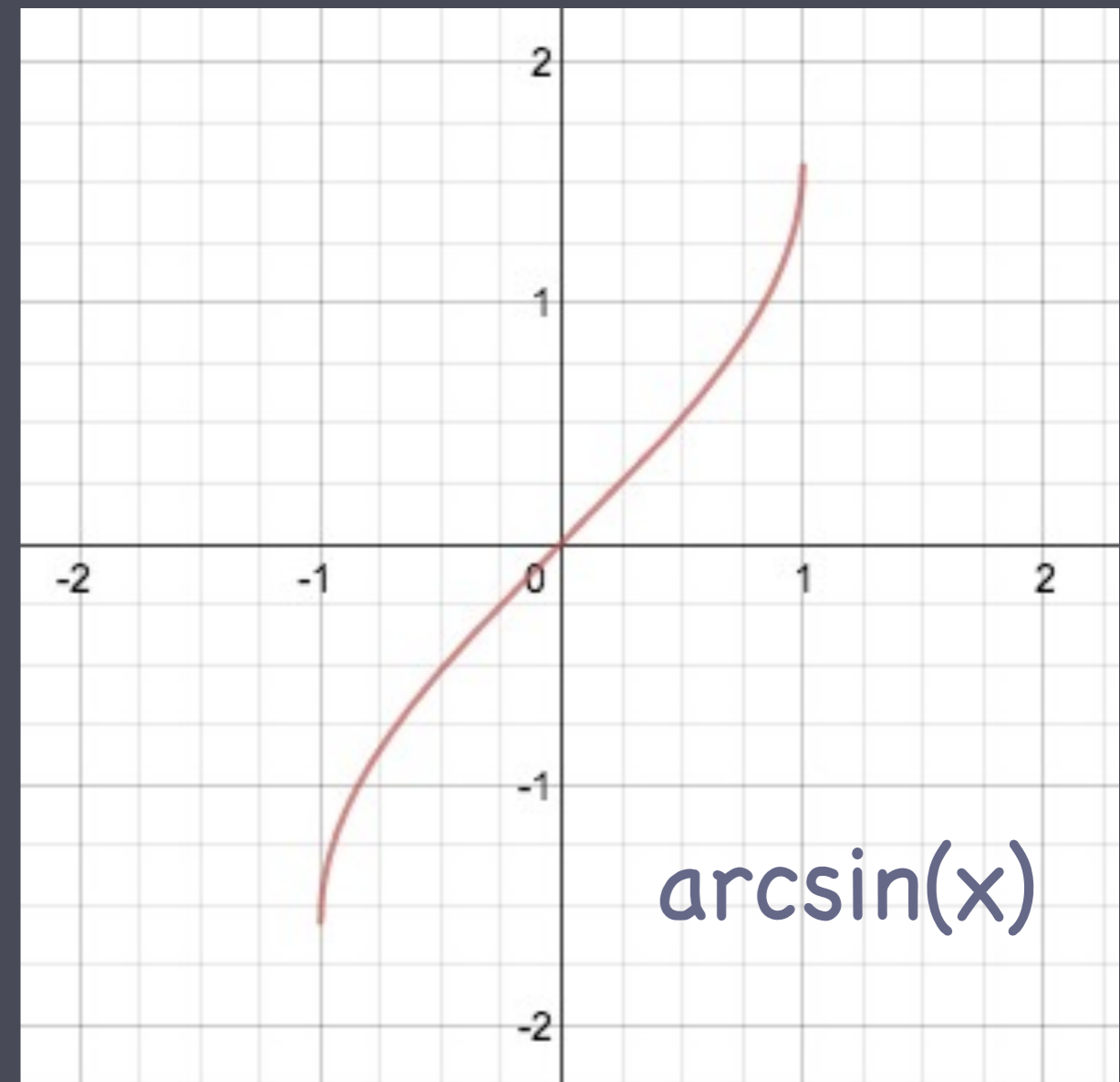
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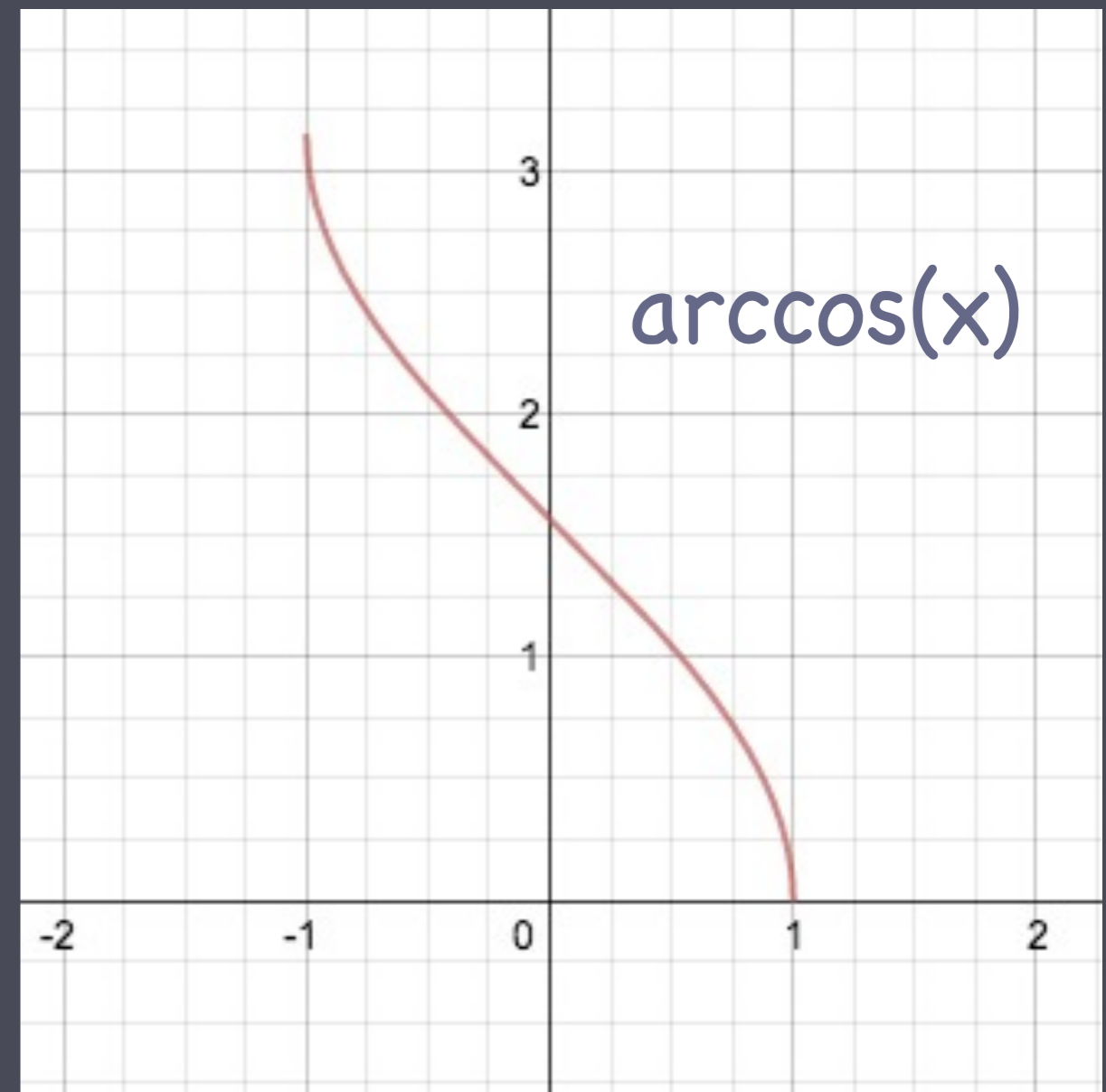
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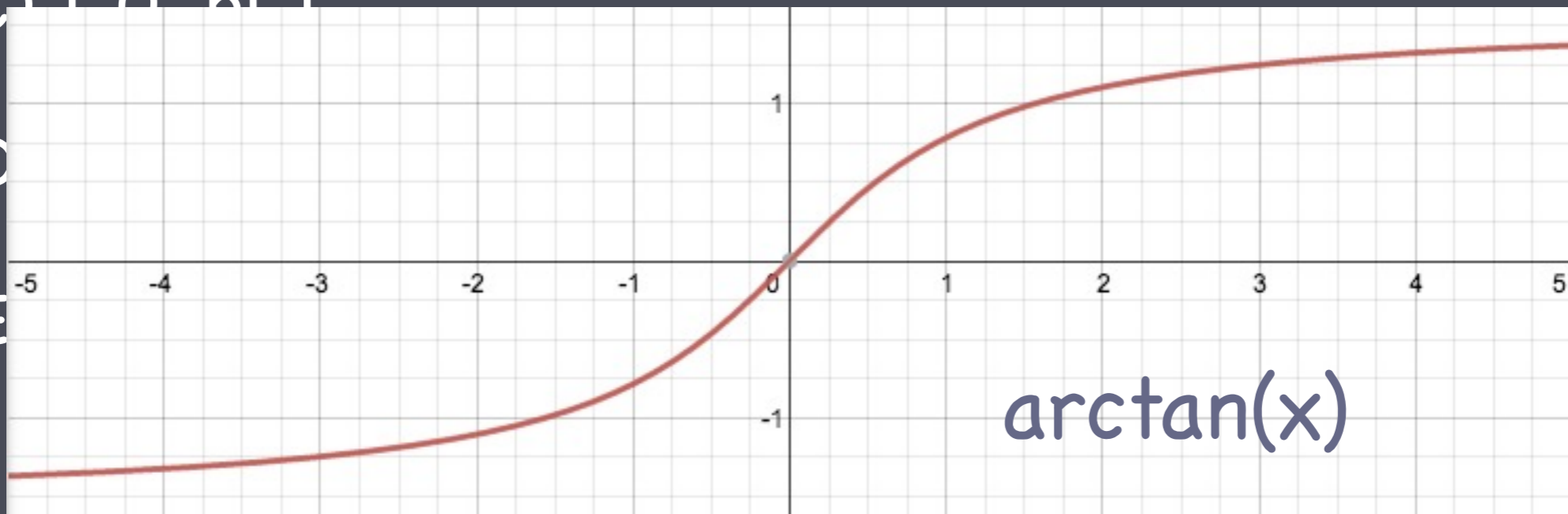
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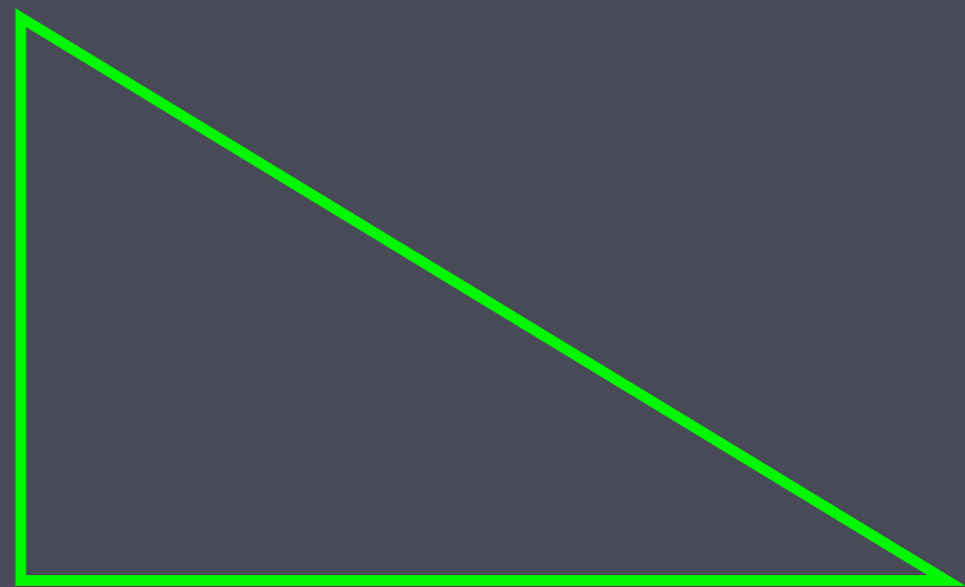
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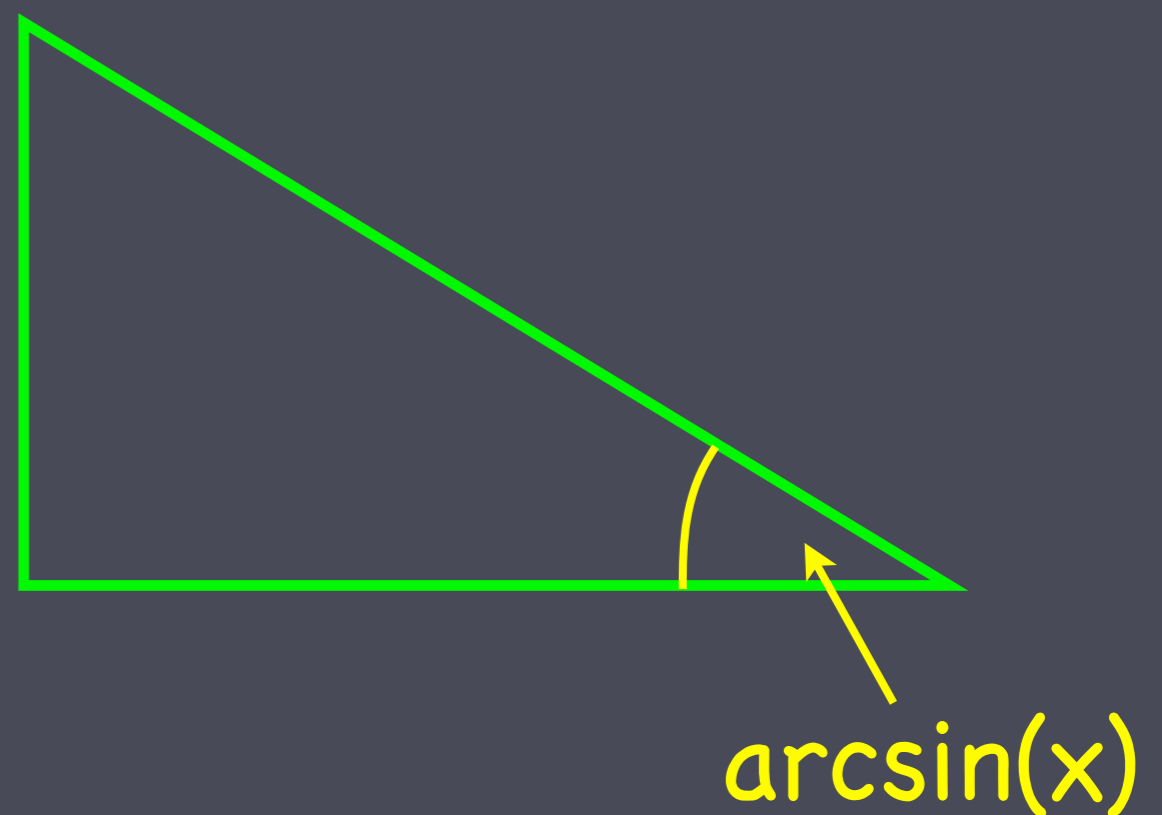
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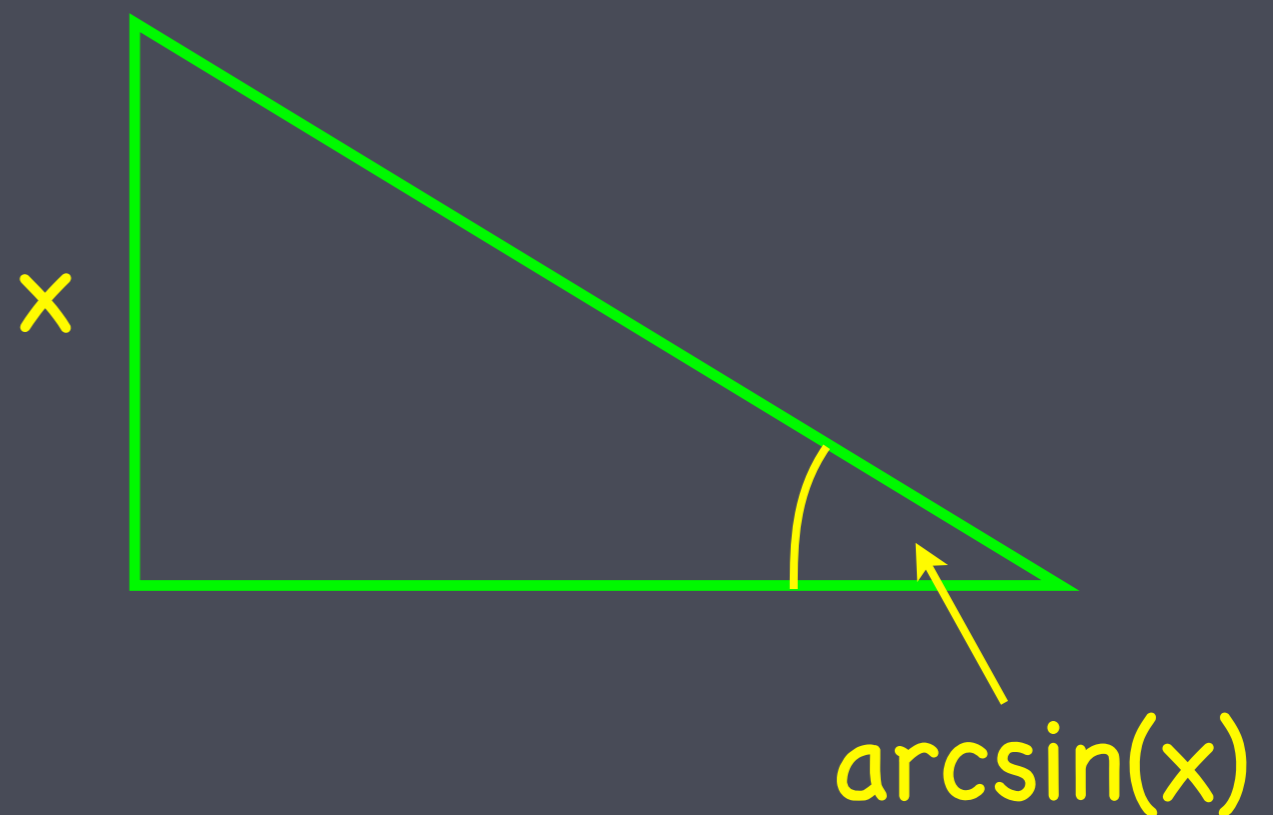
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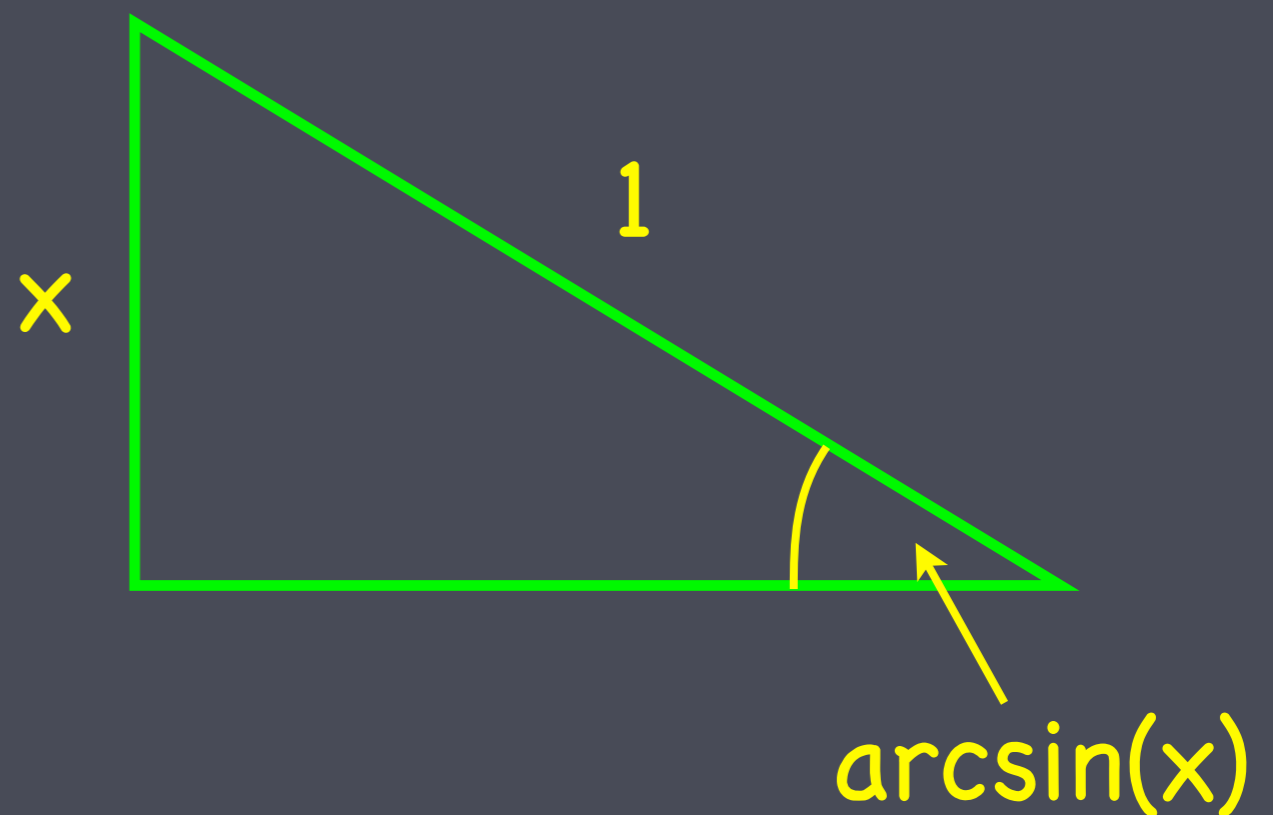
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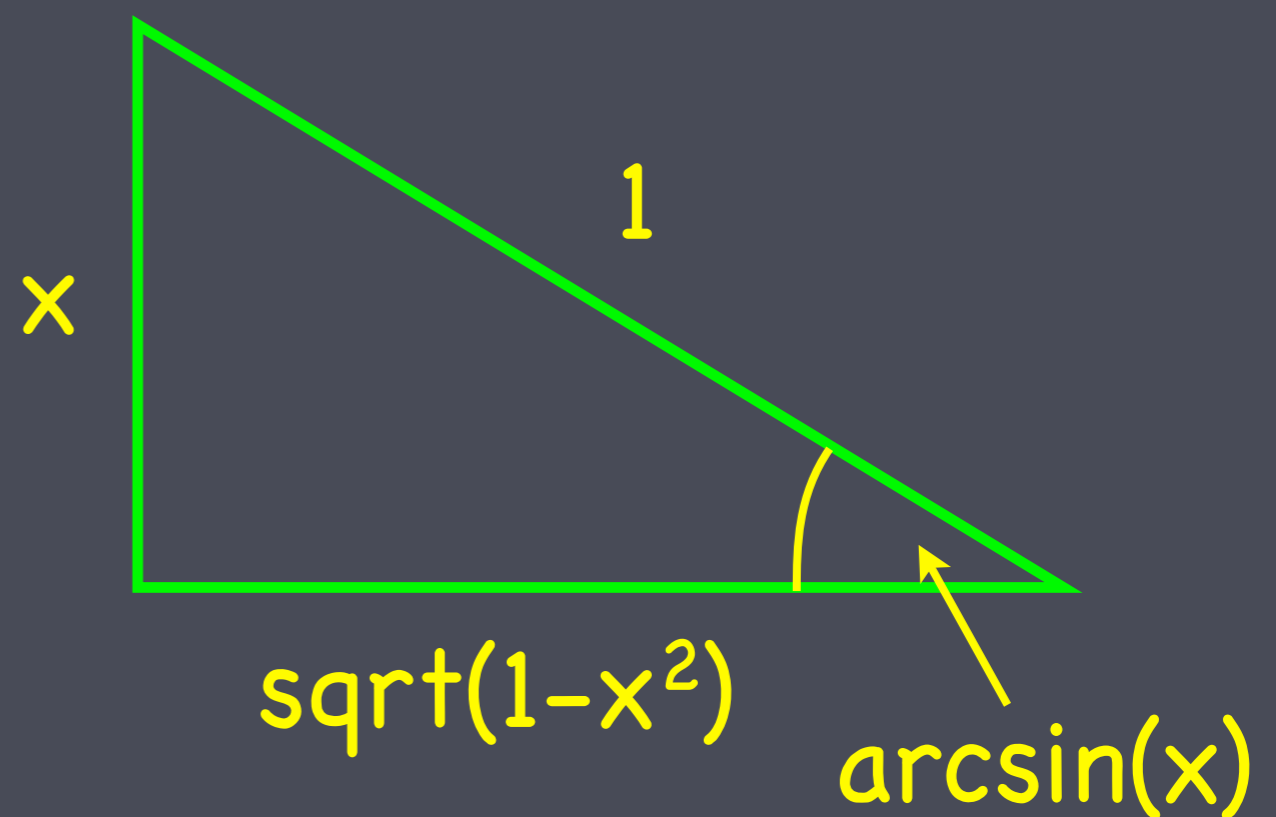
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