## OSH 5 Math 104 - Section 107

**Question 1** (2 points) Let  $f(x) = e^{\sin x}$ . Find the inflection points of f(x) on the interval  $[0, 2\pi]$ .

**Question 2** (2 points) A rancher wants to use 100 meters of fence to build a barn shaped as circular sector (see the picture). What is the maximal possible area of such a barn?



Question 3 (2 points) Of all points on the parabola  $y = x^2 + x$ , which one is the closest to the point (1, -1)? (Hint:  $(a + b + c)^2 = a^2 + b^2 + c^2 + 2ab + 2bc + 2ca$ .)

Question 4 (4 points) Do the following for each of the functions below:

- Find increasing and decreasing intervals.
- Find local extremities.
- Final concaving up and concaving down intervals.
- Find inflection points.
- Find all asymptotes (horizontal, vertical and oblique).
- Draw a graph of the function, indicating all previous information.

The functions:

1. 
$$f(x) = \frac{2x}{x^2 + 1}$$

2.  $f(x) = \frac{1}{x^3 - 3x}$