

Today...

- Demo WeBWorK tricks
- A Hill function clicker question.
- From secant line to tangent line.
- The Definition of the Derivative.

OSH

OSH

- uM and um

OSH

- uM and um

Metric prefixes in everyday use		
Text	Symbol	Factor
tera	T	1 000 000 000 000
giga	G	1 000 000 000
mega	M	1 000 000
kilo	k	1 000
hecto	h	100
deca	da	10
(none)	(none)	1
deci	d	0.1
centi	c	0.01
milli	m	0.001
micro	μ	0.000 001
nano	n	0.000 000 001
pico	p	0.000 000 000 001

V•T•E

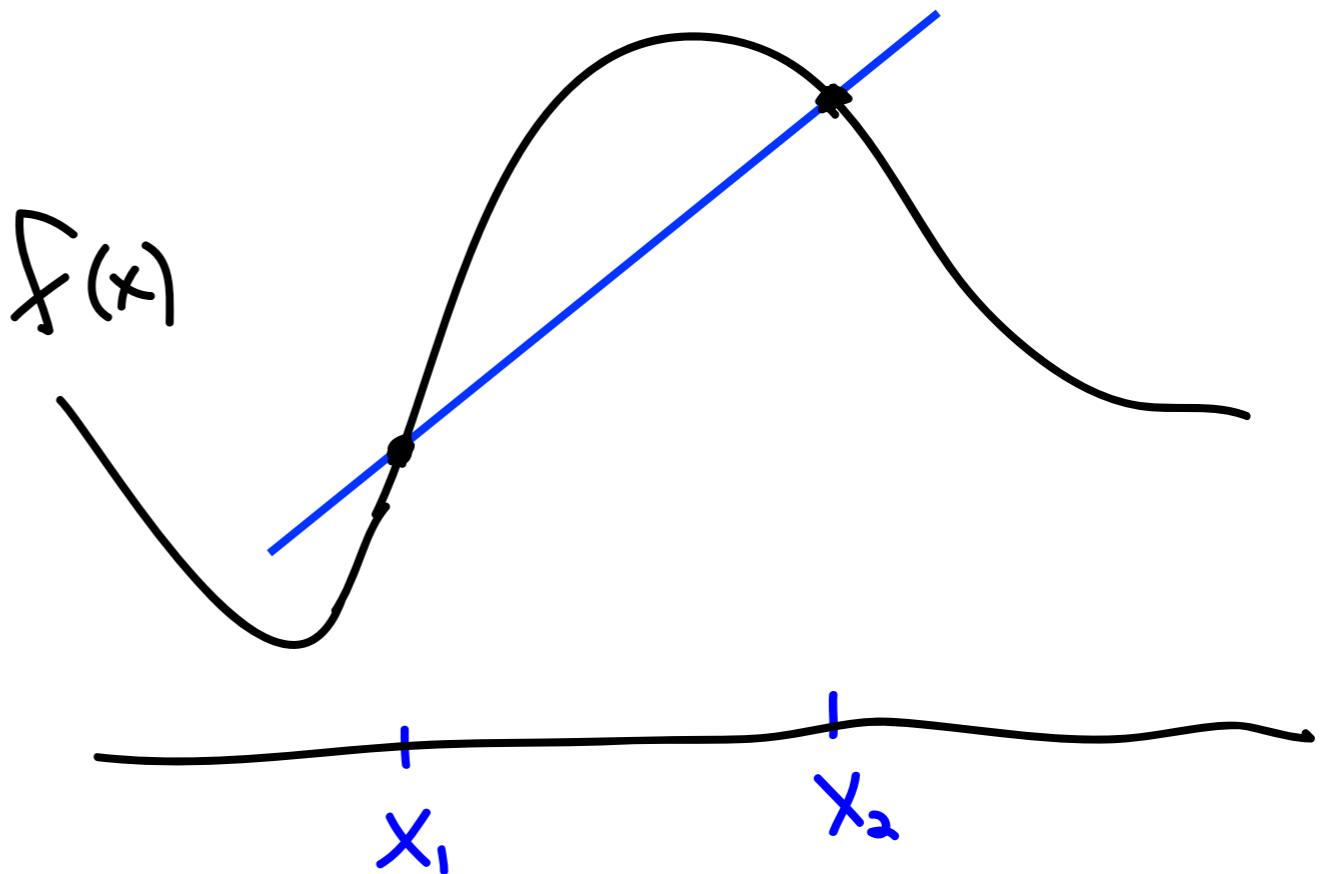
OSH

- uM and um
- How much to write for “Describe in words”.

OSH

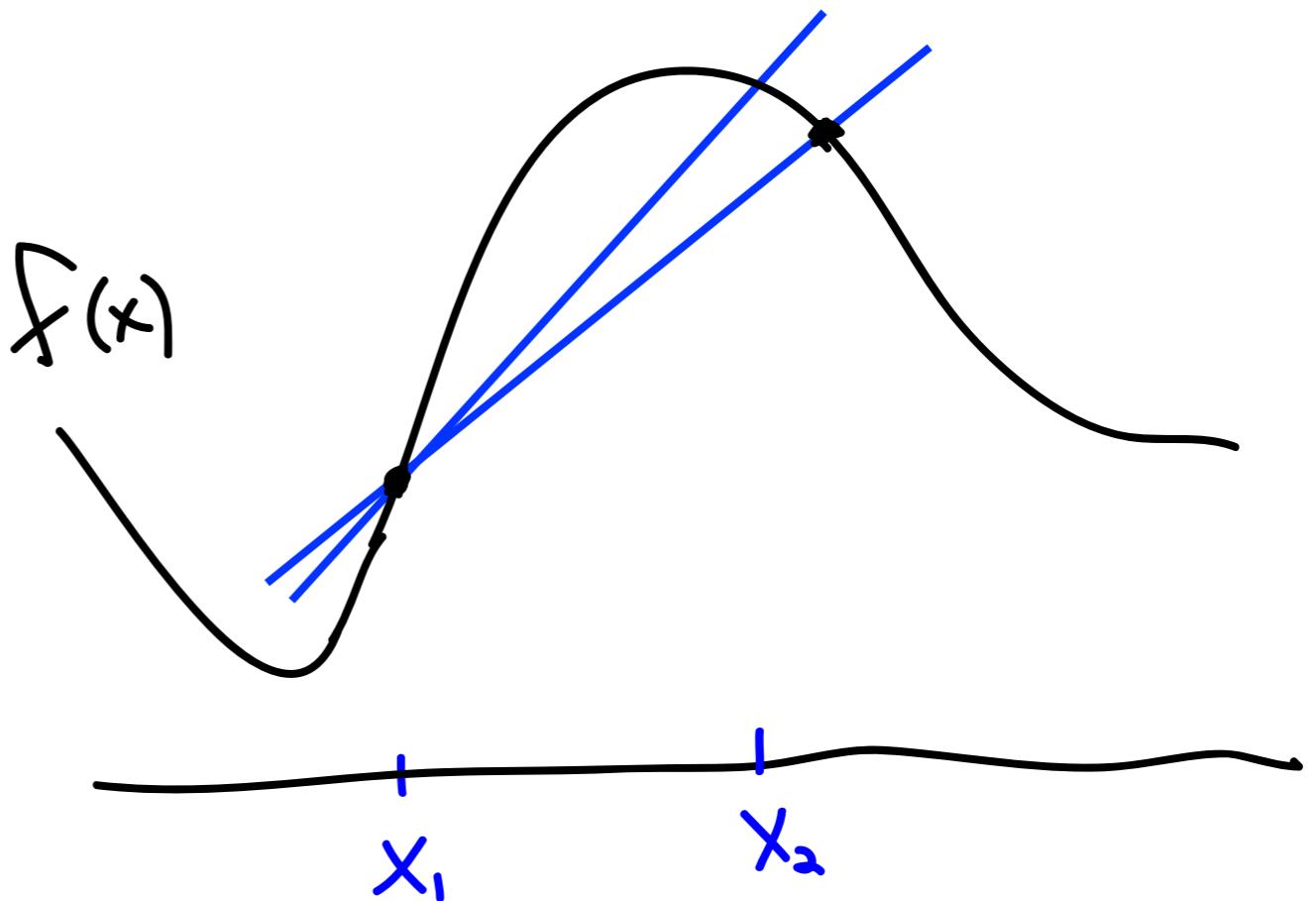
- uM and um
- How much to write for “Describe in words”.
 - I read through the example solutions carefully:
 - (A) Yes
 - (B) No

**What if you want the rate of change AT x_1 ?
(instantaneous instead of average)**



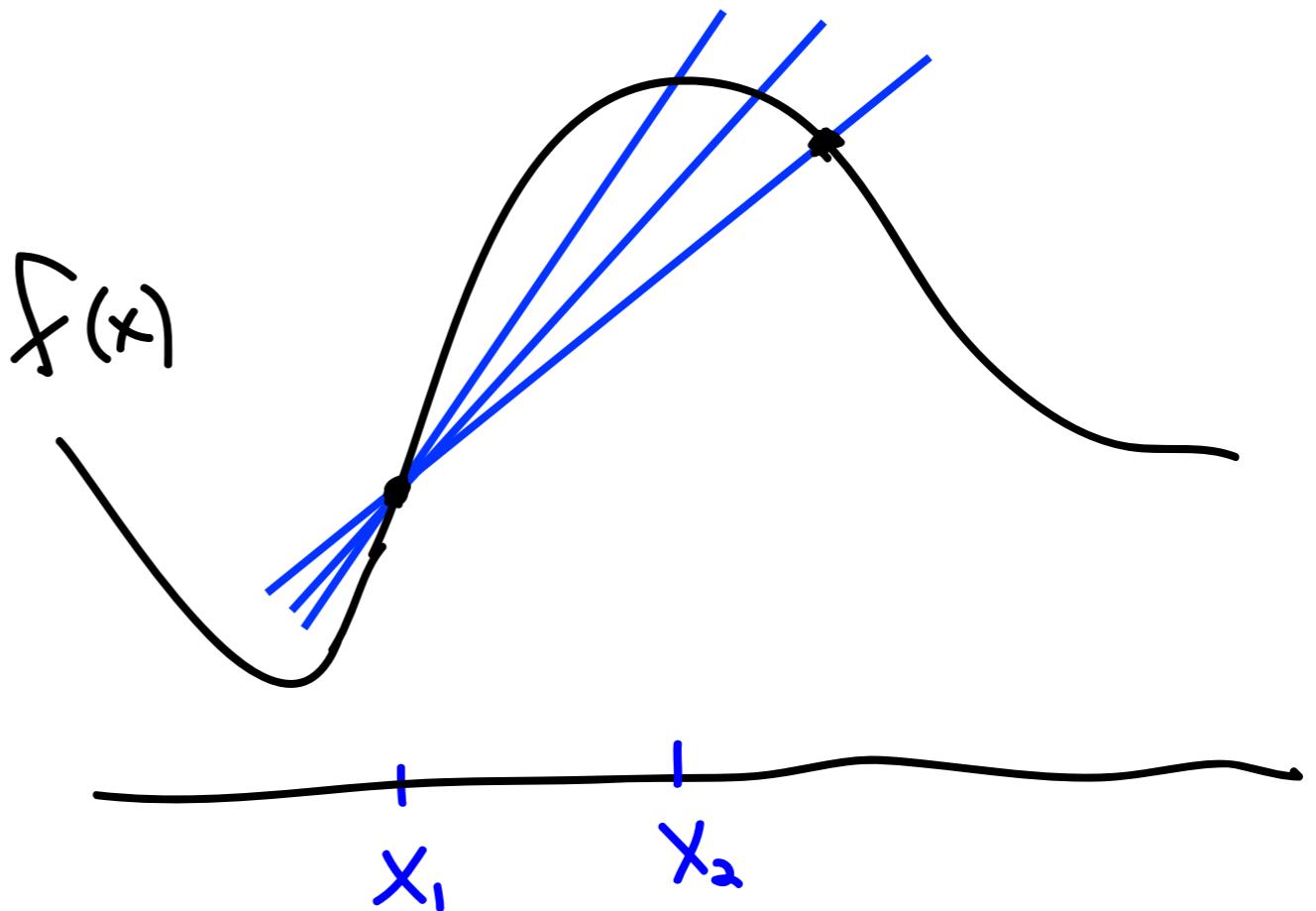
What if you want the rate of change AT x_1 ? (instantaneous instead of average)

Take a point x_2 so that the secant line is closer to the “secant line” AT x_1 .



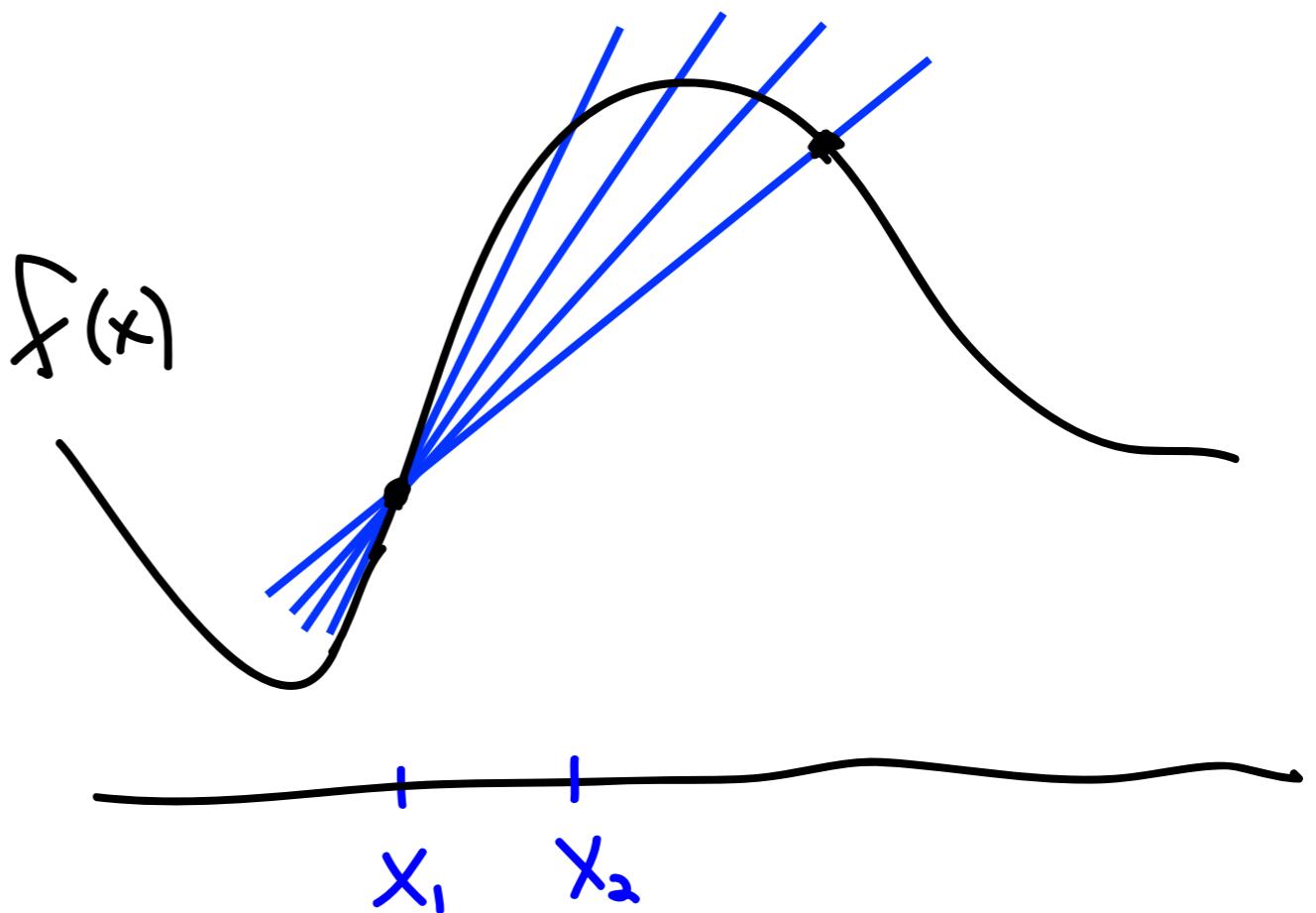
What if you want the rate of change AT x_1 ? (instantaneous instead of average)

Take a point x_2 so that the secant line is closer to the “secant line” AT x_1 .



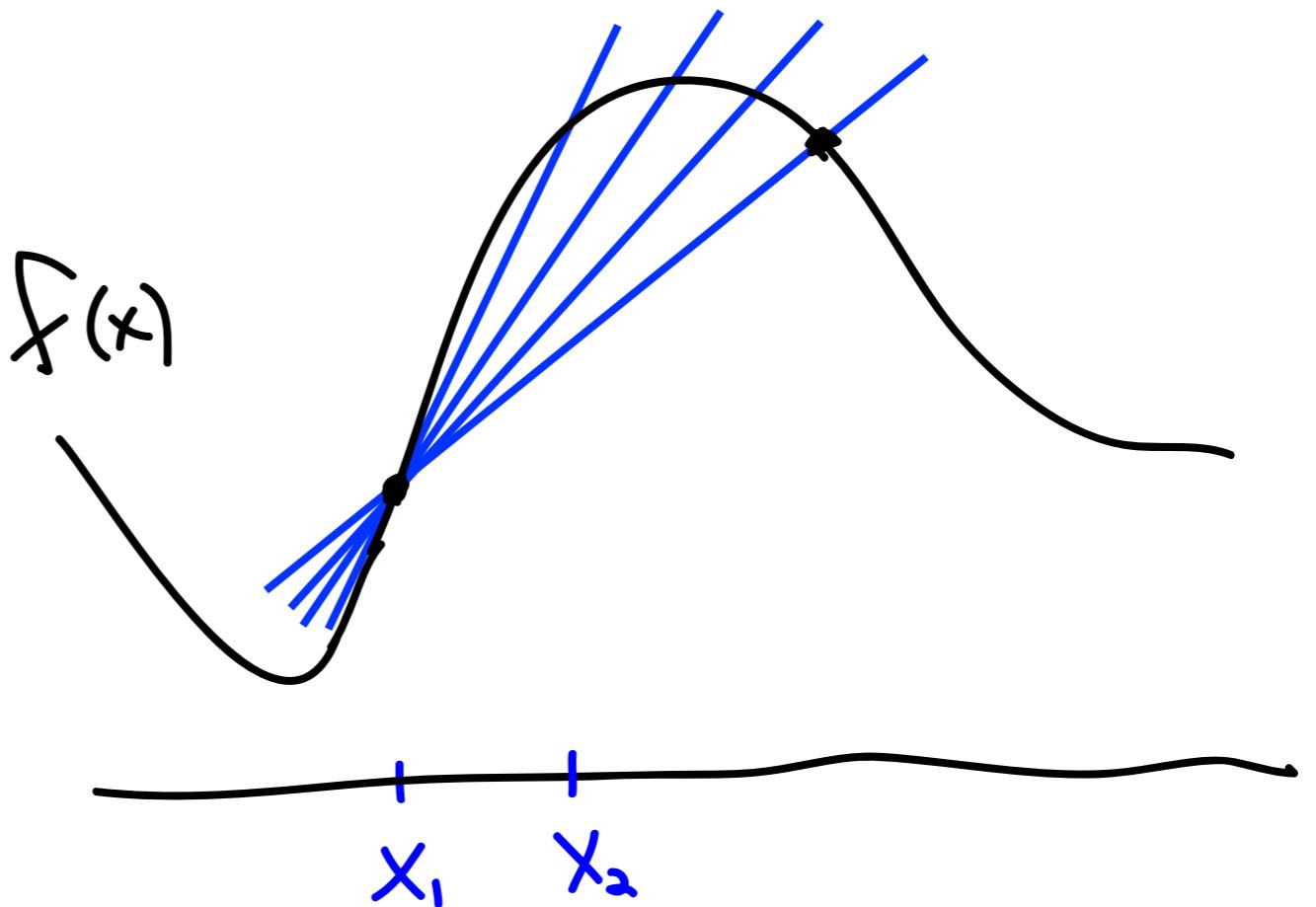
What if you want the rate of change AT x_1 ? (instantaneous instead of average)

Take a point x_2
so that the
secant line is
closer to the
“secant line”
AT x_1 .



What if you want the rate of change AT x_1 ? (instantaneous instead of average)

Take a point x_2 so that the secant line is closer to the “secant line” AT x_1 .

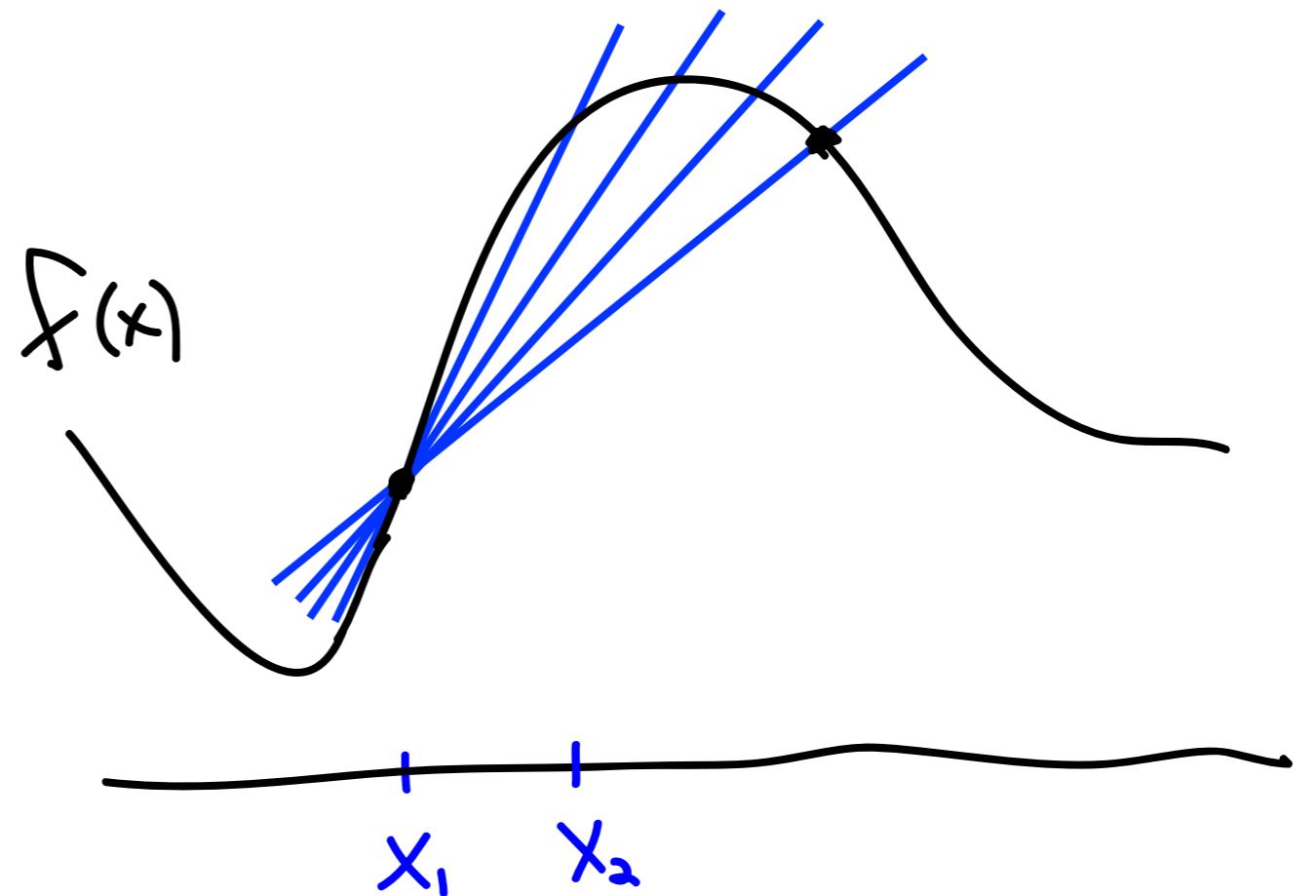


Alternate notation: let $x_2 = x_1 + h$ so that

$$m = \frac{f(x_2) - f(x_1)}{x_2 - x_1}$$

What if you want the rate of change AT x_1 ? (instantaneous instead of average)

Take a point x_2 so that the secant line is closer to the “secant line” AT x_1 .

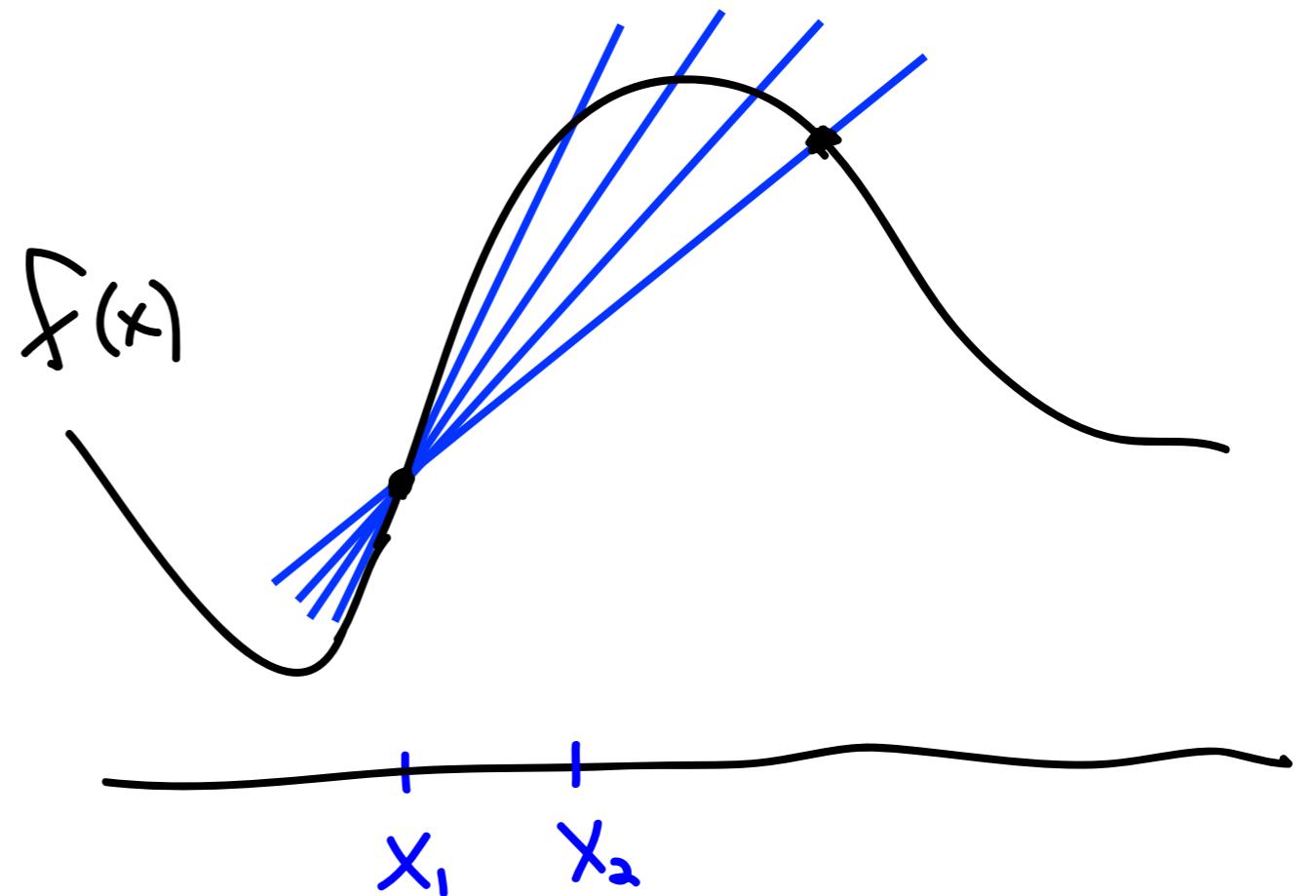


Alternate notation: let $x_2 = x_1 + h$ so that

$$m = \frac{f(x_2) - f(x_1)}{x_2 - x_1} = \frac{f(x_1 + h) - f(x_1)}{x_1 + h - x_1}$$

What if you want the rate of change AT x_1 ? (instantaneous instead of average)

Take a point x_2 so that the secant line is closer to the “secant line” AT x_1 .



Alternate notation: let $x_2 = x_1 + h$ so that

$$m = \frac{f(x_2) - f(x_1)}{x_2 - x_1} = \frac{f(x_1 + h) - f(x_1)}{h}$$

If we take h values closer and closer to 0...

If we take h values closer and closer to 0...

- The average slope becomes the instantaneous slope.

If we take h values closer and closer to 0...

- The average slope becomes the instantaneous slope.
- The secant line approaches the tangent line.

If we take h values closer and closer to 0...

- The average slope becomes the instantaneous slope.
- The secant line approaches the **tangent line**.
- The slope of the secant line approaches the slope of the tangent line.

If we take h values closer and closer to 0...

- The average slope becomes the instantaneous slope.
- The secant line approaches the **tangent line**.
- The slope of the secant line approaches the slope of the tangent line.
- We call the slope of the tangent line **the derivative at x_1** .

If we take h values closer and closer to 0...

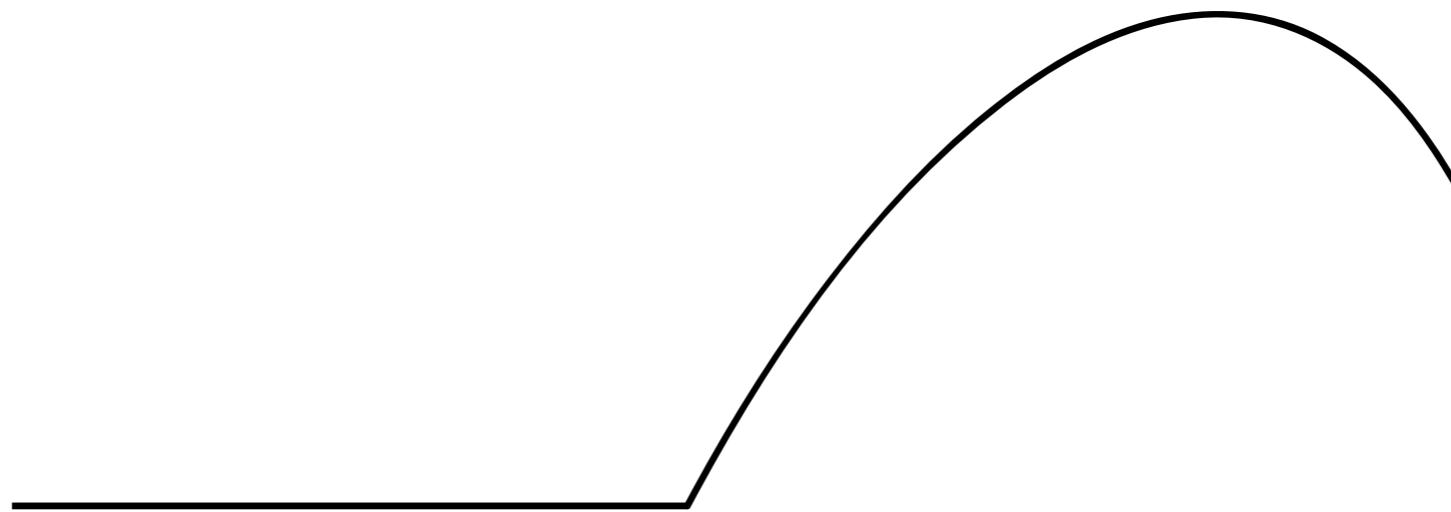
- The average slope becomes the instantaneous slope.
- The secant line approaches the **tangent line**.
- The slope of the secant line approaches the slope of the tangent line.
- We call the slope of the tangent line **the derivative at x_1** .
- We now have to learn how to take **limits!**

If we take h values closer and closer to 0...

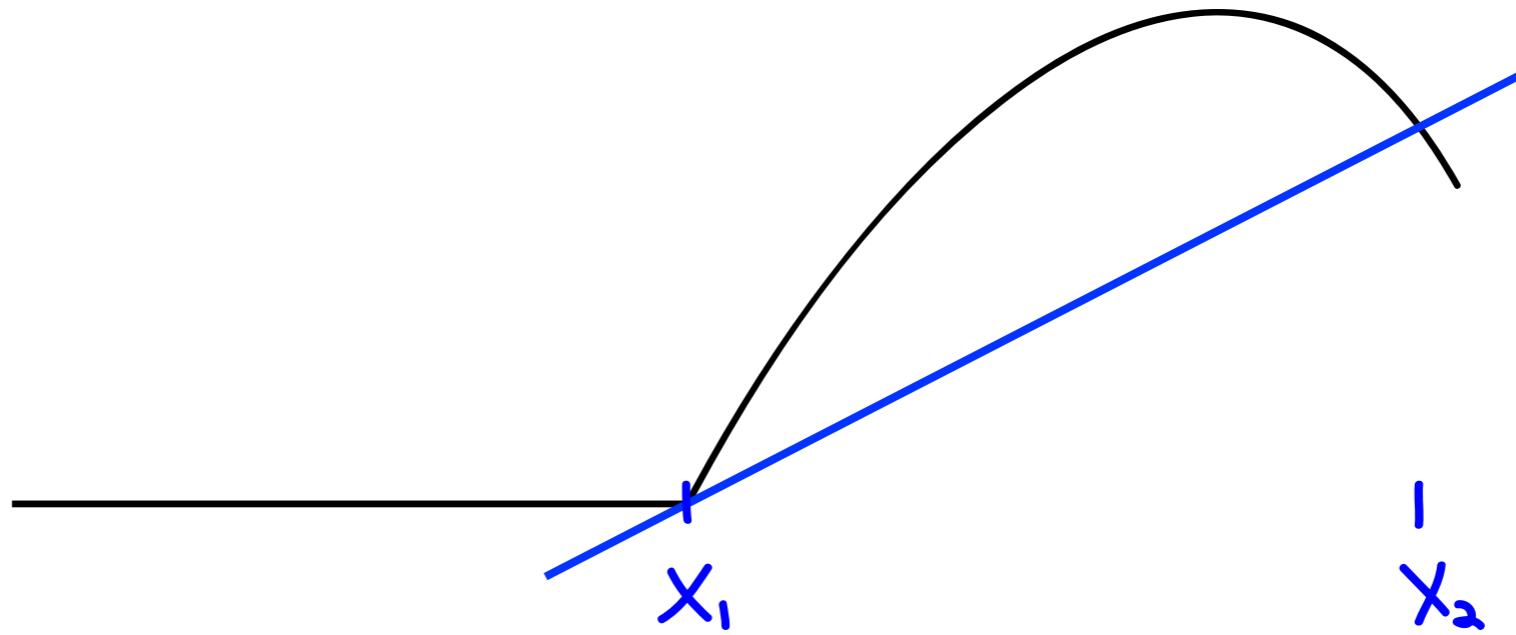
- The average slope becomes the instantaneous slope.
- The secant line approaches the **tangent line**.
- The slope of the secant line approaches the slope of the tangent line.
- We call the slope of the tangent line **the derivative at x_1** .
- We now have to learn how to take **limits!**

$$\text{slope at } x_1 = f'(x_1) = \lim_{h \rightarrow 0} \frac{f(x_1 + h) - f(x_1)}{h}$$

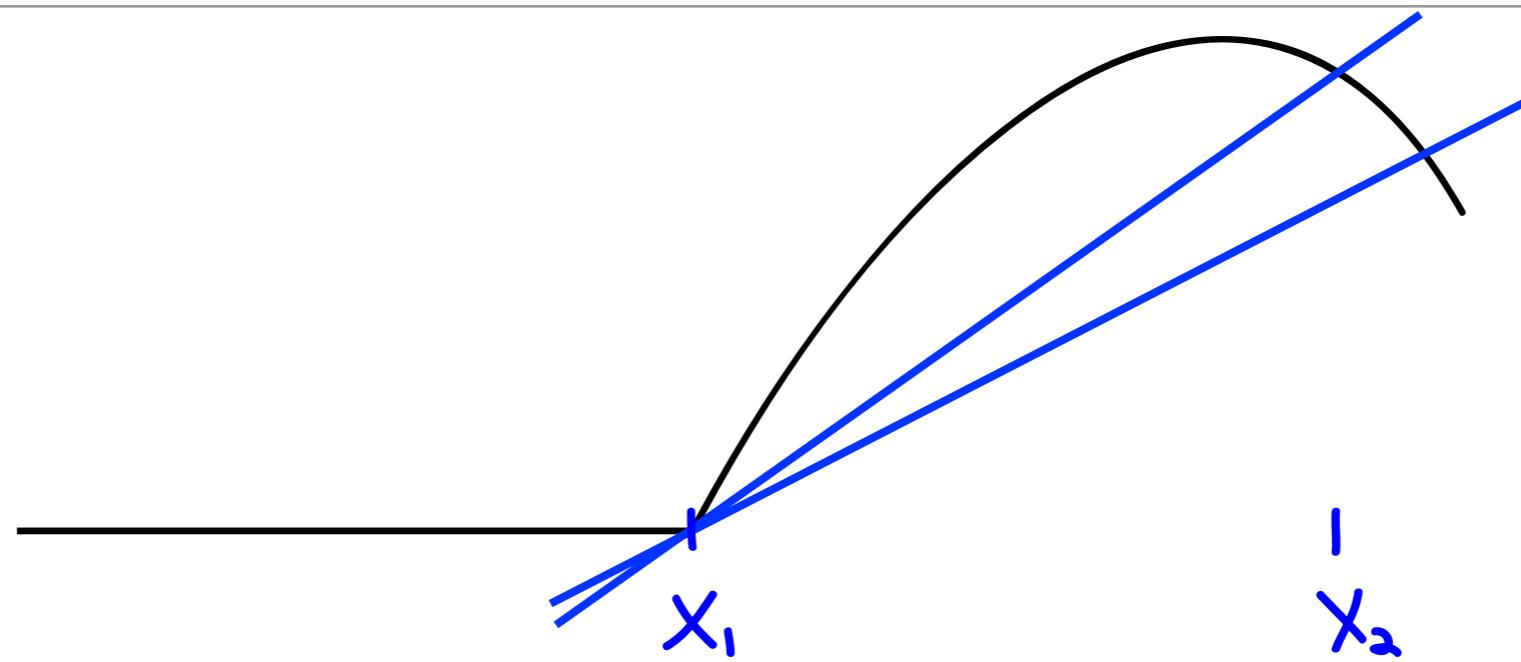
Another example



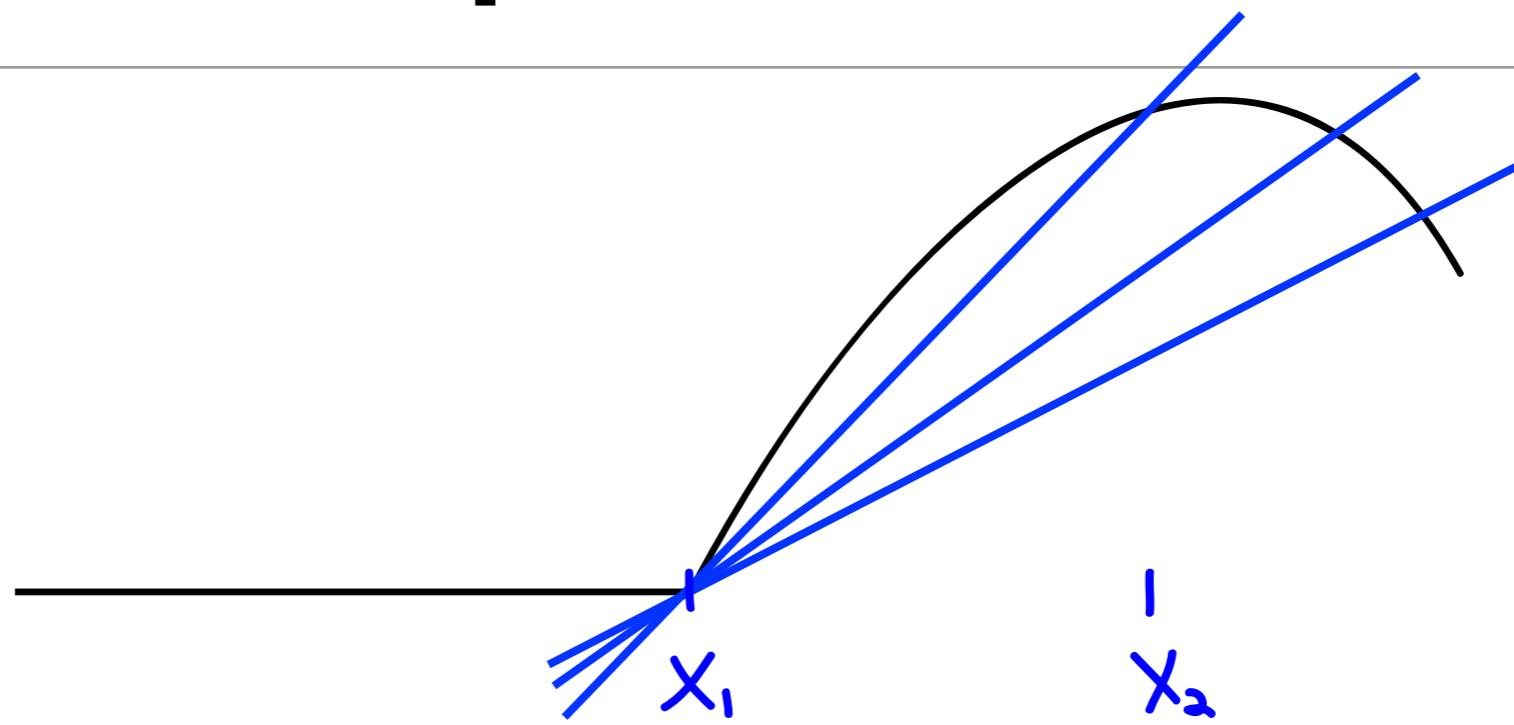
Another example



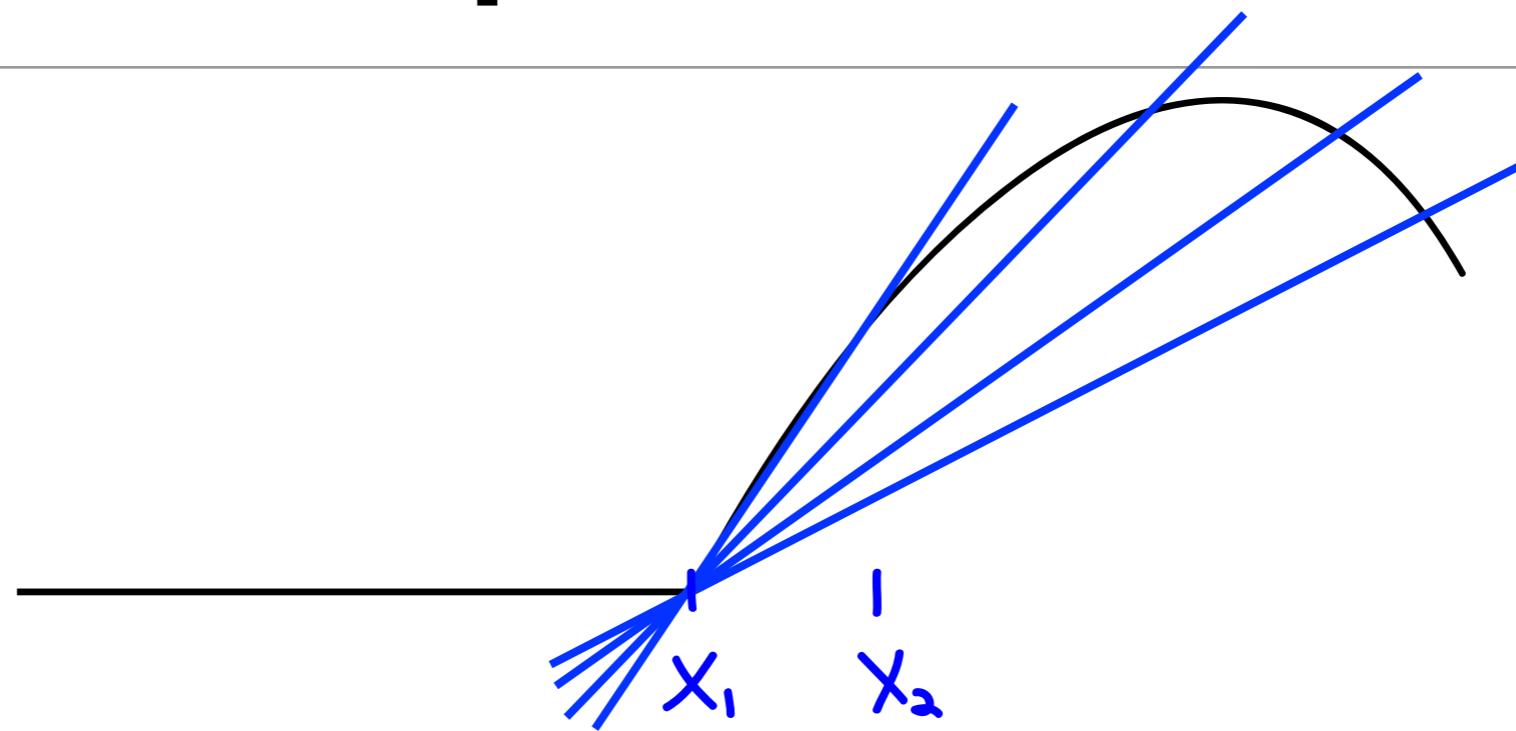
Another example



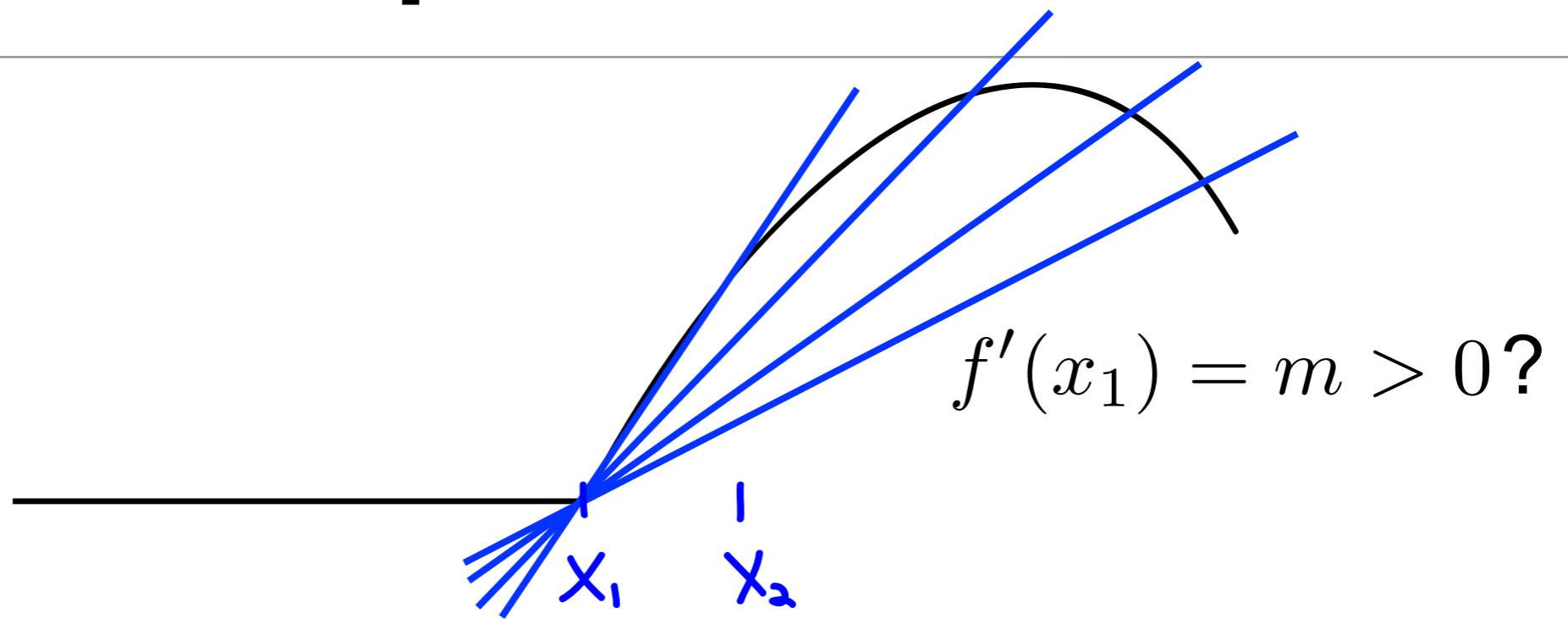
Another example



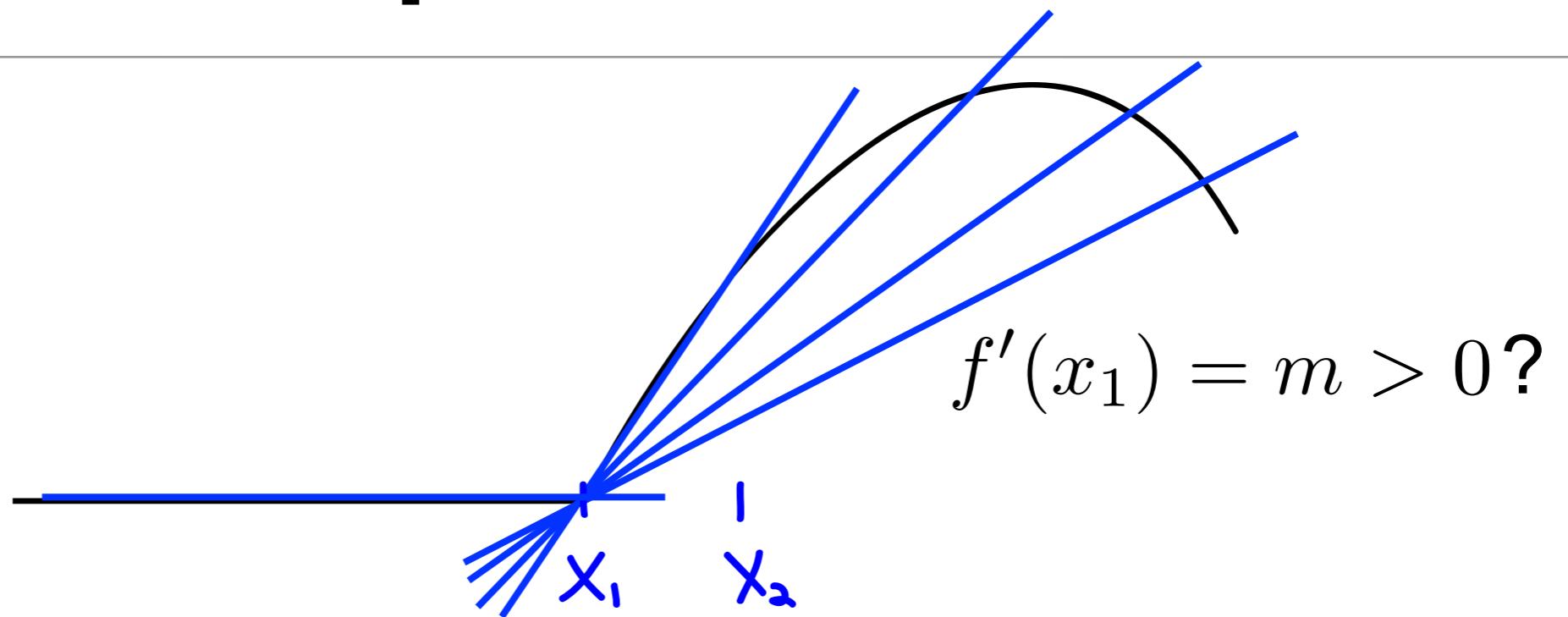
Another example



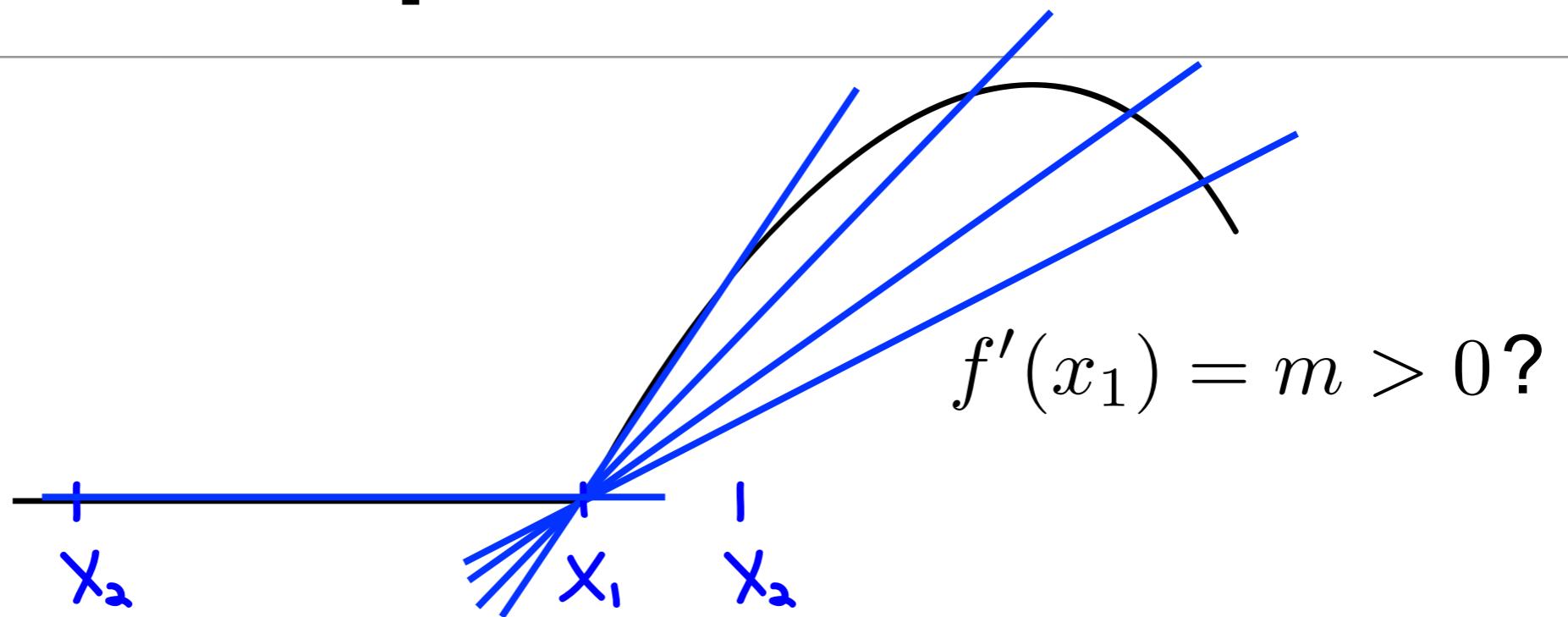
Another example



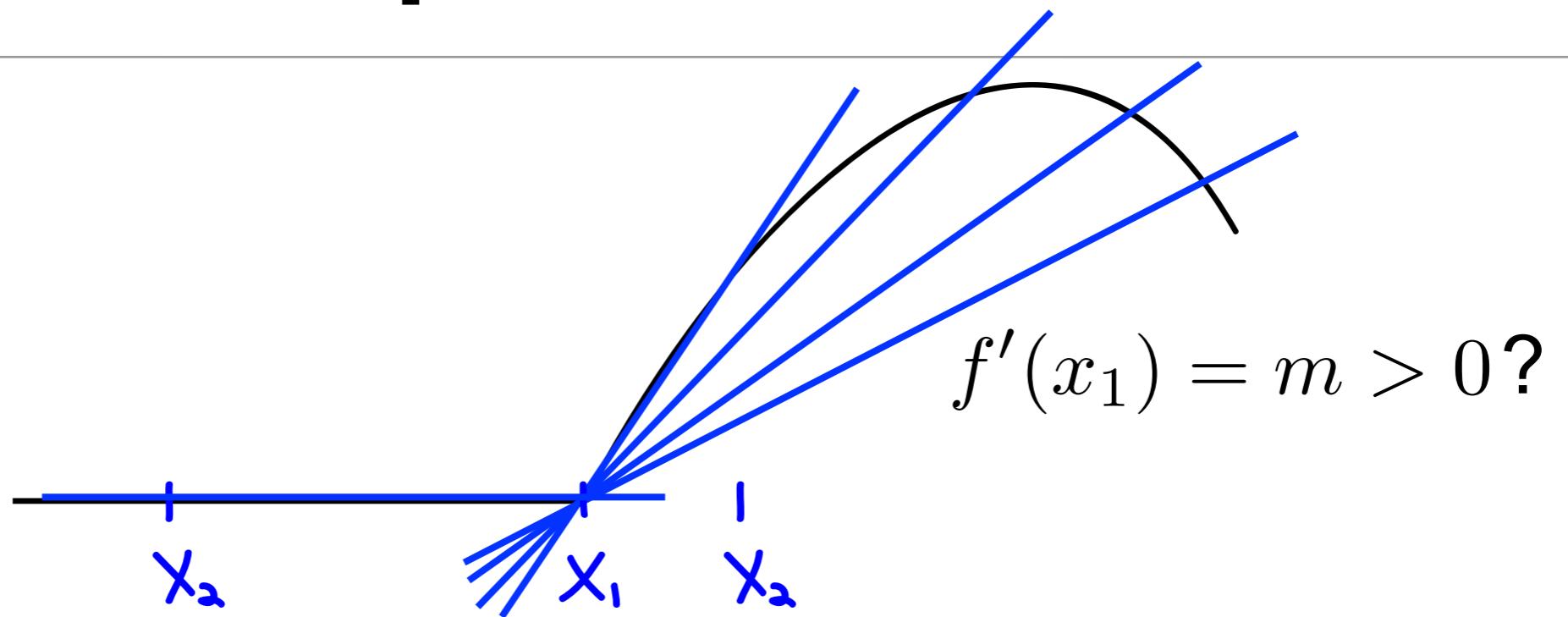
Another example



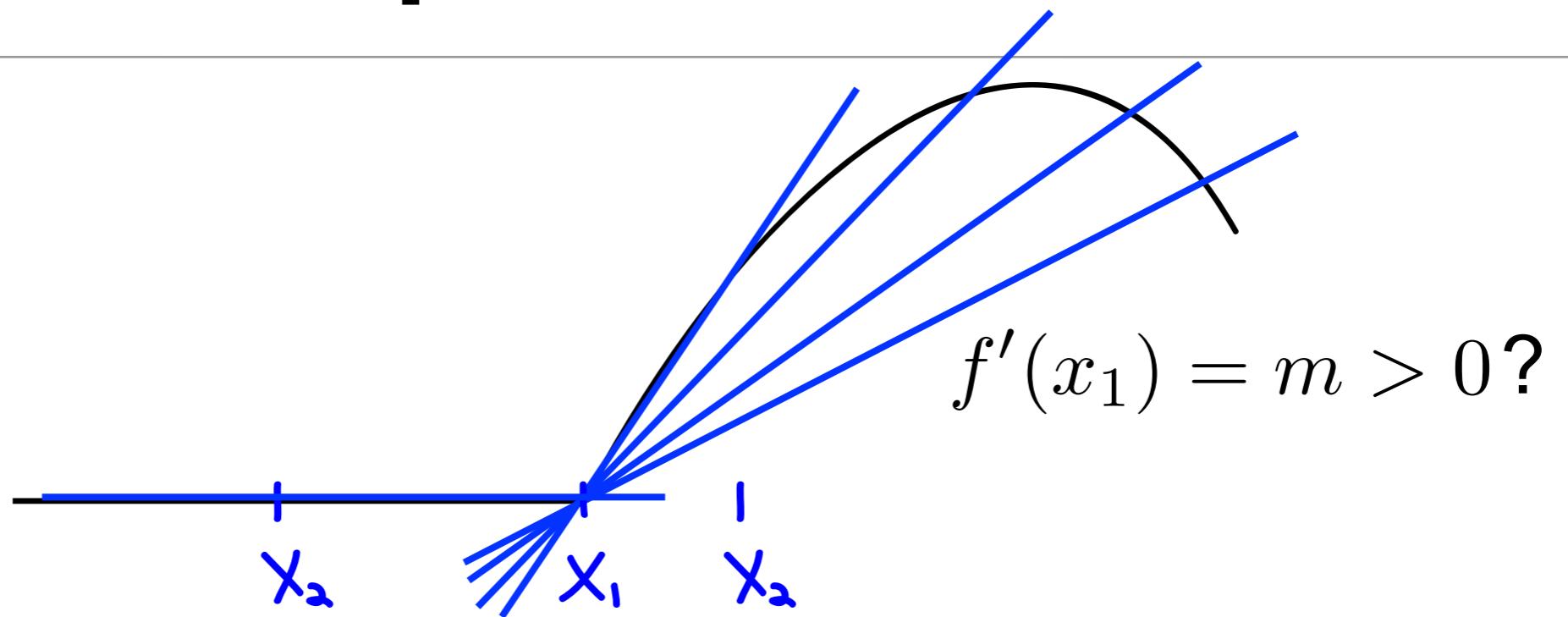
Another example



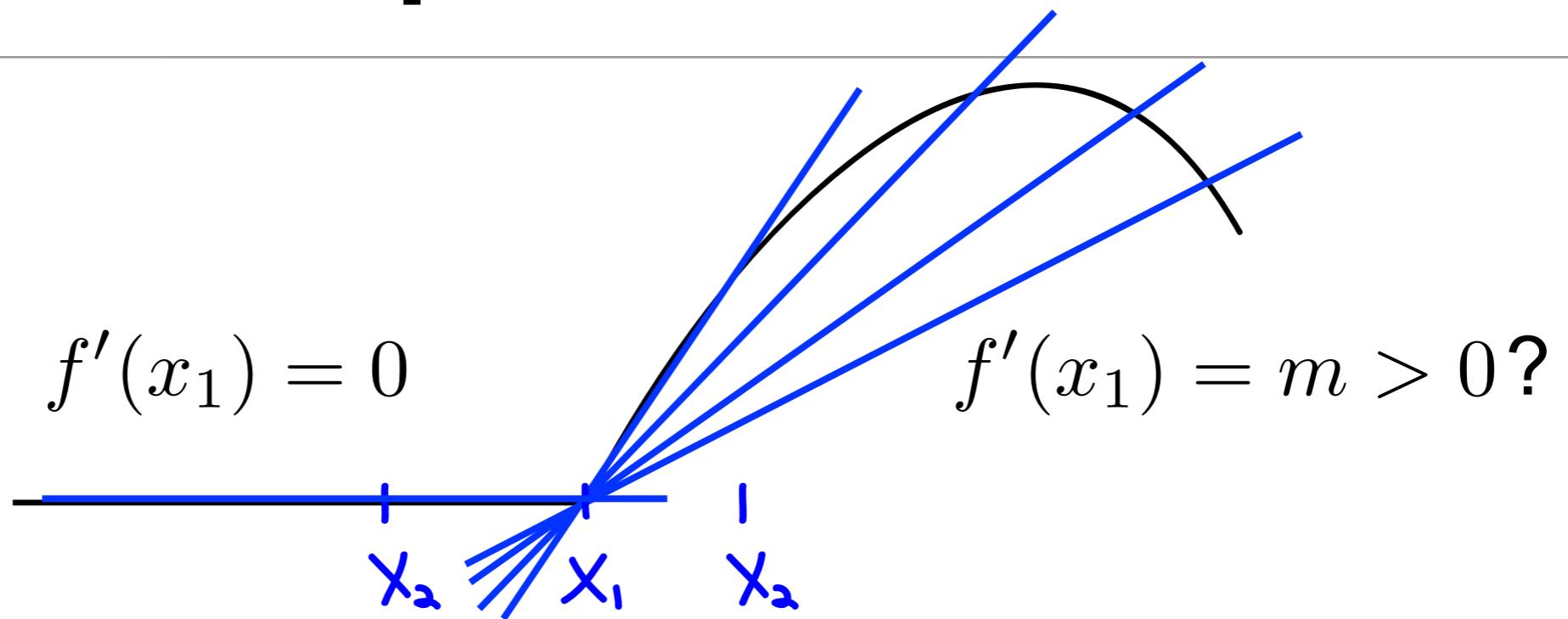
Another example



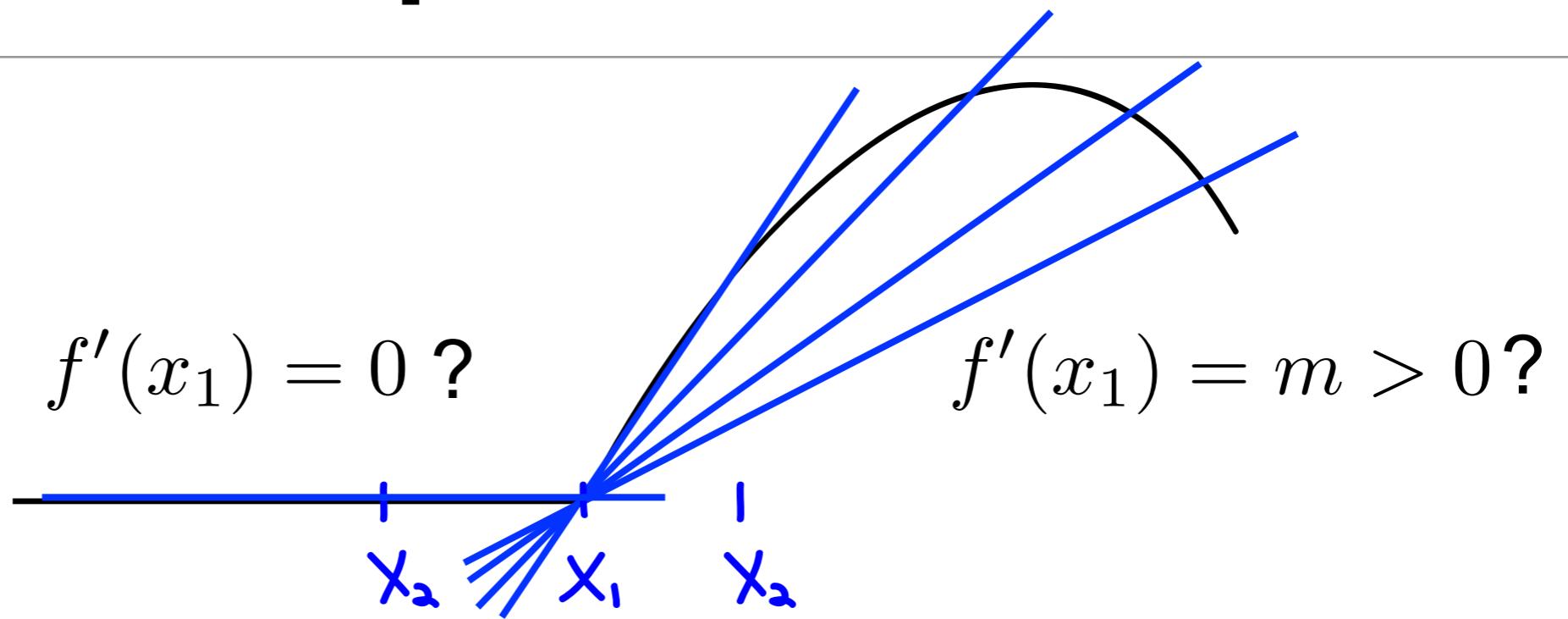
Another example



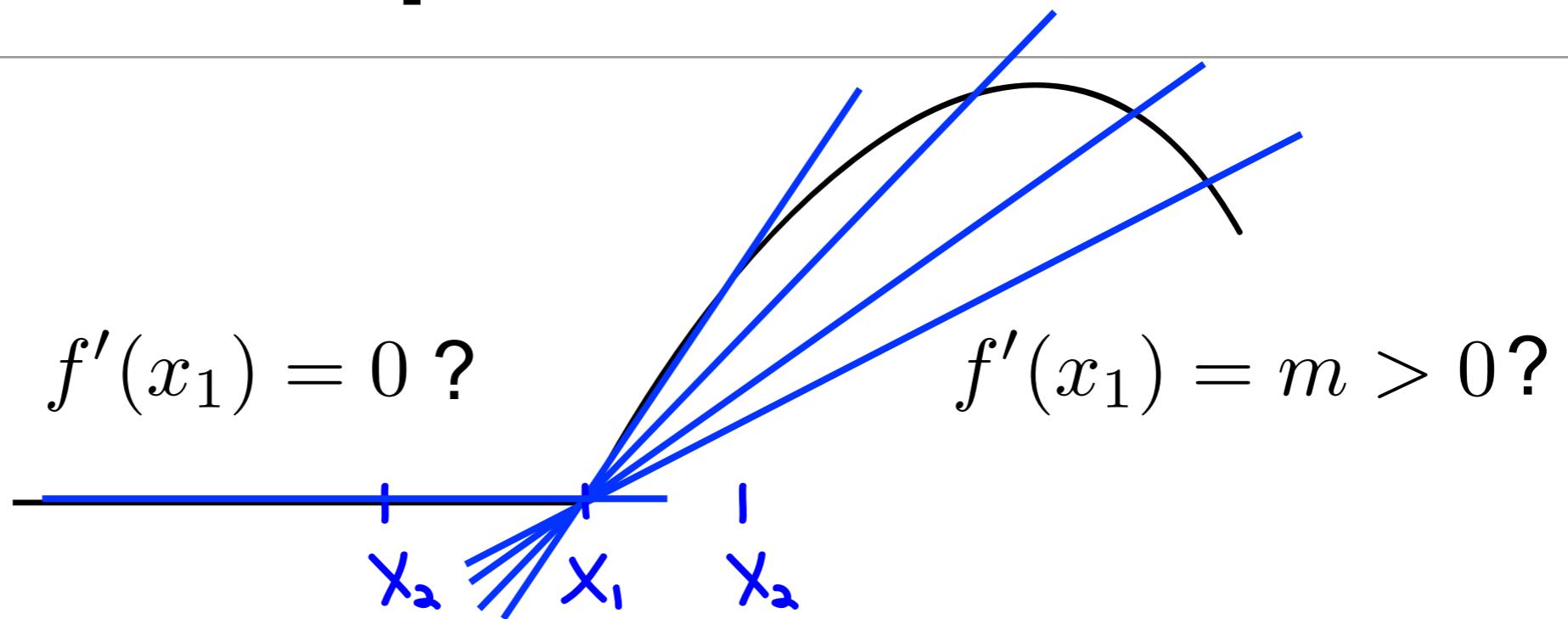
Another example



Another example



Another example



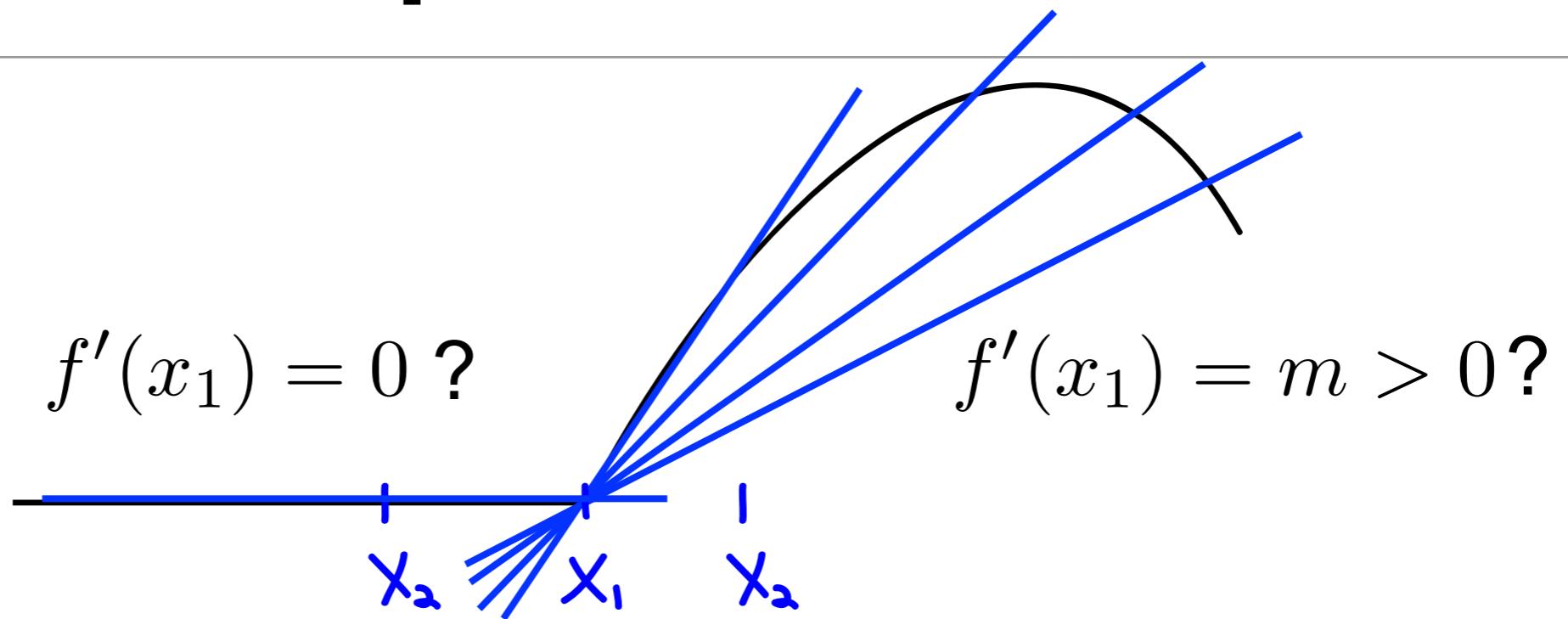
(A) $\lim_{h \rightarrow 0} \frac{f(x_1 + h) - f(x_1)}{h} = m > 0$

(B) $\lim_{h \rightarrow 0} \frac{f(x_1 + h) - f(x_1)}{h} = 0$

(C) Both (A) and (B)

(D) The limit does not exist.

Another example



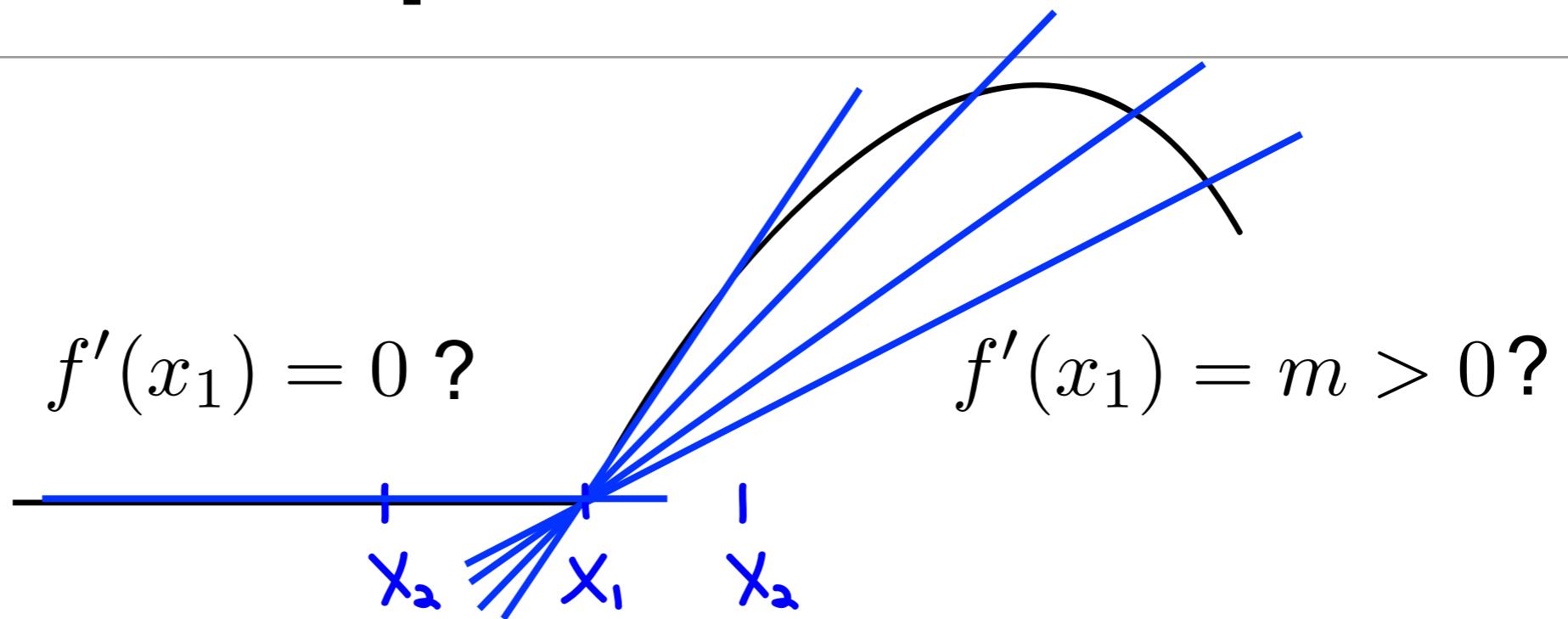
(A) $\lim_{h \rightarrow 0} \frac{f(x_1 + h) - f(x_1)}{h} = m > 0$

(B) $\lim_{h \rightarrow 0} \frac{f(x_1 + h) - f(x_1)}{h} = 0$

(C) Both (A) and (B)

(D) The limit does not exist.

Another example



(A) $\lim_{h \rightarrow 0} \frac{f(x_1 + h) - f(x_1)}{h} = m > 0$

Limits from left and right must agree for the limit to exist.

(B) $\lim_{h \rightarrow 0} \frac{f(x_1 + h) - f(x_1)}{h} = 0$

(C) Both (A) and (B)

(D) The limit does not exist.

The derivative of $f(x)$ at $x=a$...

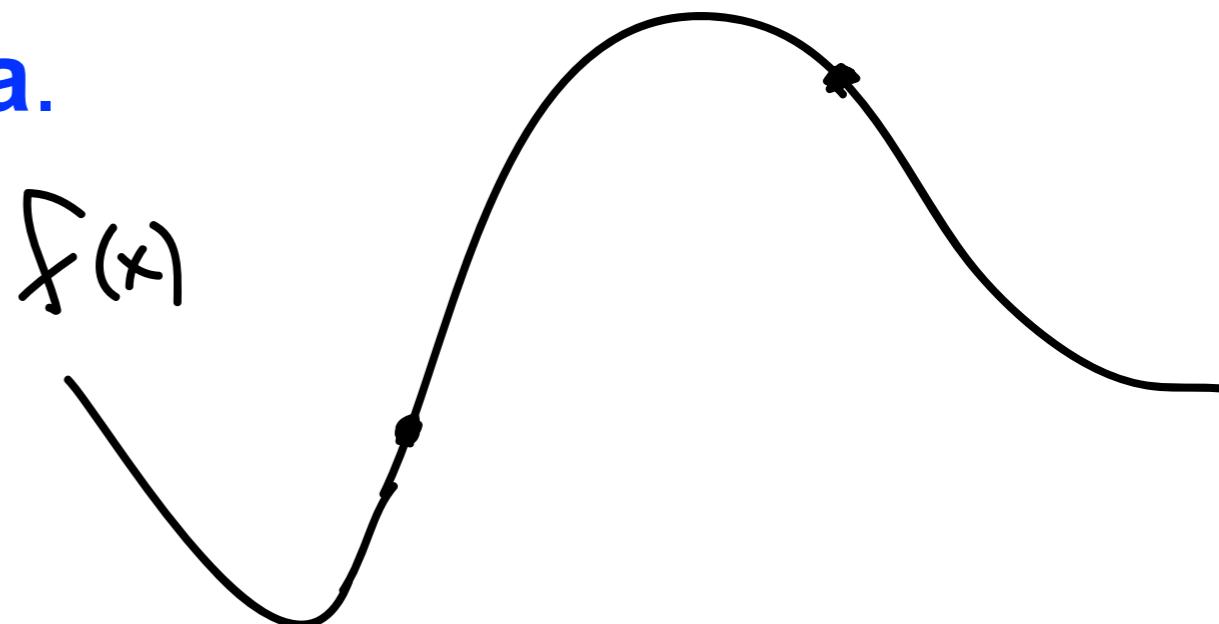
- (A) ...touches the function at $x=a$ but does not cross it.
- (B) ...looks more and more like the function as you zoom in around $x=a$.
- (C) ... only exists when the function looks like a straight line close to $x=a$.
- (D) All of the above.

The derivative of $f(x)$ at $x=a$...

- (A) ...touches the function at $x=a$ but does not cross it.
- (B) ...looks more and more like the function as you zoom in around $x=a$.
- (C) ... only exists when the function looks like a straight line close to $x=a$.
- (D) All of the above.

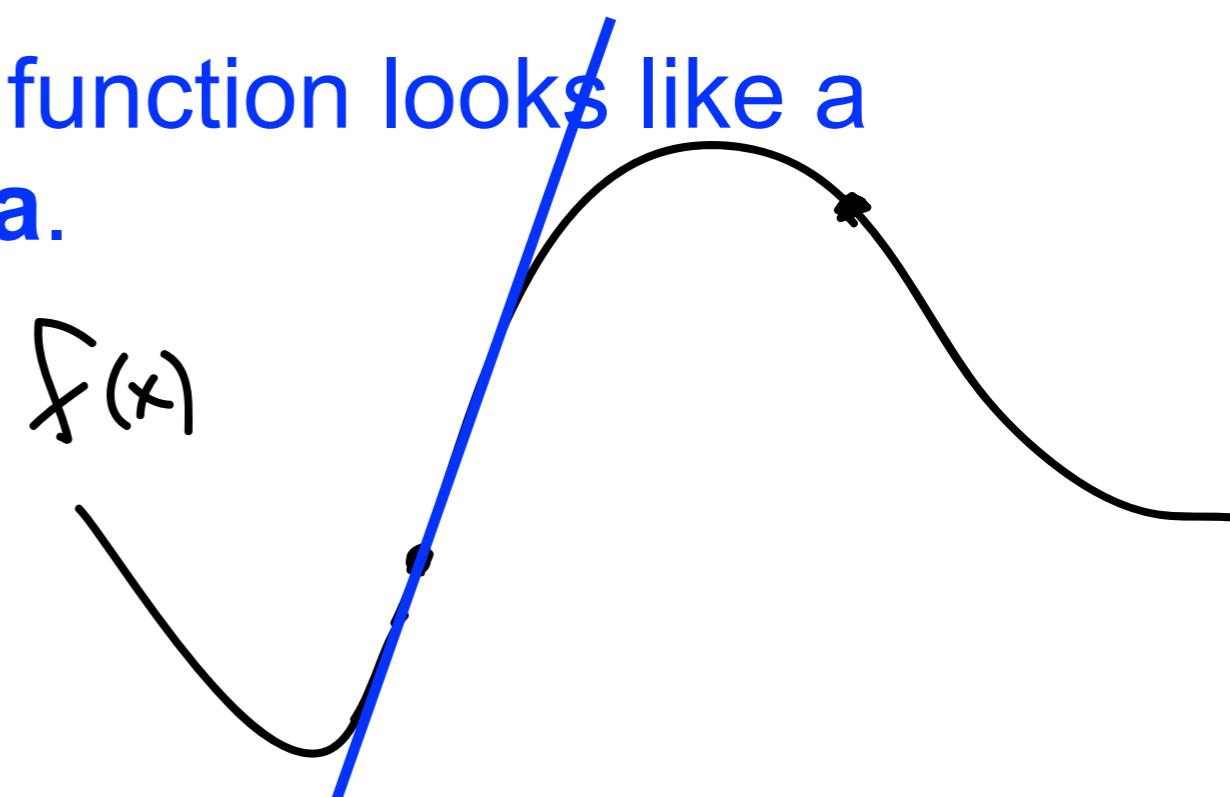
The derivative of $f(x)$ at $x=a$...

- (A) ...touches the function at $x=a$ but does not cross it.
- (B) ...looks more and more like the function as you zoom in around $x=a$.
- (C) ... only exists when the function looks like a straight line close to $x=a$.
- (D) All of the above.



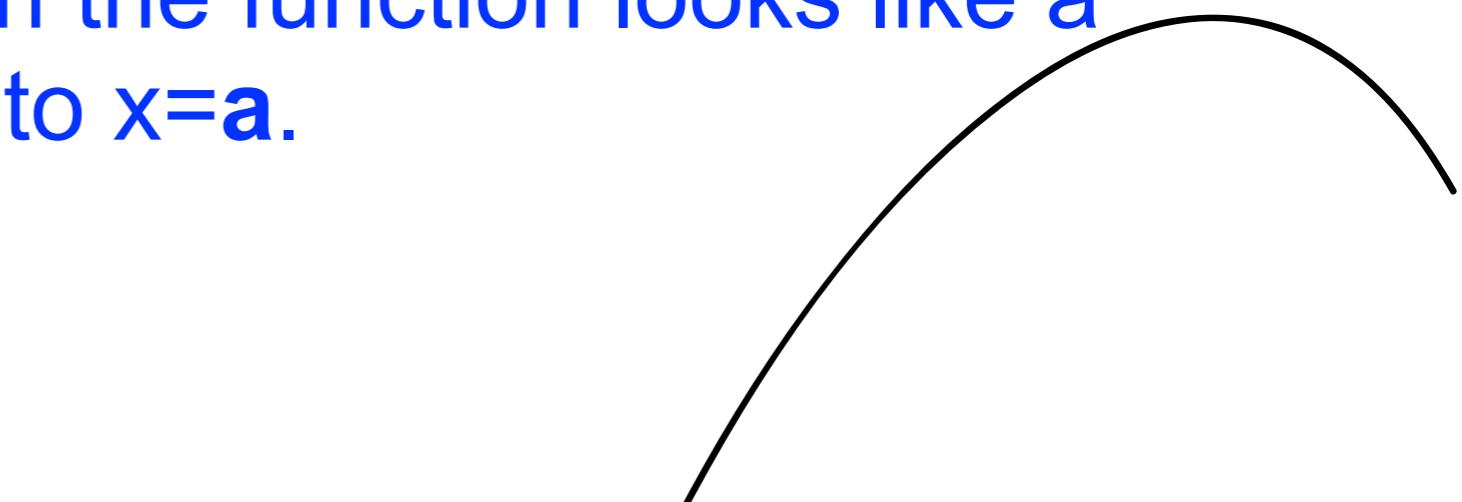
The derivative of $f(x)$ at $x=a$...

- (A) ...touches the function at $x=a$ but does not cross it.
- (B) ...looks more and more like the function as you zoom in around $x=a$.
- (C) ... only exists when the function looks like a straight line close to $x=a$.
- (D) All of the above.



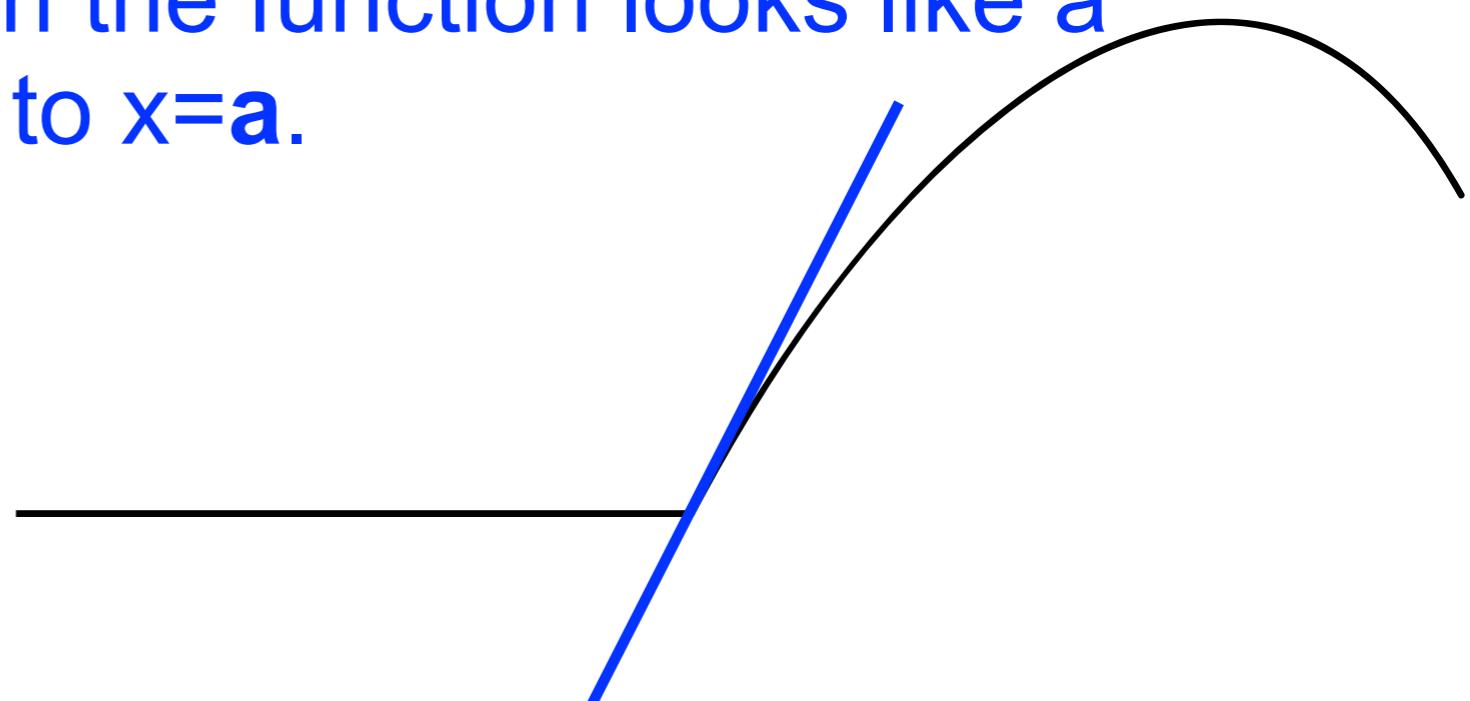
The derivative of $f(x)$ at $x=a$...

- (A) ...touches the function at $x=a$ but does not cross it.
- (B) ...looks more and more like the function as you zoom in around $x=a$.
- (C) ... only exists when the function looks like a straight line close to $x=a$.
- (D) All of the above.



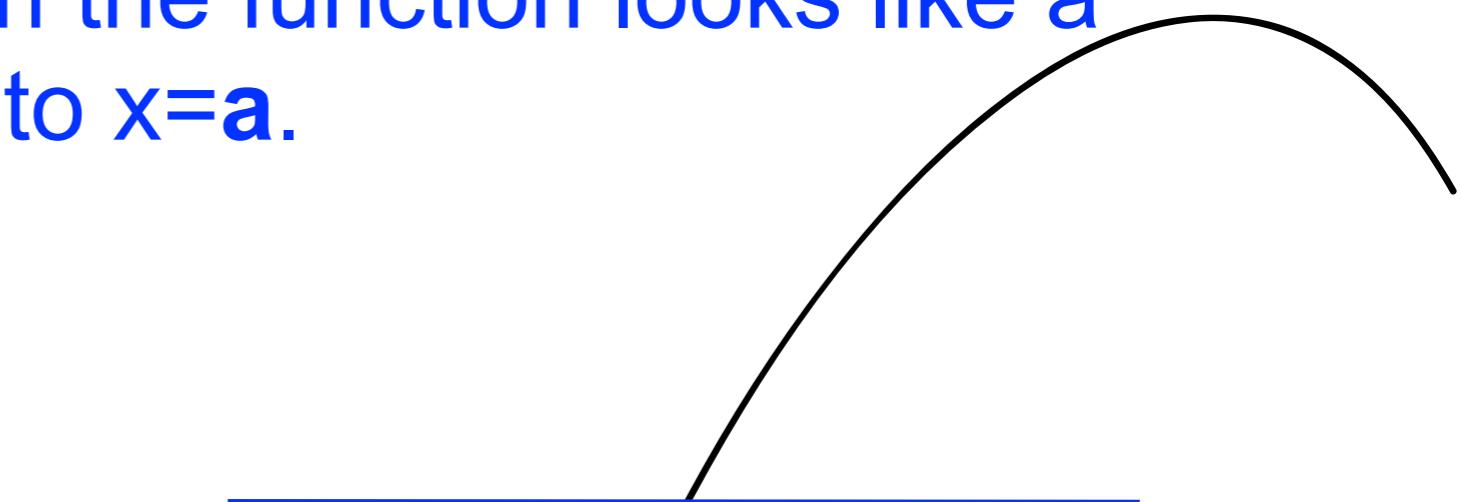
The derivative of $f(x)$ at $x=a$...

- (A) ...touches the function at $x=a$ but does not cross it.
- (B) ...looks more and more like the function as you zoom in around $x=a$.
- (C) ... only exists when the function looks like a straight line close to $x=a$.
- (D) All of the above.



The derivative of $f(x)$ at $x=a$...

- (A) ...touches the function at $x=a$ but does not cross it.
- (B) ...looks more and more like the function as you zoom in around $x=a$.
- (C) ... only exists when the function looks like a straight line close to $x=a$.
- (D) All of the above.



To evaluate a limit

To evaluate $\lim_{x \rightarrow a} f(x)$, you plug in values closer and closer to **a** but you never get to **a**. In fact, **f(a)** may not even be defined. If you always get the same number no matter how you approach **a**, then the limit exists.

To evaluate a limit

To evaluate $\lim_{x \rightarrow a} f(x)$, you plug in values closer and closer to **a** but you never get to **a**. In fact, **f(a)** may not even be defined. If you always get the same number no matter how you approach **a**, then the limit exists.

Note: the limit involved in the derivative is only one special case. The limit above is concerned with the **value** of the function. When a limit has the form

$$\lim_{h \rightarrow 0} \frac{f(2 + h) - f(2)}{h}$$

we're talking about the slope of **f** (in this case, at $x=2$).

A WeBWork limit example

Guess the value of the limit (if it exists) by evaluating the function at values close to where the limit is to be done.
If it does not exist, enter DNE below.

$$\lim_{h \rightarrow 0} \frac{\sin(\frac{\pi}{4} + h) - \sin(\frac{\pi}{4})}{h}$$

Limit:

A WeBWork limit example

Guess the value of the limit (if it exists) by evaluating the function at values close to where the limit is to be done. If it does not exist, enter DNE below.

$$\lim_{h \rightarrow 0} \frac{\sin(\frac{\pi}{4} + h) - \sin(\frac{\pi}{4})}{h}$$

Limit:

Go over $f'(2)$ where $f(x) = 1/x$ on the board.

A WeBWork limit example

Guess the value of the limit (if it exists) by evaluating the function at values close to where the limit is to be done. If it does not exist, enter DNE below.

$$\lim_{h \rightarrow 0} \frac{\sin(\frac{\pi}{4} + h) - \sin(\frac{\pi}{4})}{h}$$

Limit:

Go over $f'(2)$ where $f(x) = 1/x$ on the board.

Do not drop the “lim” along the way!