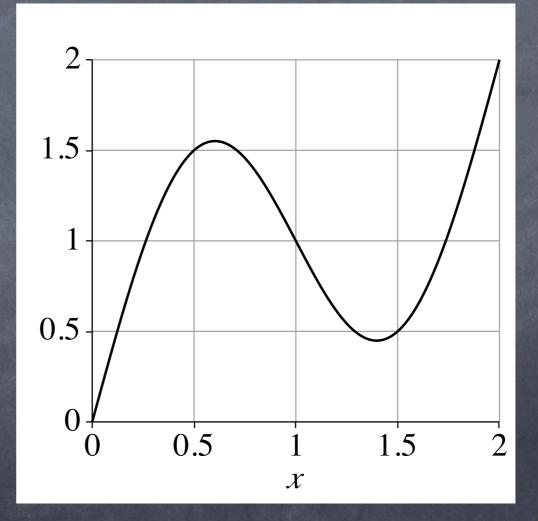
Today

Midterms - come to my office Today 2:30 – 5 pm Tues. 12 – 2 pm Wed. 11 am – 12 pm
 Multiple choice. Optimization examples

Midterm stats

Class average: 64% 18% got below 50%
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 8% got above 90% Max score 98% MC: 53%, SAP: 79%, LAP1: 90%, LAP2: 70%, LAP3 47%. The average rate of change of this function over the interval [a,b] is 1. If a=0, which of the following is possible?

(A) b=0.5(B) b=1(C) b=1.25(D) b=1.5(E) b=1.75



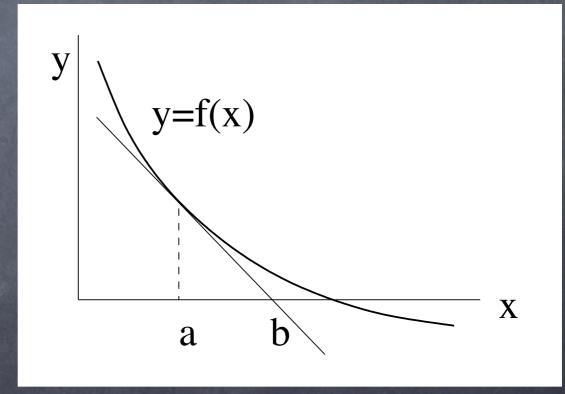
Which of the following describes the derivative of a function f(x)?

(A) It is defined as $\frac{f(x+h) - f(x)}{h}$. (B) The line we see when we zoom into the graph of f(x).

(C) The average rate of change of f(x) over the interval 0 < x < h.
(D) More than one of the above.
(E) None of the above. Which ONE of the following statements is always true for all differentiable functions f that satisfy the stated condition. (A) When f''(a) = 0, the function f(x) has an inflection point at x=a. (B) If f(x) has a local maximum at a then f'(a) < 0 and f''(a) = 0. (C) If f(x) has a local minimum at a then f'(a) = 0 and f''(a) < 0. (D) If f(x) is increasing and concave up at a then f'(a) > 0 and f''(a) > 0. (E) Both the functions $f(x) = x^3$ and f(x) = x^6 have inflection points at x=0.

As shown in the figure below, the tangent line to the graph of f(x) at x=a intersects the x-axis at x=b. Which of the following expressions gives the value of b?

(A) b=a-f(a)/f'(a).
(B) b=a+f(a)/f'(a).
(C) b=a+f'(b)/f(b).
(D) b=f(a)-f'(a)a.
(E) b=f(a)+f'(a)(x-a).



In order for the function $f(x) = 1/3 x^3 + 2x^2$ +qx+2 to have any critical points, we require that the constant q satisfy which of the following statements?

(A) $0 \le q \le 16$ (B) $q \ge 2$ (C) $4 \le q \le 16$ (D) $q \le -4$ or $q \ge 4$ (E) $q \le 4$

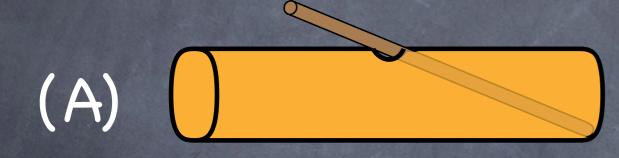


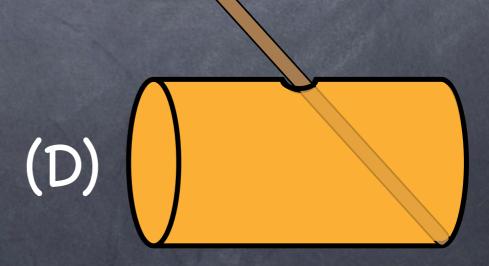
Wine was sold by "the length of the submerged part of the rod"

Same length of wet rod = same volume of wine?

Which barrel would you buy?

(C)

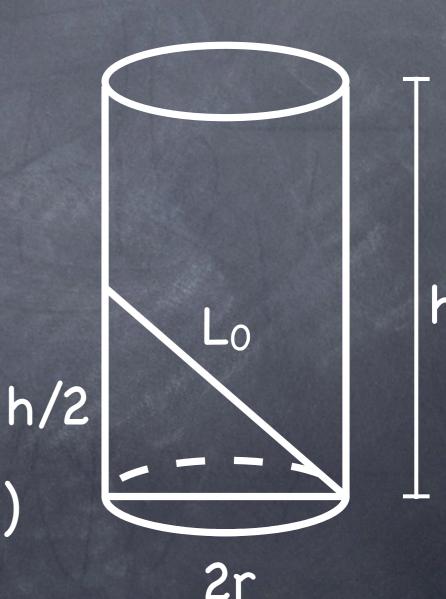




(B)

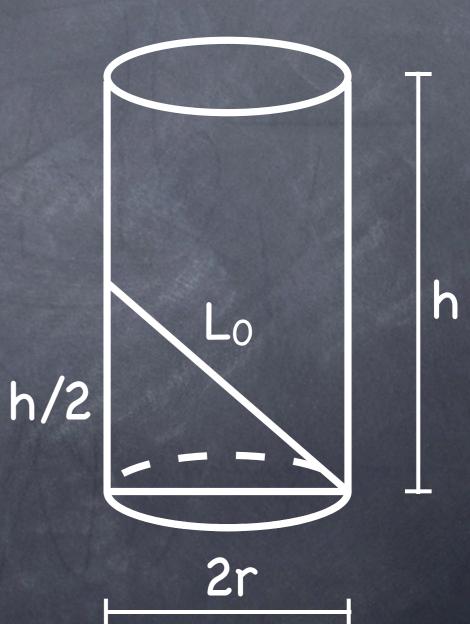
Objective function? (to be maximized)

(A) V = $2\pi rh$ (B) $r^2 = L_0^2/4 - h^2/16$ (C) V = $\pi r^2 h$ r^2 (D) $L_0 = sqrt((2r)^2 + (h/2)^2)$



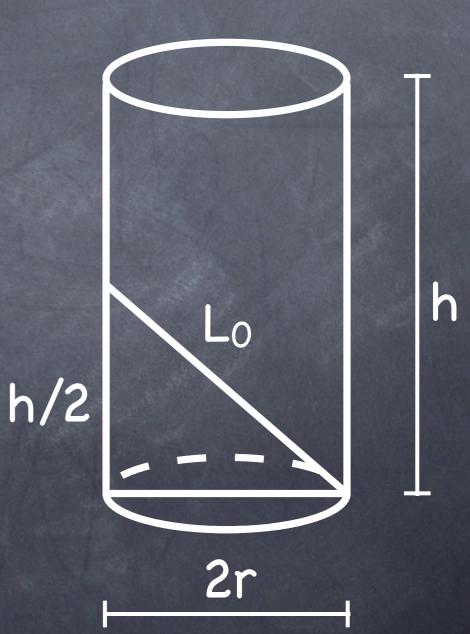
Constraint? (used to simplify OF)

(A) $L_0^2 = (2r)^2 + (h/2)^2$ (B) $L_0^2 = (2r)^2 + h^2$ (C) V = $2\pi rh$ (D) $L_0 = tan(h/4r)$



Constraint? (used to simplify OF)

(A) $L_0^2 = (2r)^2 + (h/2)^2$ (B) $L_0^2 = (2r)^2 + h^2$ (C) V = $2\pi rh$ (D) $L_0 = tan(h/4r)$



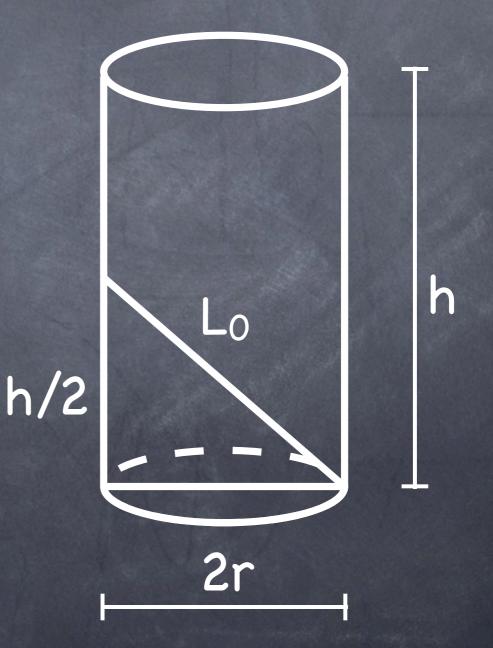
Objective functions: $V = \pi r^2 h$. Constraint: $L_0^2 = (2r)^2 + (h/2)^2$. Solve for: (A) r (B) r² (C) h (D) h^2

Objective functions: $V = \pi r^2 h$. Constraint: $L_0^2 = (2r)^2 + (h/2)^2$. Solve for: (A) r (B) r² (C) h (D) h^2

$V = \pi h (4L_0^2 - h^2)/16$ What is the best h?

(A) h = 0 (B) h = $2L_0$ (C) h = $\sqrt{3} L_0$ (D) h = $2L_0/\sqrt{3}$

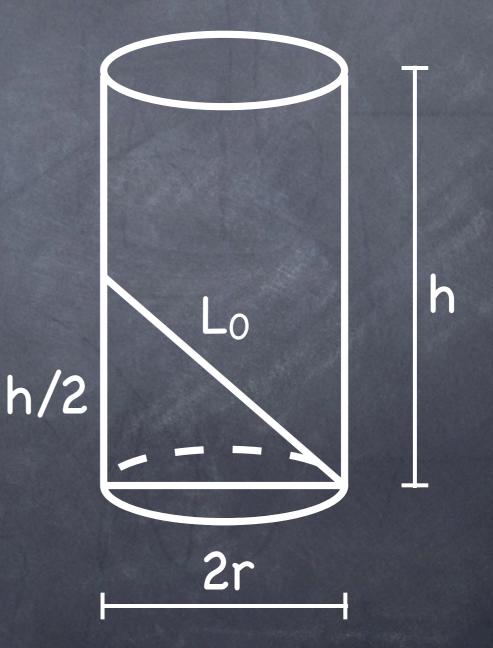
Did you check V"(h)?



$V = \pi h (4L_0^2 - h^2)/16$ What is the best h?

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Did you check V"(h)?



<u>http://www.matematicasvisuales.com/english/html/</u> <u>history/kepler/doliometry.html</u>

Overall procedure

- 1. Draw a sketch.
- 2. Determine the objective function.
- 3. Determine the constraint.
- 4. Establish an expectation (end-points or local extremum).
- 5. Solve constraint for one variable (make your life easy if possible).
- 6. Substitute it into the objective function.
- 7. Find the absolute extremum (check concavity!).