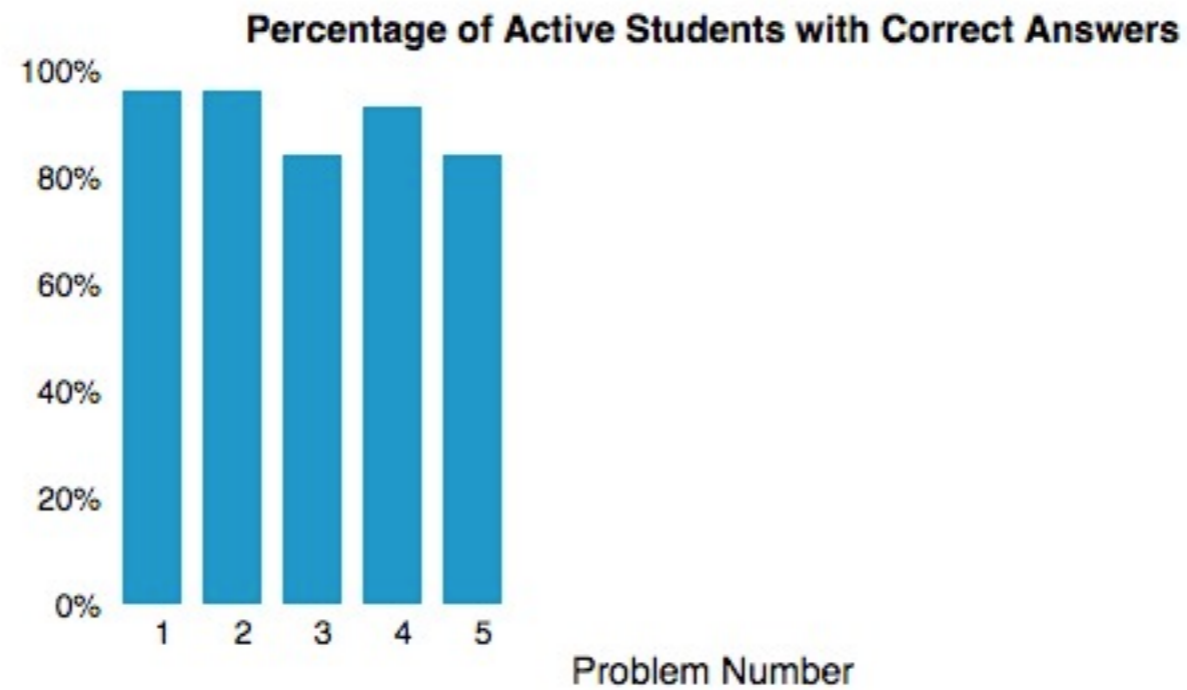


Today

- Comment on pre-lecture problems
- Finish up with integrating factors
- The structure of solutions
- Separable equations

Pre-lecture assignment comments

Pre-lecture assignment comments



Pre-lecture assignment comments

Consider the initial value problem

$$\frac{dy}{dt} - 5y = 4e^{2t}, \quad y(0) = A.$$

a. Find the solution.

$y =$

b. For what values of A does the above solution tend to ∞ , 0 or $-\infty$ as $t \rightarrow \infty$?

As $t \rightarrow \infty$,

$y \rightarrow \infty$ if $A \in$

$y \rightarrow 0$ if $A \in$

$y \rightarrow -\infty$ if $A \in$

Pre-lecture assignment comments

Solve the differential equation $\frac{dy}{dx} = \frac{x}{9y}$.

- a. Find the equation of the solution through the point $(x, y) = (-3, 1)$.

[help \(equations\)](#)

- b. Find the equation of the solution through the point $(x, y) = (0, -3)$.

[help \(equations\)](#)

Method of integrating factors (Section 2.1)

$$\frac{d}{dt} (t^2 y(t)) =$$

(A) $2t \frac{dy}{dt}$

(B) $t^2 \frac{dy}{dt}$

(C) $2ty$

(D) $t^2 \frac{dy}{dt} + 2ty$

(E) Don't know.

Method of integrating factors (Section 2.1)

$$\frac{d}{dt} (t^2 y(t)) =$$

(A) $2t \frac{dy}{dt}$

(B) $t^2 \frac{dy}{dt}$

(C) $2ty$

(D) $t^2 \frac{dy}{dt} + 2ty$

(E) Don't know.

Method of integrating factors (Section 2.1)

- Given that $\frac{d}{dt} (t^2 y(t)) = t^2 \frac{dy}{dt} + 2ty$

- if you're given the equation $t^2 \frac{dy}{dt} + 2ty = 0$

- you can rewrite it as $\frac{d}{dt} (t^2 y(t)) = 0$

- so the solution is $t^2 y(t) = C$ or equivalently $y(t) = \frac{C}{t^2}$.

arbitrary constant
that appeared at an
integration step



Method of integrating factors (Section 2.1)

- Solve the equation $t^2 \frac{dy}{dt} + 2ty(t) = \sin(t)$ (not brute force checking).

(A) $y(t) = -\cos(t) + C$

(B) $y(t) = \frac{C - \cos(t)}{t^2}$

(C) $y(t) = \sin(t) + C$

(D) $y(t) = -\frac{1}{t^2} \cos(t)$

(E) Don't know.

Method of integrating factors (Section 2.1)

- Solve the equation $t^2 \frac{dy}{dt} + 2ty(t) = \sin(t)$ (not brute force checking).

(A) $y(t) = -\cos(t) + C$

(B) $y(t) = \frac{C - \cos(t)}{t^2}$

(C) $y(t) = \sin(t) + C$

(D) $y(t) = -\frac{1}{t^2} \cos(t)$

(E) Don't know.

← general solution
(although that's not
obvious)

← a particular solution

Initial conditions (IC) and initial value problems (IVP)

(E) Don't know.

Initial conditions (IC) and initial value problems (IVP)

- An initial condition is an added constraint on a solution.

(E) Don't know.

Initial conditions (IC) and initial value problems (IVP)

- An initial condition is an added constraint on a solution.
- e.g. Solve $t^2 \frac{dy}{dt} + 2ty(t) = \sin(t)$ subject to the IC $y(\pi) = 0$.

(E) Don't know.

Initial conditions (IC) and initial value problems (IVP)

- An initial condition is an added constraint on a solution.
- e.g. Solve $t^2 \frac{dy}{dt} + 2ty(t) = \sin(t)$ subject to the IC $y(\pi) = 0$.

(A) $y(t) = -\frac{C + \cos(\pi)}{\pi^2}$

(B) $y(t) = -\frac{1 - \cos(t)}{t^2}$

(C) $y(t) = \frac{1 + \cos(t)}{t^2}$

(D) $y(t) = -\frac{1 + \cos(t)}{t^2}$

(E) Don't know.

Initial conditions (IC) and initial value problems (IVP)

- An initial condition is an added constraint on a solution.
- e.g. Solve $t^2 \frac{dy}{dt} + 2ty(t) = \sin(t)$ subject to the IC $y(\pi) = 0$.

(A) $y(t) = -\frac{C + \cos(\pi)}{\pi^2}$

(B) $y(t) = -\frac{1 - \cos(t)}{t^2}$

(C) $y(t) = \frac{1 + \cos(t)}{t^2}$

(D) $y(t) = -\frac{1 + \cos(t)}{t^2}$

(E) Don't know.

- An Initial Value Problem (IVP) is a ODE together with an IC.

Method of integrating factors (Section 2.1)

- What's the integrating factor?

$$t \frac{dy}{dt} + 2y(t) = 1$$

$$t^2 \frac{dy}{dt} + 4ty(t) = \frac{1}{t}$$

$$\frac{dy}{dt} + y(t) = 0$$

$$\frac{dy}{dt} + \cos(t)y(t) = 0$$

$$\frac{dy}{dt} + g'(t)y(t) = 0$$

Method of integrating factors (Section 2.1)

- What's the integrating factor?

$$t \frac{dy}{dt} + 2y(t) = 1 \quad \rightarrow f(t) = t$$

$$t^2 \frac{dy}{dt} + 4ty(t) = \frac{1}{t}$$

$$\frac{dy}{dt} + y(t) = 0$$

$$\frac{dy}{dt} + \cos(t)y(t) = 0$$

$$\frac{dy}{dt} + g'(t)y(t) = 0$$

Method of integrating factors (Section 2.1)

- What's the integrating factor?

$$t \frac{dy}{dt} + 2y(t) = 1 \quad \rightarrow f(t) = t$$

$$t^2 \frac{dy}{dt} + 4ty(t) = \frac{1}{t} \quad \rightarrow f(t) = t^2$$

$$\frac{dy}{dt} + y(t) = 0$$

$$\frac{dy}{dt} + \cos(t)y(t) = 0$$

$$\frac{dy}{dt} + g'(t)y(t) = 0$$

Method of integrating factors (Section 2.1)

- What's the integrating factor?

$$t \frac{dy}{dt} + 2y(t) = 1 \quad \rightarrow f(t) = t$$

$$t^2 \frac{dy}{dt} + 4ty(t) = \frac{1}{t} \quad \rightarrow f(t) = t^2$$

$$\frac{dy}{dt} + y(t) = 0 \quad \rightarrow f(t) = e^t$$

$$\frac{dy}{dt} + \cos(t)y(t) = 0$$

$$\frac{dy}{dt} + g'(t)y(t) = 0$$

Method of integrating factors (Section 2.1)

- What's the integrating factor?

$$t \frac{dy}{dt} + 2y(t) = 1 \quad \rightarrow f(t) = t$$

$$t^2 \frac{dy}{dt} + 4ty(t) = \frac{1}{t} \quad \rightarrow f(t) = t^2$$

$$\frac{dy}{dt} + y(t) = 0 \quad \rightarrow f(t) = e^t$$

$$\frac{dy}{dt} + \cos(t)y(t) = 0 \quad \rightarrow f(t) = e^{\sin(t)}$$

$$\frac{dy}{dt} + g'(t)y(t) = 0$$

Method of integrating factors (Section 2.1)

- What's the integrating factor?

$$t \frac{dy}{dt} + 2y(t) = 1 \quad \rightarrow f(t) = t$$

$$t^2 \frac{dy}{dt} + 4ty(t) = \frac{1}{t} \quad \rightarrow f(t) = t^2$$

$$\frac{dy}{dt} + y(t) = 0 \quad \rightarrow f(t) = e^t$$

$$\frac{dy}{dt} + \cos(t)y(t) = 0 \quad \rightarrow f(t) = e^{\sin(t)}$$

$$\frac{dy}{dt} + g'(t)y(t) = 0 \quad \rightarrow f(t) = e^{g(t)}$$

Method of integrating factors (Section 2.1)

- What's the integrating factor?

$$t \frac{dy}{dt} + 2y(t) = 1 \quad \rightarrow f(t) = t$$

$$t^2 \frac{dy}{dt} + 2ty(t) = 1 \quad \rightarrow f(t) = t^2$$

In class, I referred to these $f(t)$ functions as the integrating factors. This is incorrect. They are functions that you can multiply the ORIGINAL equation by to get a perfect “product rule” form. But an integrating factor is defined as the function that you would multiply the “normalized” equation by to get the “product rule” form. By “normalized”, I mean after dividing through by the coefficient on dy/dt . So for the first example above, the integrating factor would be $I(t)=t^2$ and the equation you multiply it through is $dy/dt + 2/t y = 1/t$.

$$\frac{dy}{dt} + g'(t)y(t) = 0 \quad \rightarrow f(t) = e^{g(t)}$$

Method of integrating factors (Section 2.1)

- General case - all first order linear ODEs can be written in the form

$$\frac{dy}{dt} + p(t)y = q(t)$$

Method of integrating factors (Section 2.1)

- General case - all first order linear ODEs can be written in the form

$$\frac{dy}{dt} + p(t)y = q(t)$$

- The appropriate integrating factor is $e^{\int p(t)dt}$.

Method of integrating factors (Section 2.1)

- General case - all first order linear ODEs can be written in the form

$$\frac{dy}{dt} + p(t)y = q(t)$$

- The appropriate integrating factor is $e^{\int p(t)dt}$.

- The equation can be rewritten $\frac{d}{dt} \left(e^{\int p(t)dt} y \right) = e^{\int p(t)dt} q(t)$ which is solvable provided you can find the antiderivative of the right hand side.

Method of integrating factors (Section 2.1)

- General case - all first order linear ODEs can be written in the form

$$\frac{dy}{dt} + p(t)y = q(t)$$

- The appropriate integrating factor is $e^{\int p(t)dt}$.

- The equation can be rewritten $\frac{d}{dt} \left(e^{\int p(t)dt} y \right) = e^{\int p(t)dt} q(t)$ which is solvable provided you can find the antiderivative of the right hand side.

$$e^{\int p(t)dt} y(t) = \int e^{\int p(t)dt} q(t) dt + C$$

Method of integrating factors (Section 2.1)

- General case - all first order linear ODEs can be written in the form

$$\frac{dy}{dt} + p(t)y = q(t)$$

- The appropriate integrating factor is $e^{\int p(t)dt}$.
- The equation can be rewritten $\frac{d}{dt} \left(e^{\int p(t)dt} y \right) = e^{\int p(t)dt} q(t)$ which is solvable provided you can find the antiderivative of the right hand side.

$$e^{\int p(t)dt} y(t) = \int e^{\int p(t)dt} q(t) dt + C$$

$$y(t) = e^{-\int p(t)dt} \int e^{\int p(t)dt} q(t) dt + C e^{-\int p(t)dt}$$

The structure of solutions

- When the equation is of the form (called homogeneous)

$$\frac{dy}{dt} + p(t)y = 0$$

- the solution is

$$y(t) = C\mu(t)^{-1}$$

- where

$$\mu(t) = \exp\left(\int p(t)dt\right)$$

- is the integrating factor.

The structure of solutions

- When the equation is of the form (called nonhomogeneous)

$$\frac{dy}{dt} + p(t)y = q(t)$$

- the solution is $y(t) = k(t) + C\mu(t)^{-1}$
- where $k(t)$ involves no arbitrary constants.
- Think about this expression as $y(t) = y_p(t) + y_h(t)$
- Directly analogous to solving the vector equations $A\bar{x} = 0$ and $A\bar{x} = \bar{b}$.

Examples

- Find the general solution to

$$t \frac{dy}{dt} + 2y = 4t^2$$

- and plot a few of the integral curves.
- Integral curve - the graph of a solution to an ODE.

Examples

- Find the general solution to

$$t \frac{dy}{dt} + 2y = 4t^2$$

- and plot a few of the integral curves.
- Integral curve - the graph of a solution to an ODE.

(A) $y(t) = t^2$

(B) $y(t) = t^2 + C \frac{1}{t^2}$

(C) $y(t) = t^2 + C$

(D) $y(t) = C \frac{1}{t^2}$

(E) Don't know.

Examples

- Find the general solution to

$$t \frac{dy}{dt} + 2y = 4t^2$$

- and plot a few of the integral curves.
- Integral curve - the graph of a solution to an ODE.

$$y(t) = t^2 + C \frac{1}{t^2}$$

(A) $y(t) = t^2$

(B) $y(t) = t^2 + C \frac{1}{t^2}$

(C) $y(t) = t^2 + C$

(D) $y(t) = C \frac{1}{t^2}$

(E) Don't know.

Examples

- Find the general solution to

$$t \frac{dy}{dt} + 2y = 4t^2$$

- and plot a few of the integral curves.
- Integral curve - the graph of a solution to an ODE.

$$y(t) = t^2 + C \frac{1}{t^2}$$

- Steps: divide through by t , calculate $I(t)$, take antiderivatives, solve for y .
Or shortcut.

(A) $y(t) = t^2$

(B) $y(t) = t^2 + C \frac{1}{t^2}$

(C) $y(t) = t^2 + C$

(D) $y(t) = C \frac{1}{t^2}$

(E) Don't know.

Examples

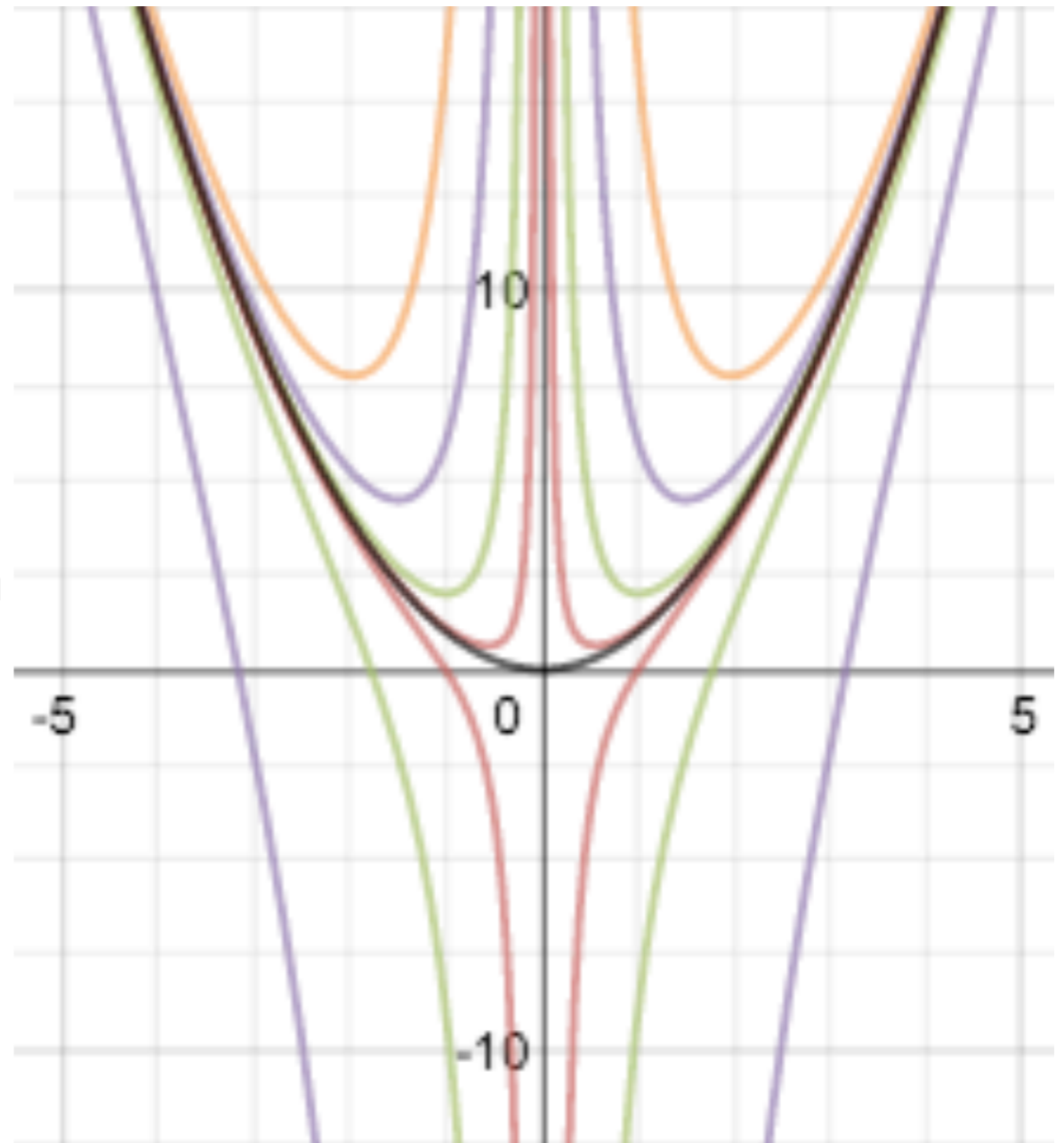
- Find the general solution to

$$t \frac{dy}{dt} + 2y = 4t^2$$

- and plot a few of the integral curves.
- Integral curve - the graph of a solution to an ODE.

$$y(t) = t^2 + C \frac{1}{t^2}$$

- Steps: divide through by t , calculate $I(t)$, take antiderivatives, solve for y . Or shortcut.



Examples

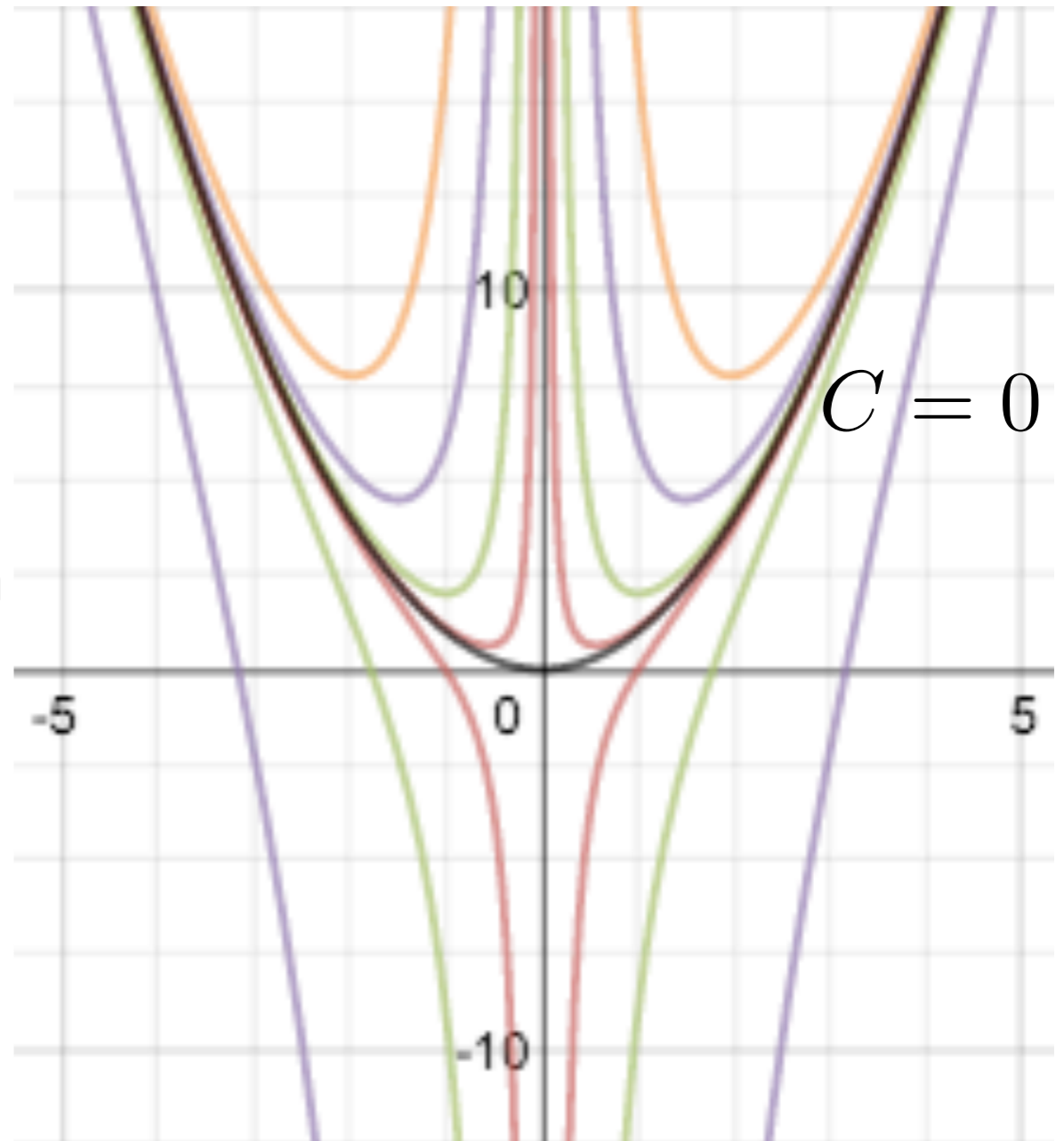
- Find the general solution to

$$t \frac{dy}{dt} + 2y = 4t^2$$

- and plot a few of the integral curves.
- Integral curve - the graph of a solution to an ODE.

$$y(t) = t^2 + C \frac{1}{t^2}$$

- Steps: divide through by t , calculate $I(t)$, take antiderivatives, solve for y . Or shortcut.



Examples

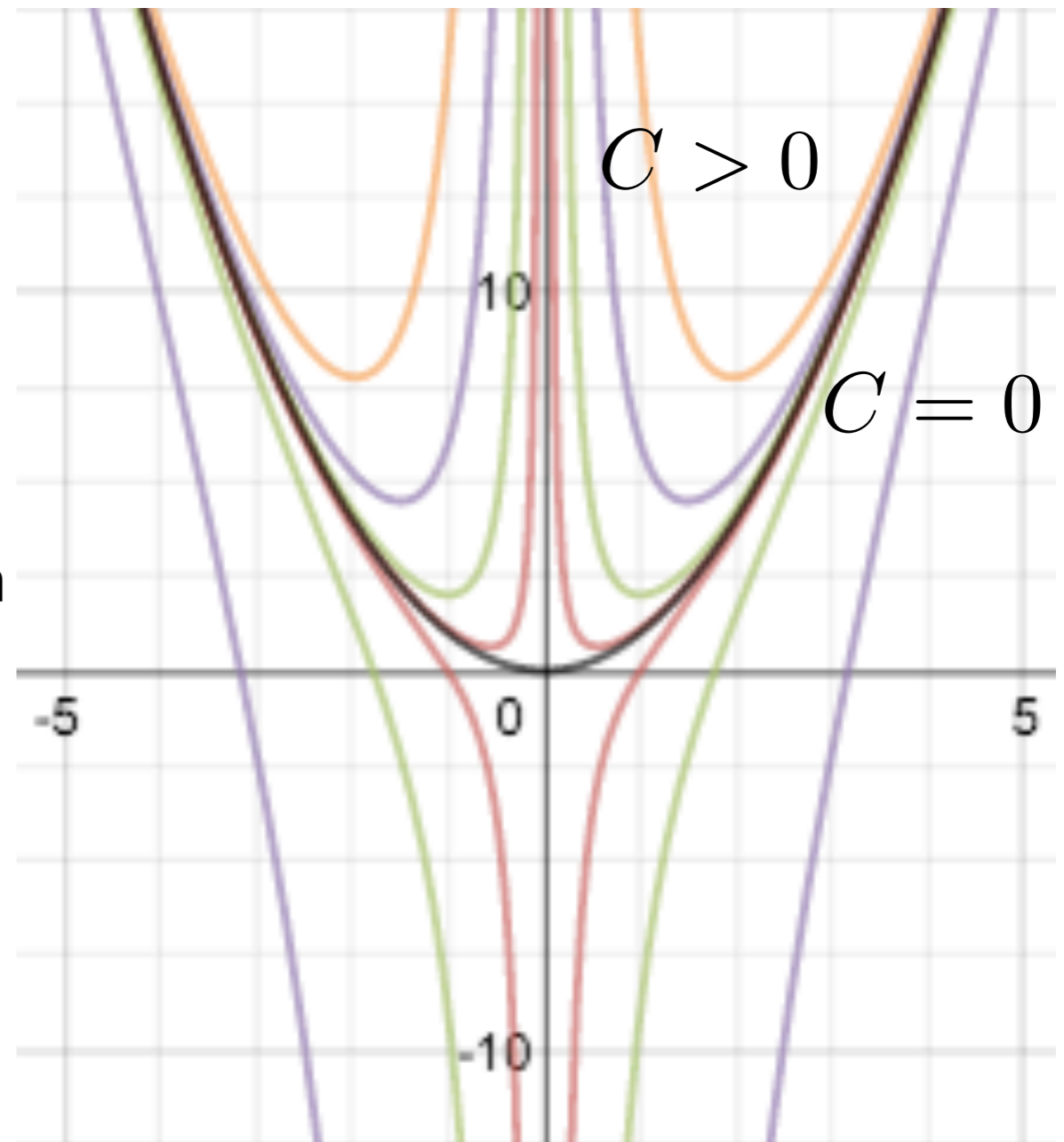
- Find the general solution to

$$t \frac{dy}{dt} + 2y = 4t^2$$

- and plot a few of the integral curves.
- Integral curve - the graph of a solution to an ODE.

$$y(t) = t^2 + C \frac{1}{t^2}$$

- Steps: divide through by t , calculate $I(t)$, take antiderivatives, solve for y . Or shortcut.



Examples

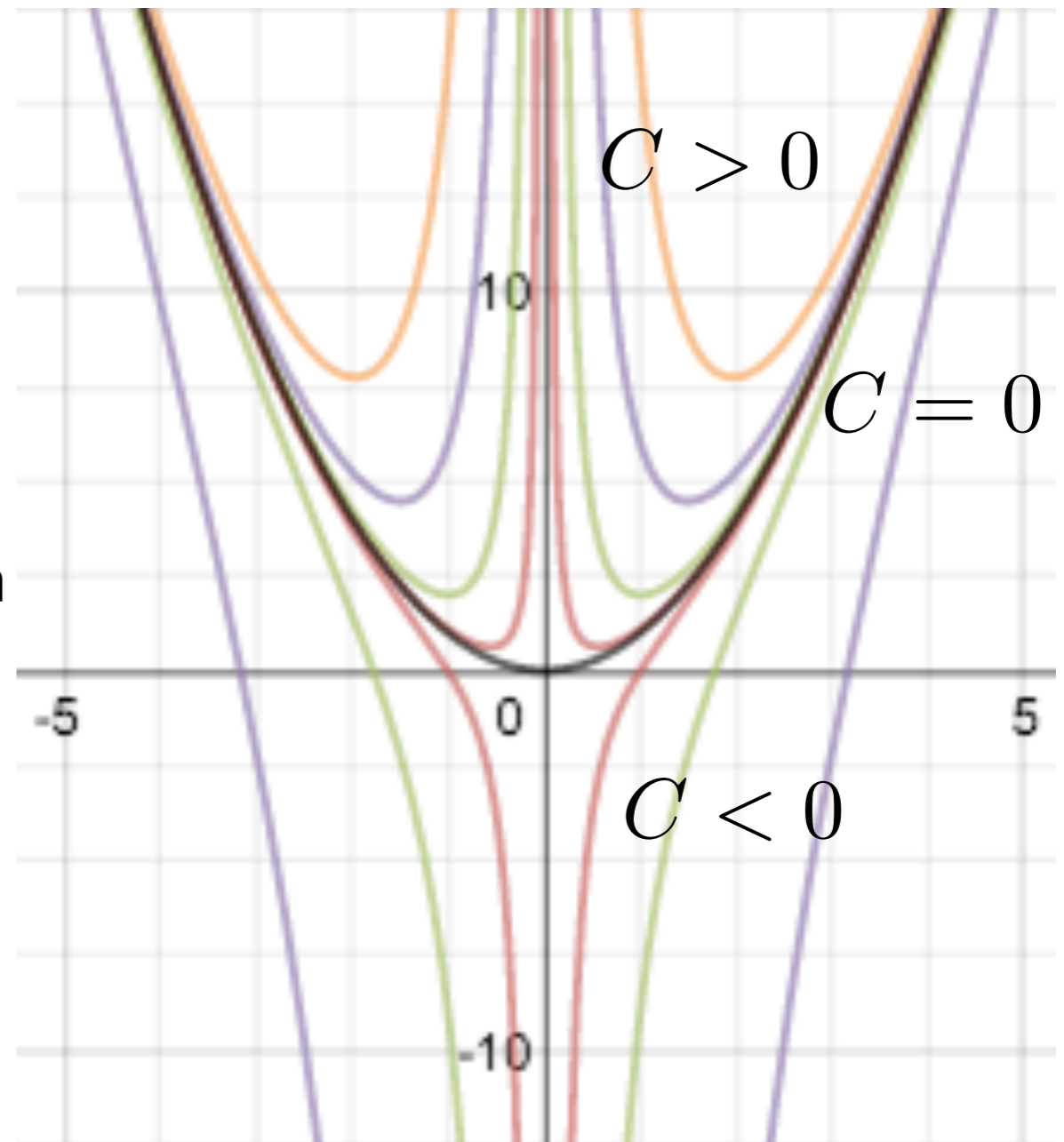
- Find the general solution to

$$t \frac{dy}{dt} + 2y = 4t^2$$

- and plot a few of the integral curves.
- Integral curve - the graph of a solution to an ODE.

$$y(t) = t^2 + C \frac{1}{t^2}$$

- Steps: divide through by t , calculate $I(t)$, take antiderivatives, solve for y . Or shortcut.



Examples

- Find the general solution to

$$\frac{dy}{dt} - 3y = -4e^{-t}$$

- and plot a few of the integral curves.

Examples

- Find the general solution to

$$\frac{dy}{dt} - 3y = -4e^{-t}$$

- and plot a few of the integral curves.

(A) $y(t) = e^{-t}$

(B) $y(t) = e^{-t} + Ce^{3t}$

(C) $y(t) = e^{-3t}$

(D) $y(t) = e^{-4t} + C$

(E) Don't know.

Examples

- Find the general solution to

$$\frac{dy}{dt} - 3y = -4e^{-t}$$

- and plot a few of the integral curves.

$$y(t) = e^{-t} + Ce^{3t}$$

(A) $y(t) = e^{-t}$

(B) $y(t) = e^{-t} + Ce^{3t}$

(C) $y(t) = e^{-3t}$

(D) $y(t) = e^{-4t} + C$

(E) Don't know.

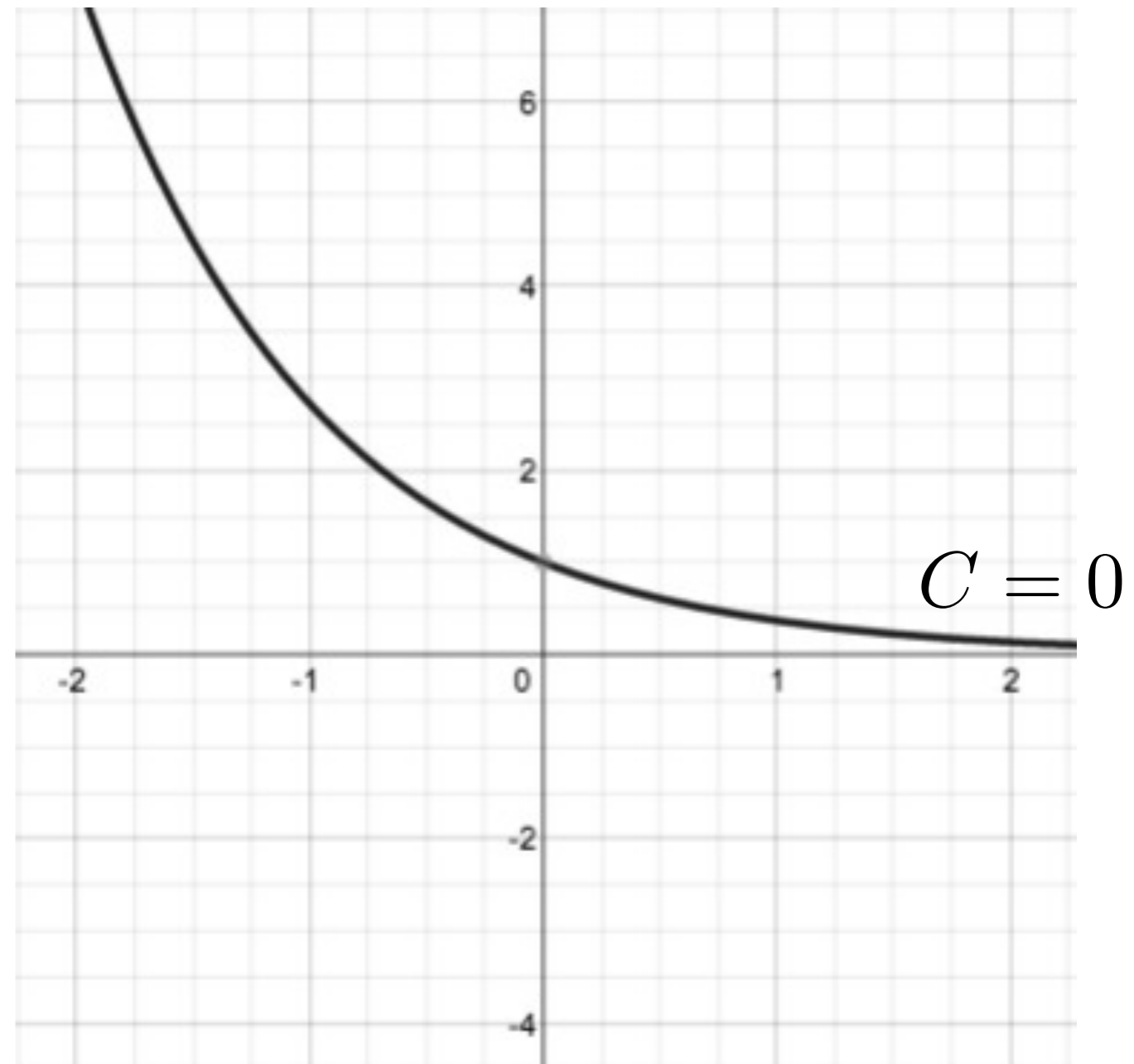
Examples

- Find the general solution to

$$\frac{dy}{dt} - 3y = -4e^{-t}$$

- and plot a few of the integral curves.

$$y(t) = e^{-t} + Ce^{3t}$$



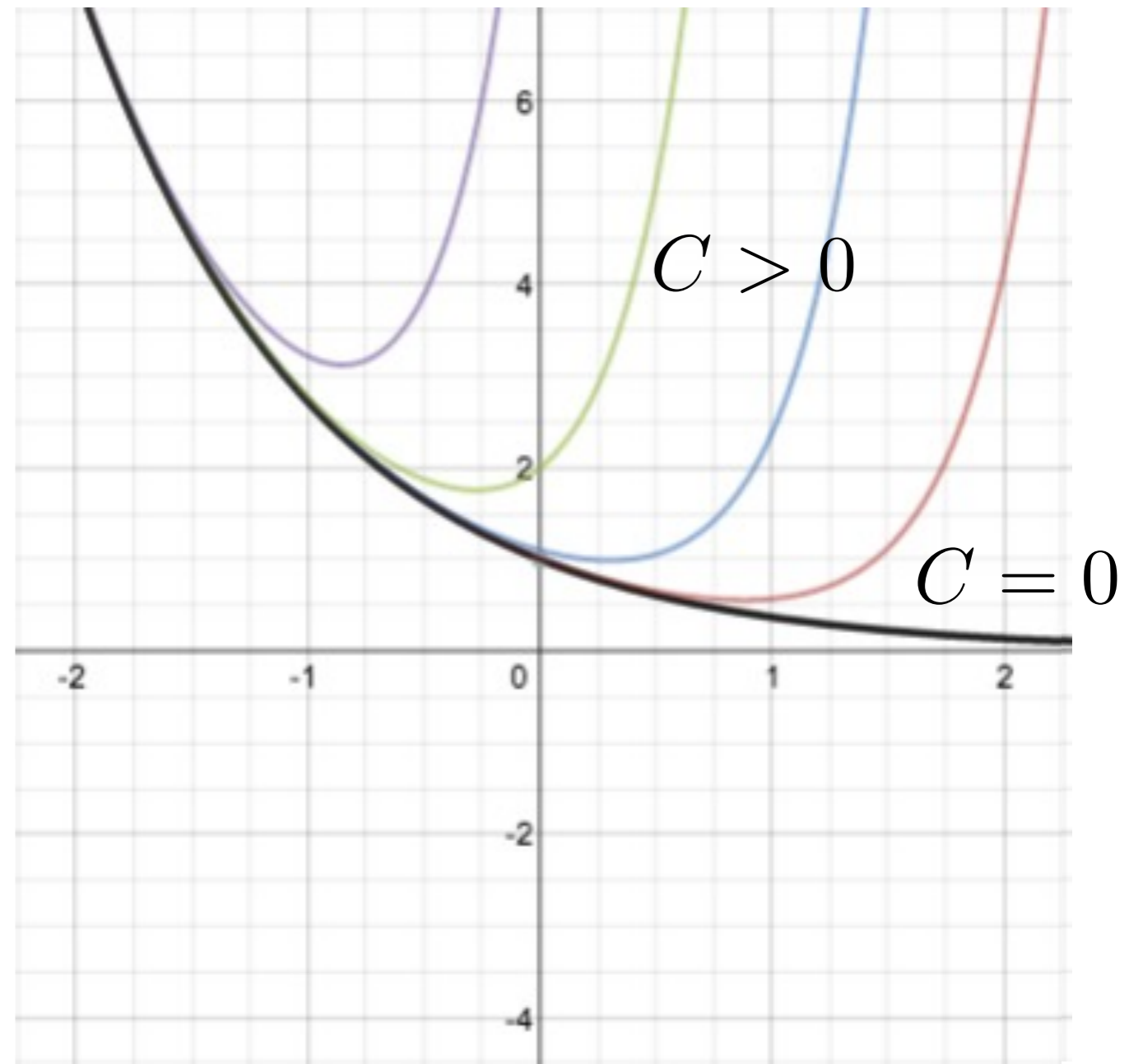
Examples

- Find the general solution to

$$\frac{dy}{dt} - 3y = -4e^{-t}$$

- and plot a few of the integral curves.

$$y(t) = e^{-t} + Ce^{3t}$$



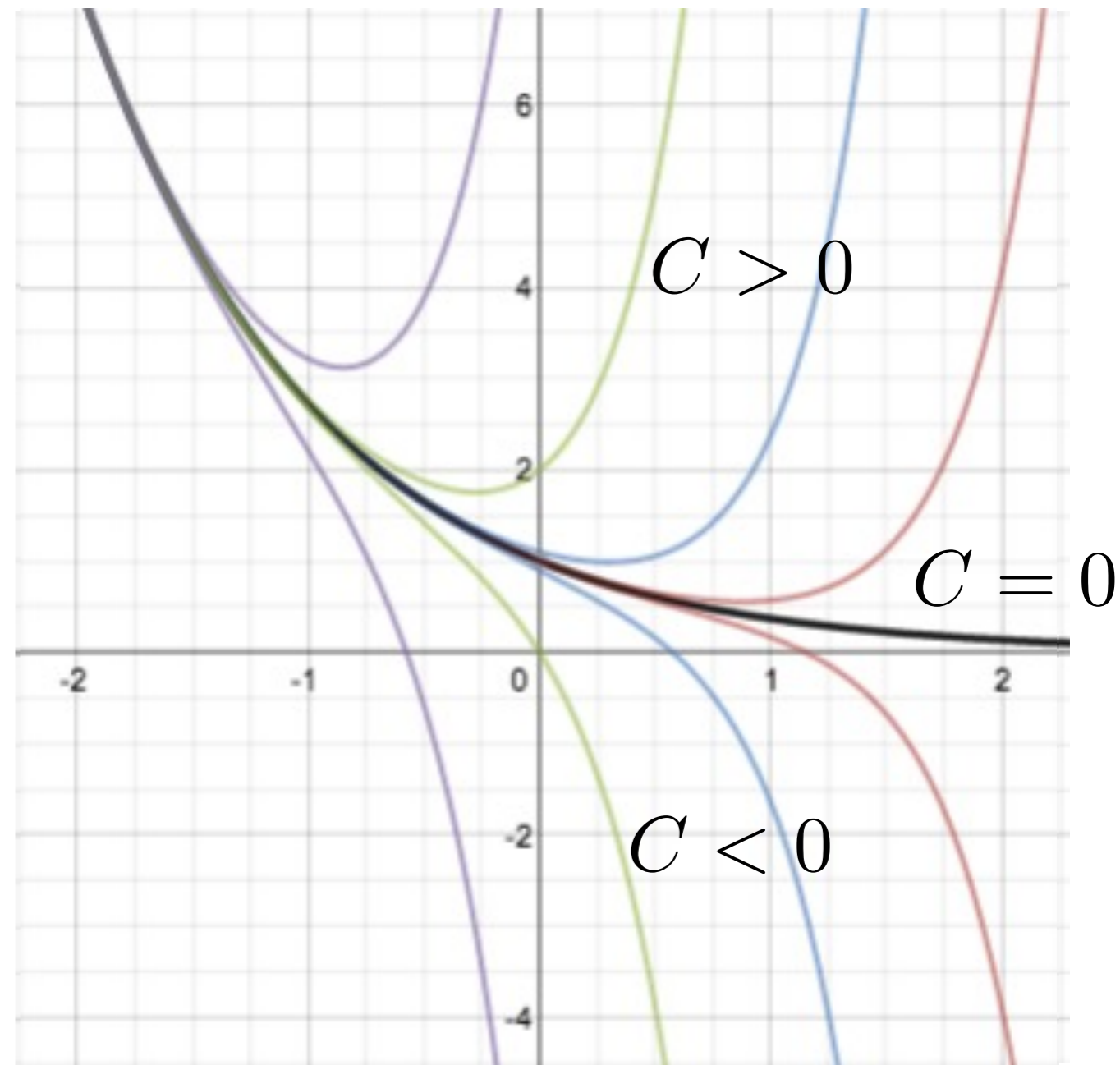
Examples

- Find the general solution to

$$\frac{dy}{dt} - 3y = -4e^{-t}$$

- and plot a few of the integral curves.

$$y(t) = e^{-t} + Ce^{3t}$$



Limits at infinity

- If $y(t)$ is a particular solution to

$$\frac{dy}{dt} - 3y = -4e^{-t}$$

- depending on C , how many different results are possible for

$$\lim_{t \rightarrow \infty} y(t) ?$$

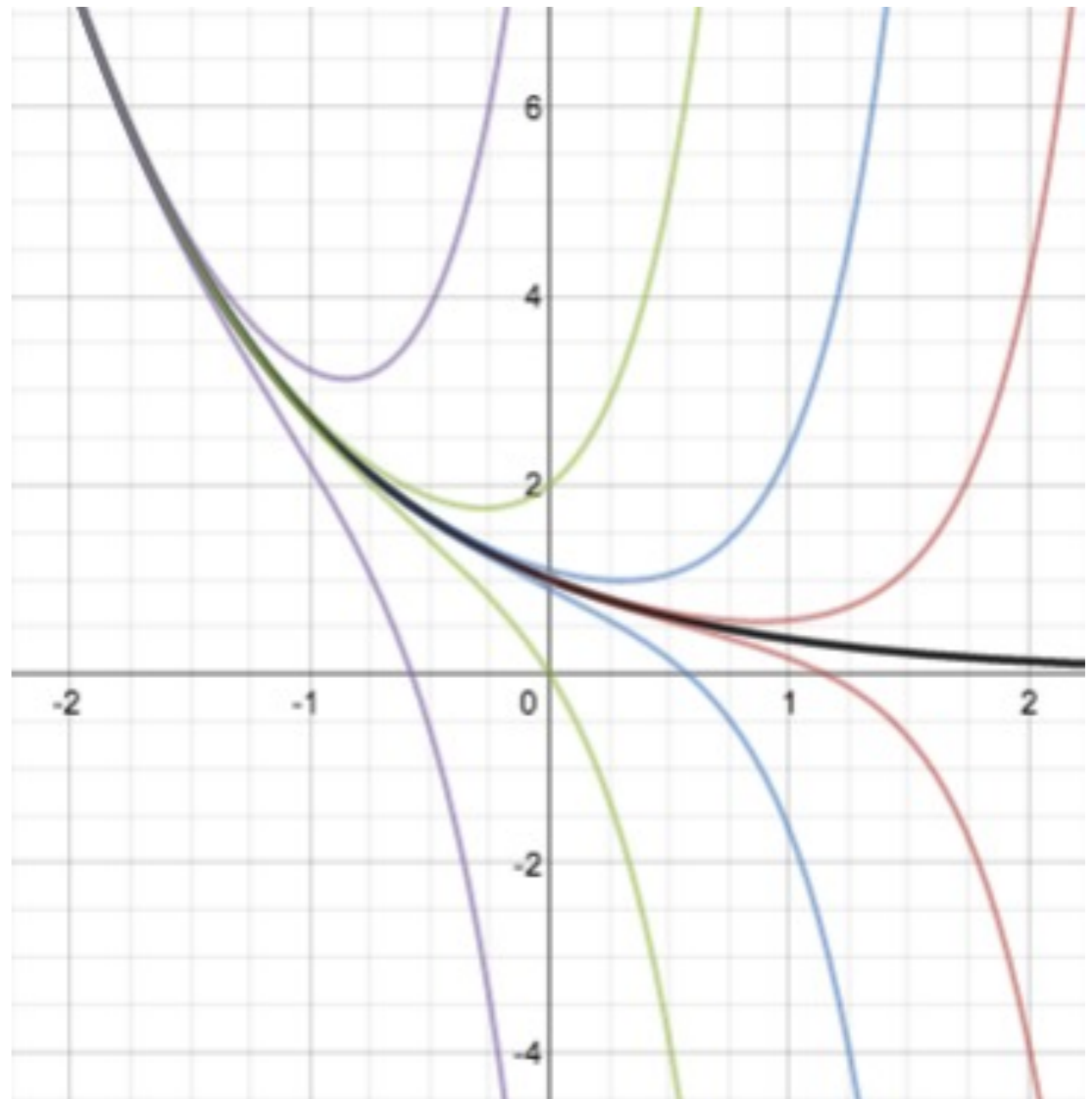
(A) 0

(B) 1

(C) 2

(D) 3

(E) Don't know.



Limits at infinity

- If $y(t)$ is a particular solution to

$$\frac{dy}{dt} - 3y = -4e^{-t}$$

- depending on C , how many different results are possible for

$$\lim_{t \rightarrow \infty} y(t) ?$$

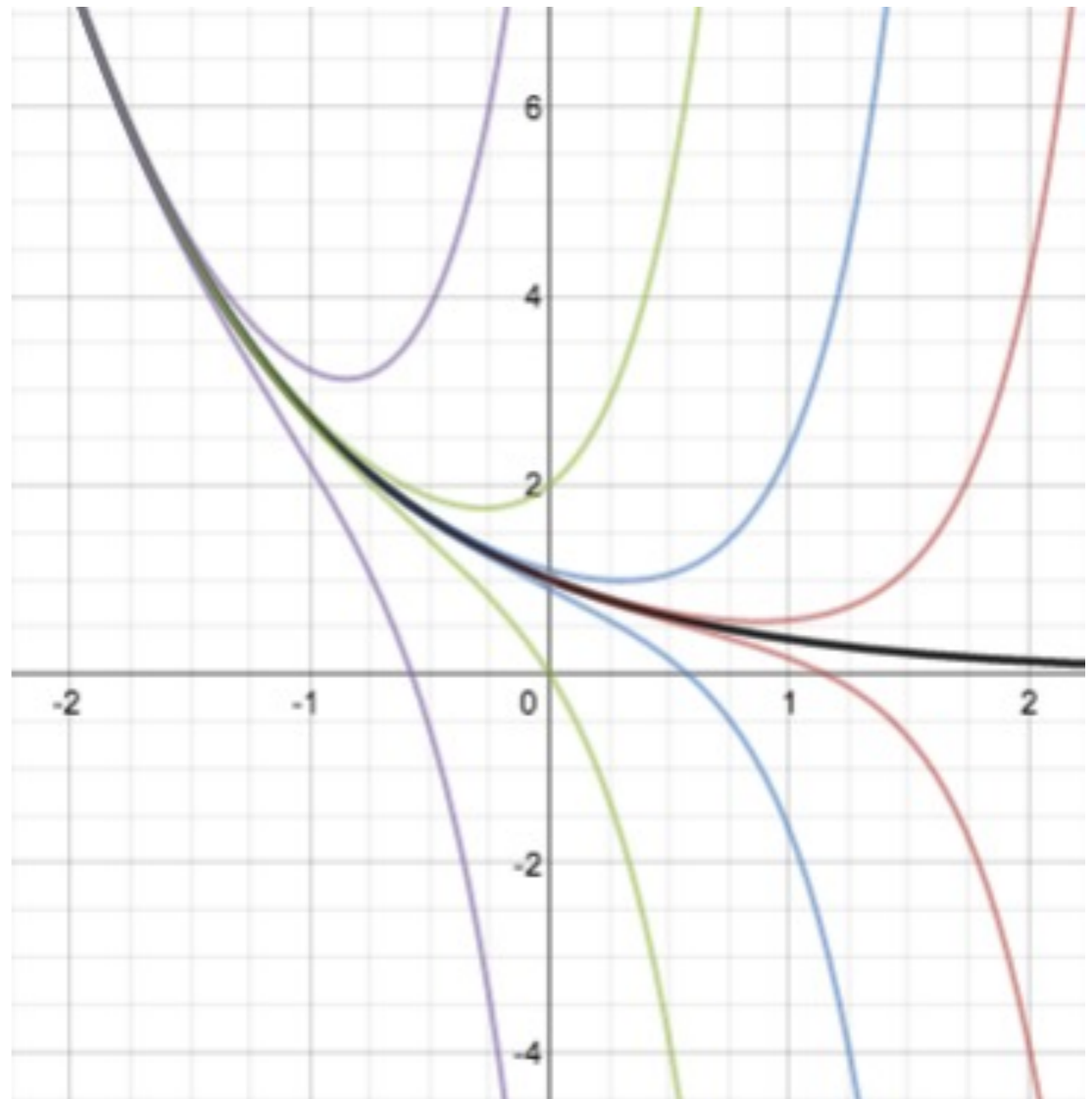
(A) 0

(B) 1

(C) 2

(D) 3

(E) Don't know.



Limits at infinity

- If $y(t)$ is a particular solution to

$$\frac{dy}{dt} - 3y = -4e^{-t}$$

- depending on C , how many different results are possible for

$$\lim_{t \rightarrow \infty} y(t) ?$$

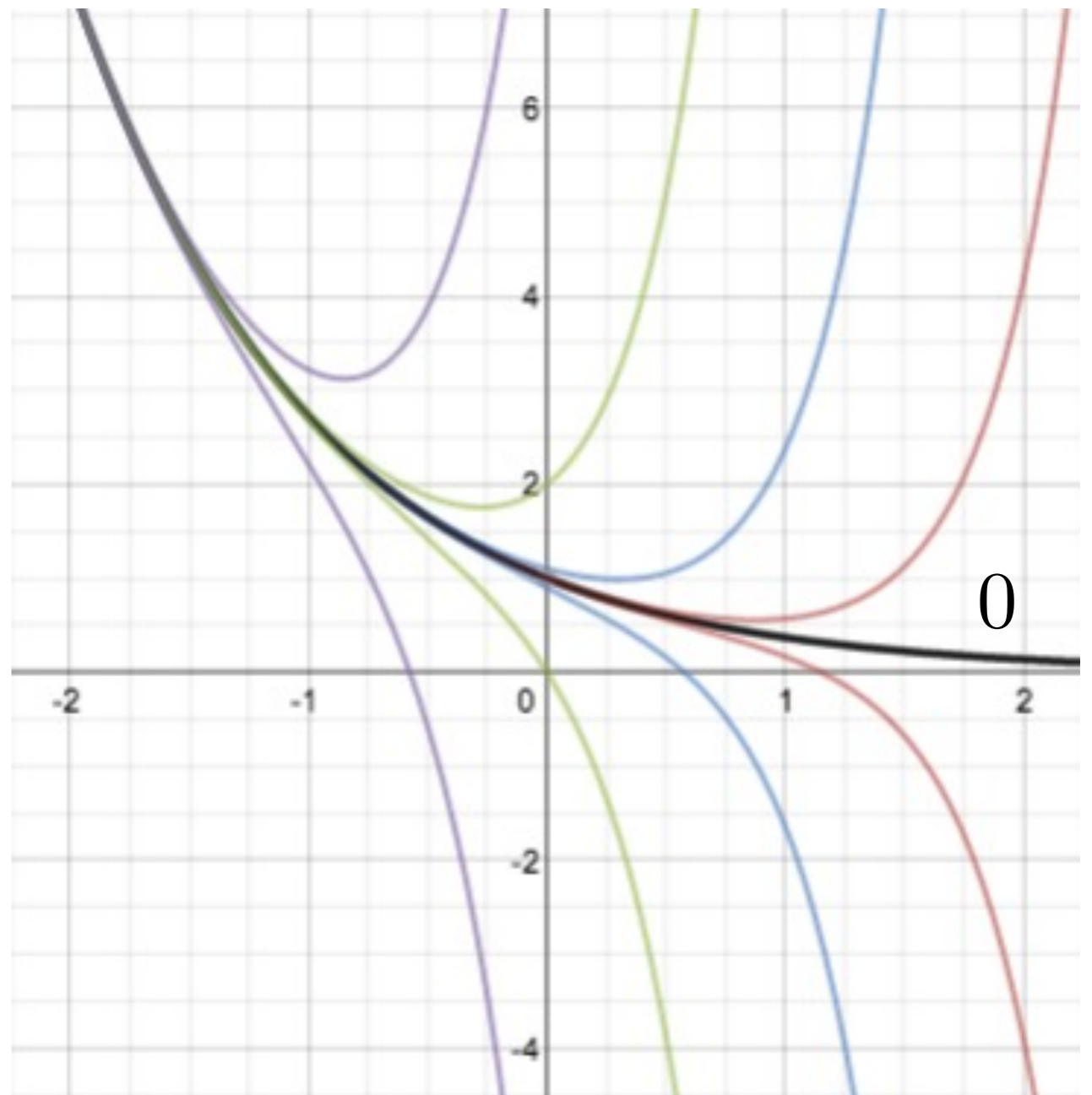
(A) 0

(B) 1

(C) 2

(D) 3

(E) Don't know.



Limits at infinity

- If $y(t)$ is a particular solution to

$$\frac{dy}{dt} - 3y = -4e^{-t}$$

- depending on C , how many different results are possible for

$$\lim_{t \rightarrow \infty} y(t) ?$$

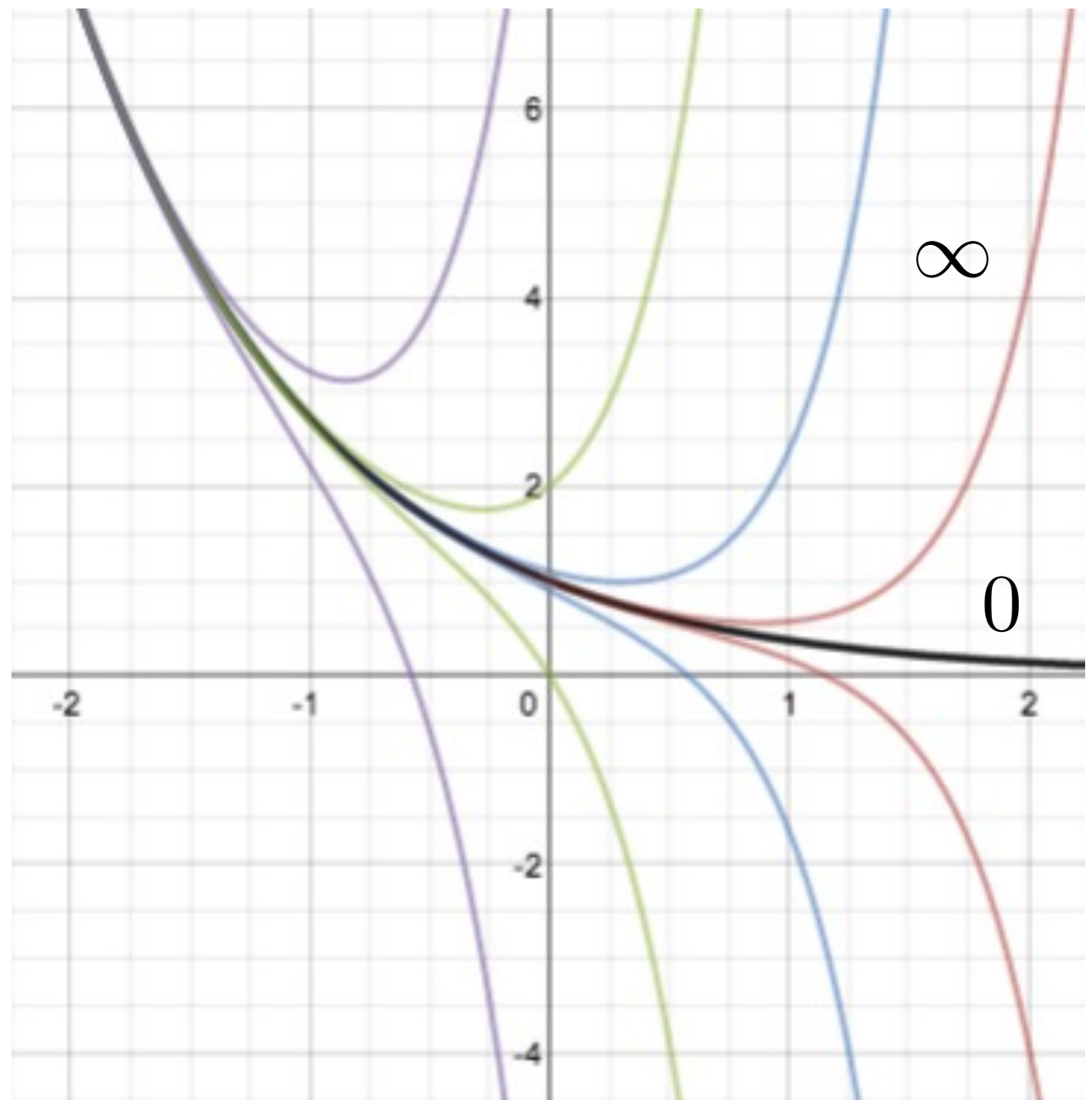
(A) 0

(B) 1

(C) 2

(D) 3

(E) Don't know.



Limits at infinity

- If $y(t)$ is a particular solution to

$$\frac{dy}{dt} - 3y = -4e^{-t}$$

- depending on C , how many different results are possible for

$$\lim_{t \rightarrow \infty} y(t) ?$$

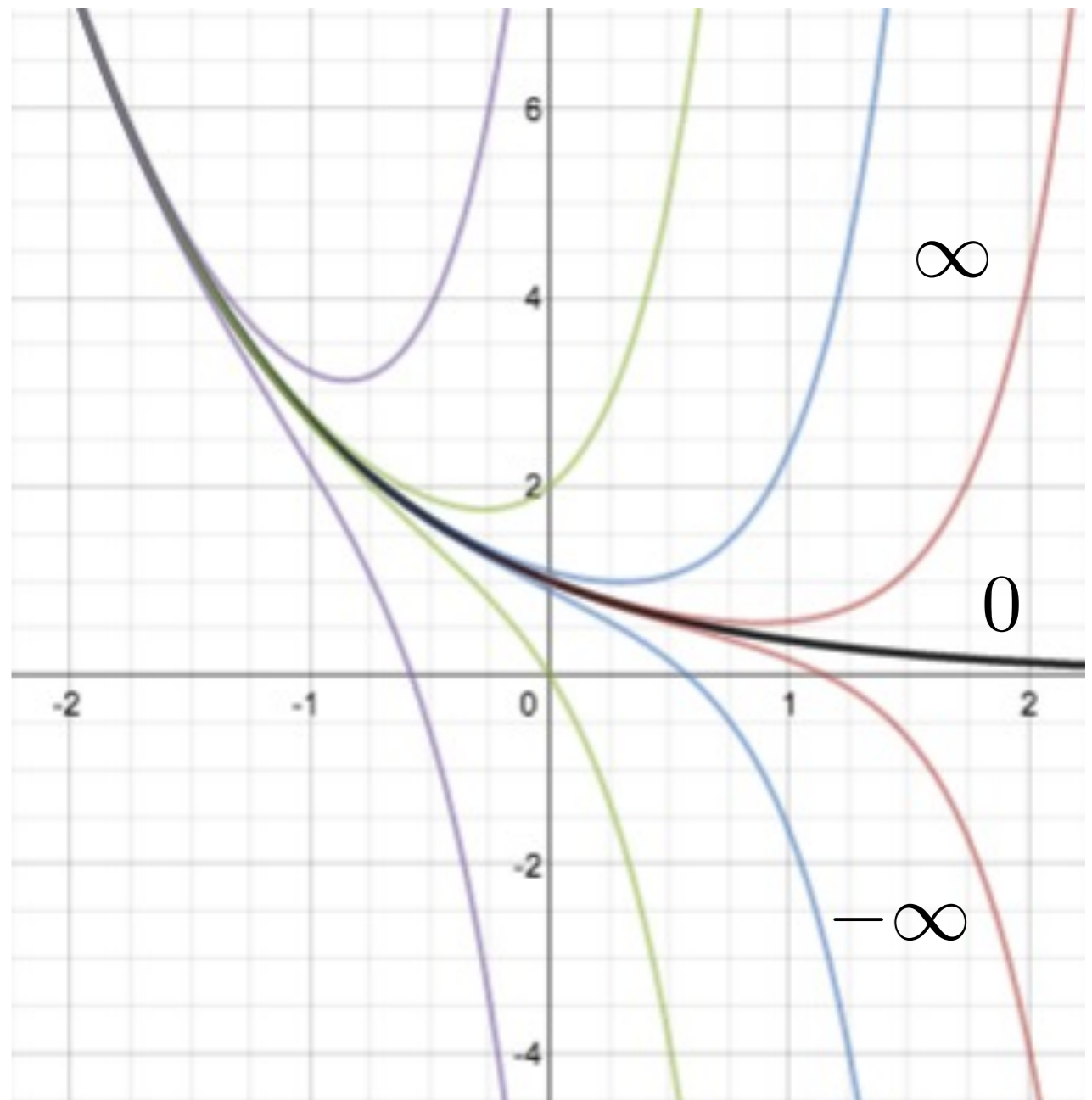
(A) 0

(B) 1

(C) 2

(D) 3

(E) Don't know.



Limits at infinity

- If $y(t)$ is a particular solution to

$$\frac{dy}{dt} - 3y = -e^t$$

- depending on C , how many different results are possible for

$$\lim_{t \rightarrow \infty} y(t) ?$$

(A) 0

(B) 1

(C) 2

(D) 3

(E) Don't know.

Limits at infinity

- If $y(t)$ is a particular solution to

$$\frac{dy}{dt} - 3y = -e^t$$

- depending on C , how many different results are possible for

$$\lim_{t \rightarrow \infty} y(t) ?$$

(A) 0

(B) 1

(C) 2

(D) 3

(E) Don't know.

$$y(t) = \frac{1}{2}e^t + Ce^{3t}$$

Limits at infinity

- If $y(t)$ is a particular solution to

$$\frac{dy}{dt} - 3y = -e^t$$

- depending on C , how many different results are possible for

$$\lim_{t \rightarrow \infty} y(t) ?$$

(A) 0

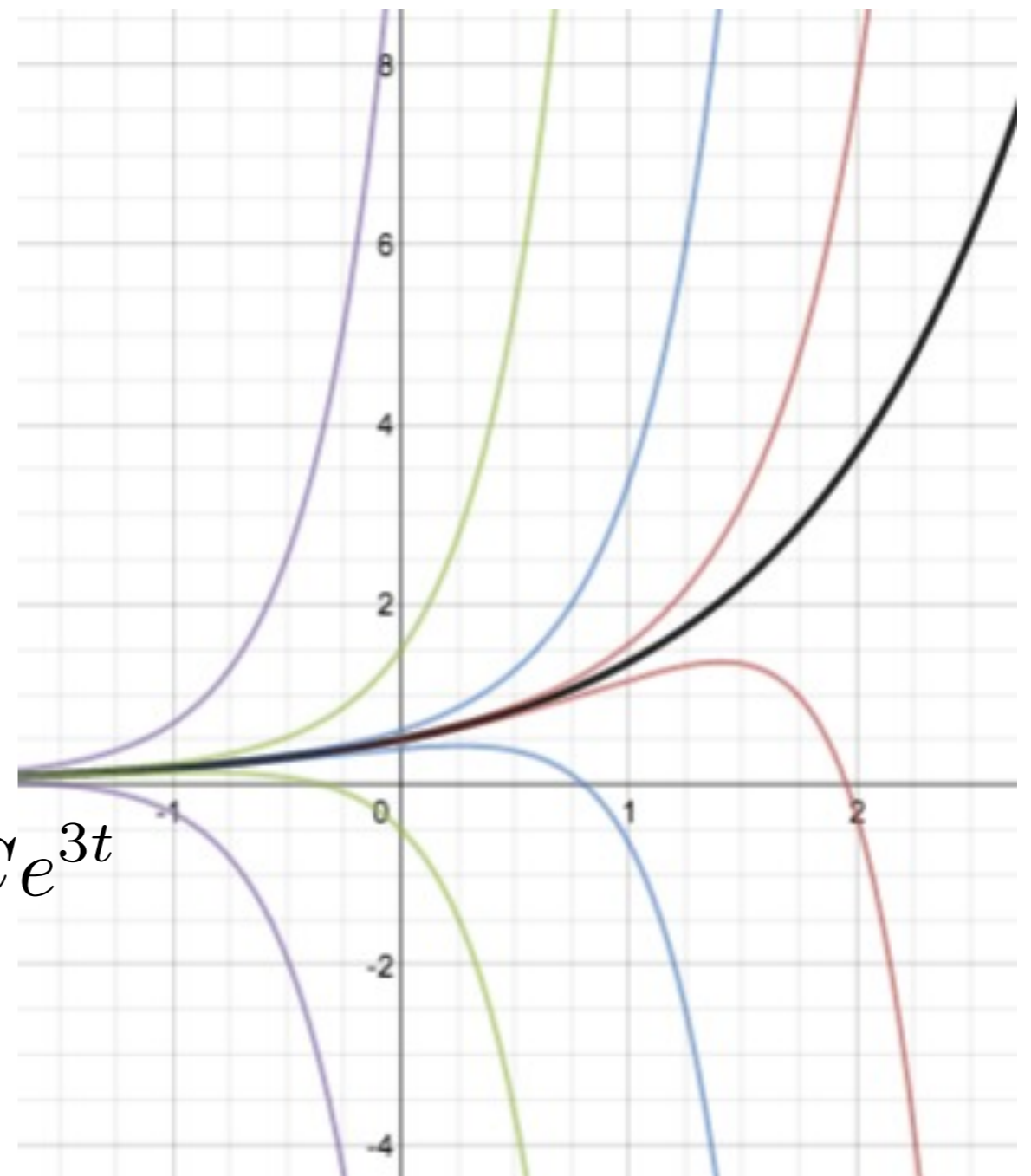
(B) 1

(C) 2

(D) 3

(E) Don't know.

$$y(t) = \frac{1}{2}e^t + Ce^{3t}$$



Limits at infinity

- If $y(t)$ is a particular solution to

$$\frac{dy}{dt} - 3y = -e^t$$

- depending on C , how many different results are possible for

$$\lim_{t \rightarrow \infty} y(t) ?$$

(A) 0

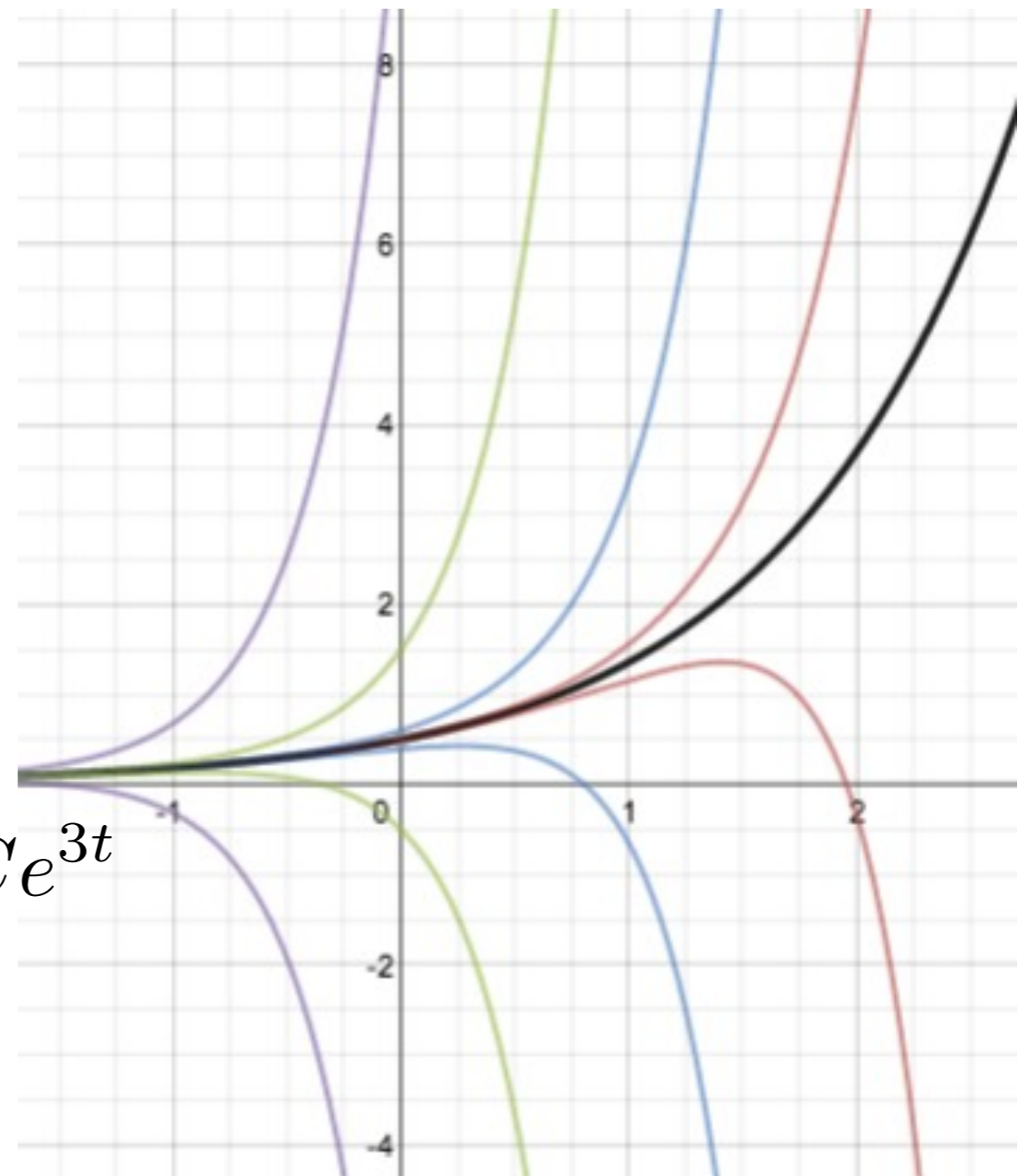
(B) 1

(C) 2

(D) 3

(E) Don't know.

$$y(t) = \frac{1}{2}e^t + Ce^{3t}$$



Limits at infinity

- If $y(t)$ is a particular solution to

$$\frac{dy}{dt} - 3y = -e^t$$

- depending on C , how many different results are possible for

$$\lim_{t \rightarrow \infty} y(t) ?$$

(A) 0

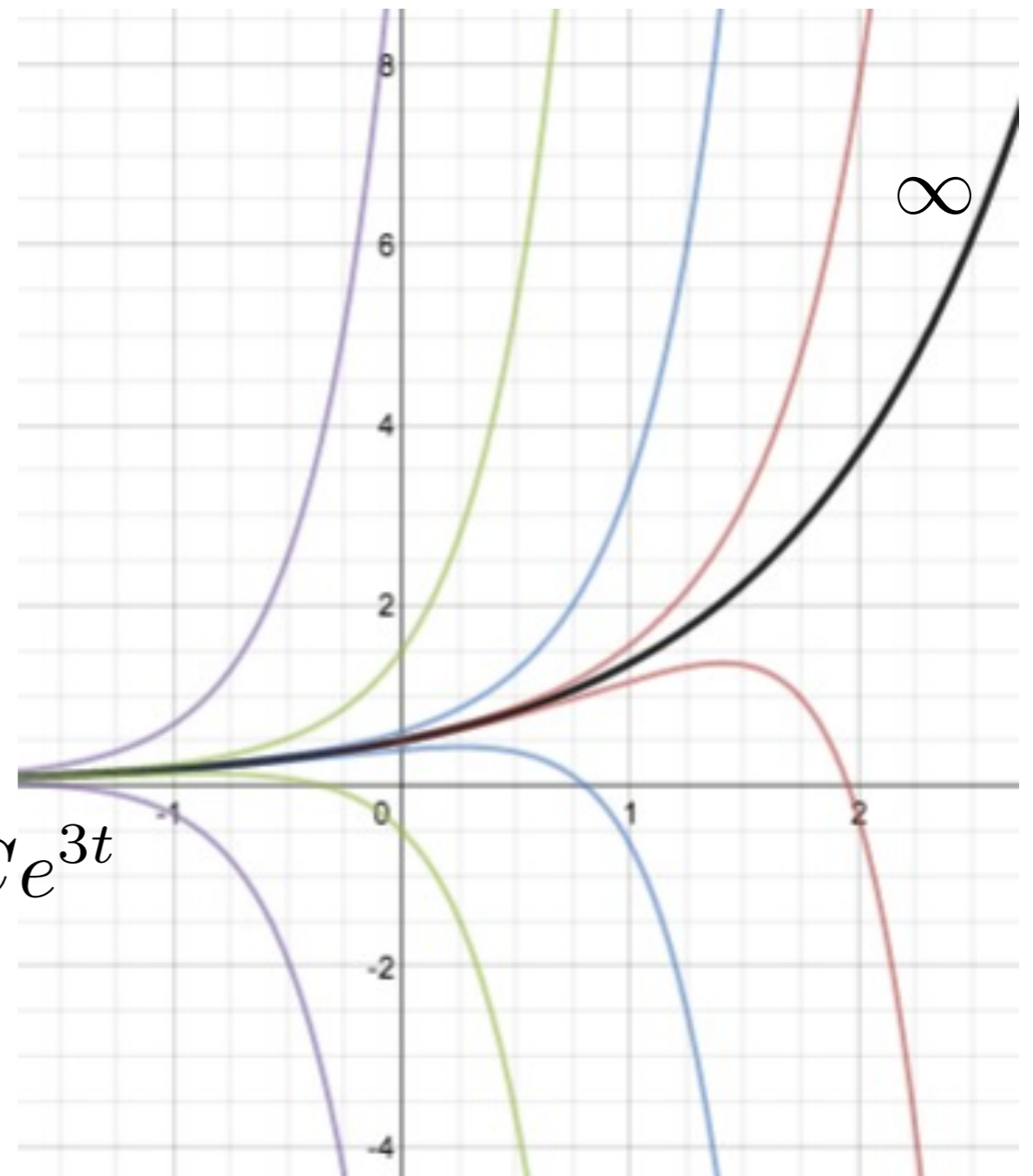
(B) 1

(C) 2

(D) 3

(E) Don't know.

$$y(t) = \frac{1}{2}e^t + Ce^{3t}$$



Limits at infinity

- If $y(t)$ is a particular solution to

$$\frac{dy}{dt} - 3y = -e^t$$

- depending on C , how many different results are possible for

$$\lim_{t \rightarrow \infty} y(t) ?$$

(A) 0

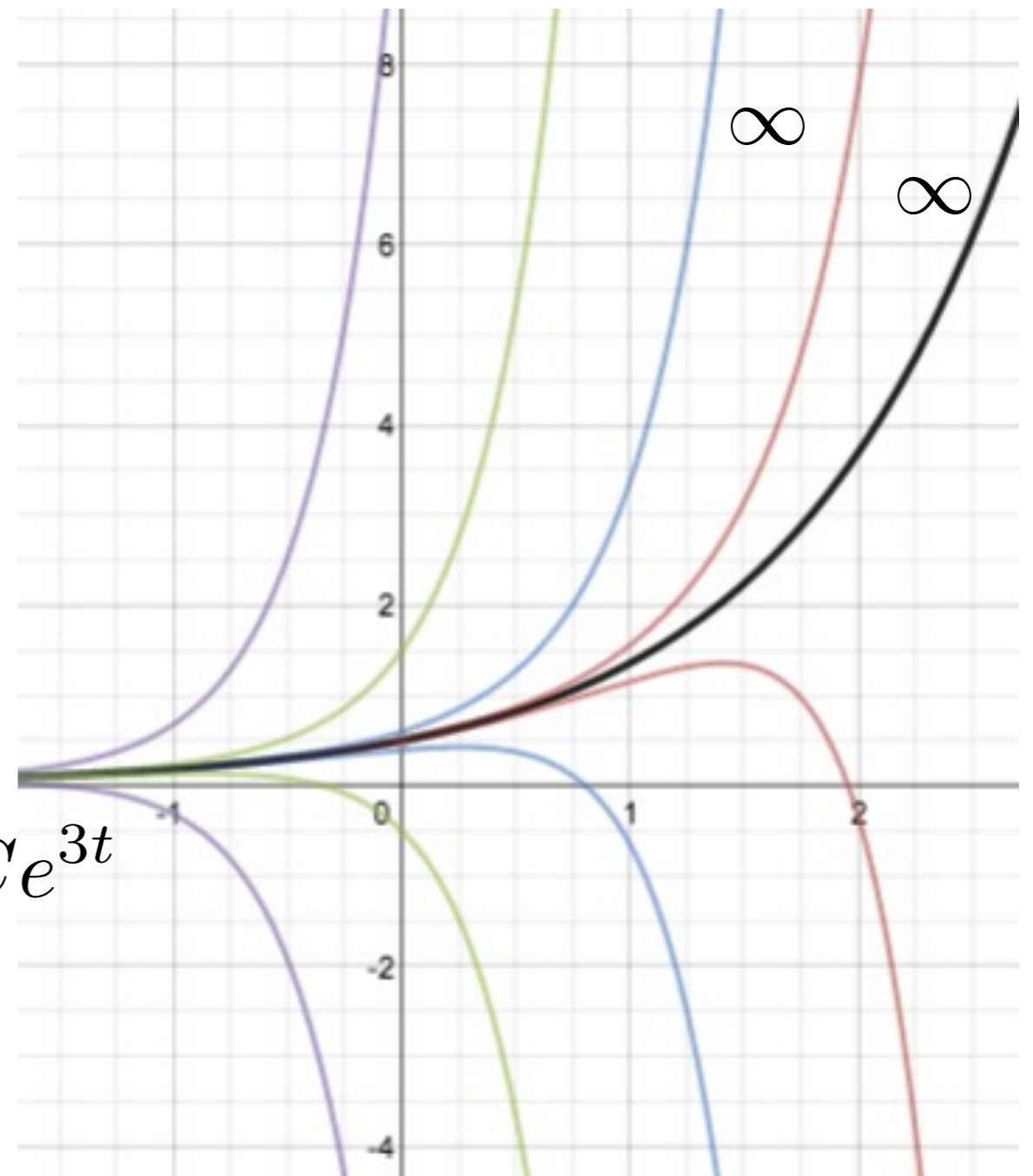
(B) 1

(C) 2

(D) 3

(E) Don't know.

$$y(t) = \frac{1}{2}e^t + Ce^{3t}$$



Limits at infinity

- If $y(t)$ is a particular solution to

$$\frac{dy}{dt} - 3y = -e^t$$

- depending on C , how many different results are possible for

$$\lim_{t \rightarrow \infty} y(t) ?$$

(A) 0

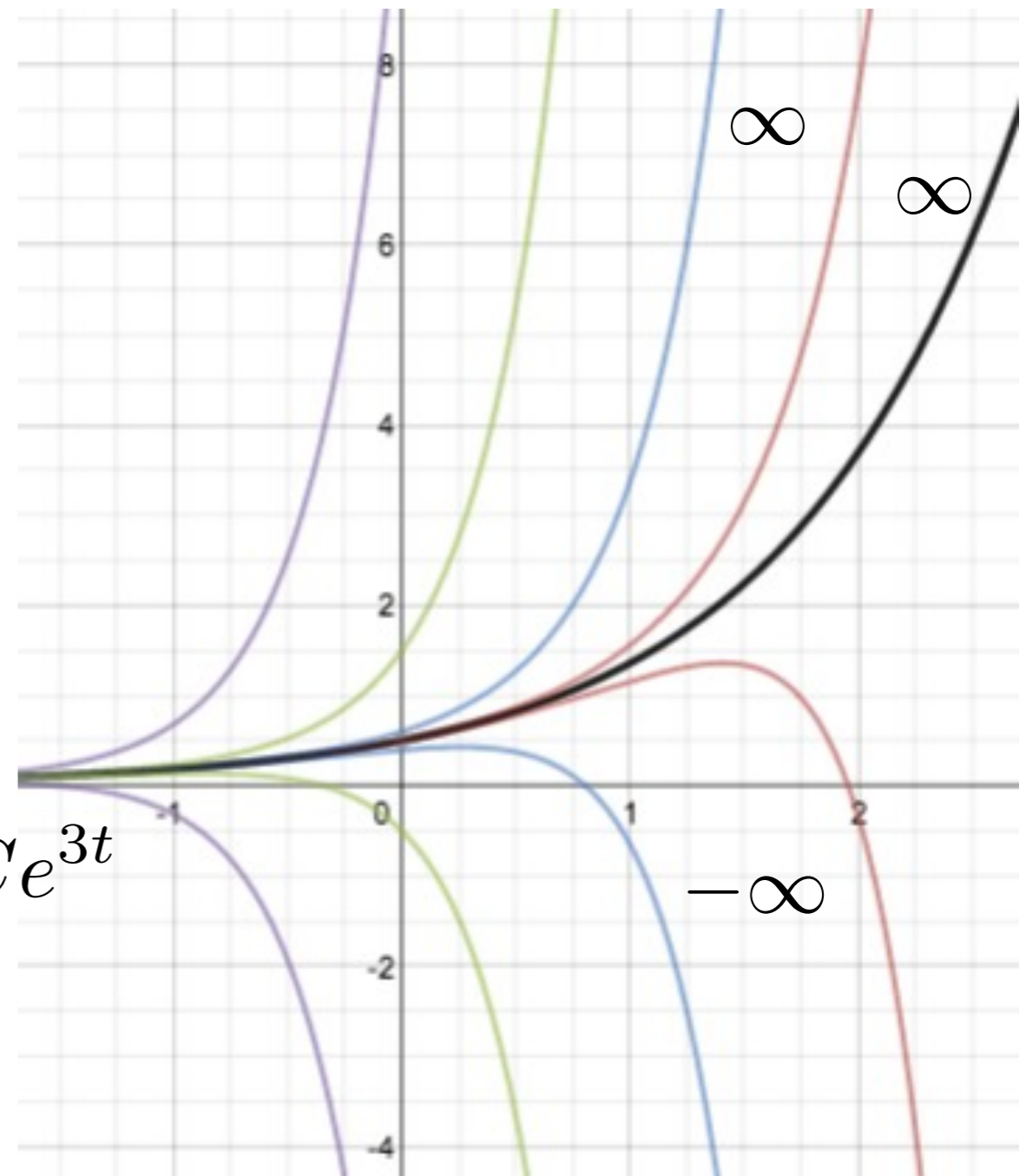
(B) 1

(C) 2

(D) 3

(E) Don't know.

$$y(t) = \frac{1}{2}e^t + Ce^{3t}$$



Separable equations (Section 2.2)

• What is $\frac{d}{dt} e^y$?

(A) e^y

(B) $e^y \frac{dy}{dt}$

(C) ye^{y-1}

(D) $ye^{y-1} \frac{dy}{dt}$

(E) Don't know.

Separable equations (Section 2.2)

• What is $\frac{d}{dt} e^y$?

(A) e^y

(B) $e^y \frac{dy}{dt}$

(C) ye^{y-1}

(D) $ye^{y-1} \frac{dy}{dt}$

(E) Don't know.

Separable equations (Section 2.2)

• What is $\frac{d}{dt} e^y$?

(A) e^y

(B) $e^y \frac{dy}{dt}$

(C) ye^{y-1}

(D) $ye^{y-1} \frac{dy}{dt}$

(E) Don't know.

• Solve $\frac{dy}{dt} = e^{-y}$.

(A) $y(t) = 0$

(B) $y(t) = \ln(t) + C$

(C) $y(t) = \ln(t + C)$

(D) $y(t) = e^{t+C}$

(E) Don't know.

Separable equations (Section 2.2)

- What is $\frac{d}{dt} e^y$?

Hint: rewrite as $e^y \frac{dy}{dt} = 1$.

(B) $e^y \frac{dy}{dt}$

(C) ye^{y-1}

(D) $ye^{y-1} \frac{dy}{dt}$

(E) Don't know.

- Solve $\frac{dy}{dt} = e^{-y}$.

(A) $y(t) = 0$

(B) $y(t) = \ln(t) + C$

(C) $y(t) = \ln(t + C)$

(D) $y(t) = e^{t+C}$

(E) Don't know.

Separable equations (Section 2.2)

- What is $\frac{d}{dt} e^y$?

Hint: rewrite as $e^y \frac{dy}{dt} = 1$.

$$\frac{d}{dt}(e^y) = 1$$

(C) $y e^{y-1} \frac{dy}{dt}$

(E) Don't know.

- Solve $\frac{dy}{dt} = e^{-y}$.

(A) $y(t) = 0$

(B) $y(t) = \ln(t) + C$

(C) $y(t) = \ln(t + C)$

(D) $y(t) = e^{t+C}$

(E) Don't know.

Separable equations (Section 2.2)

- What is $\frac{d}{dt} e^y$?

Hint: rewrite as $e^y \frac{dy}{dt} = 1$.

$$\frac{d}{dt} (e^y) = 1$$

$$e^y = t + C$$

(D) $y e^y = \frac{t}{dt}$

(E) Don't know.

- Solve $\frac{dy}{dt} = e^{-y}$.

(A) $y(t) = 0$

(B) $y(t) = \ln(t) + C$

(C) $y(t) = \ln(t + C)$

(D) $y(t) = e^{t+C}$

(E) Don't know.

Separable equations (Section 2.2)

• What is $\frac{d}{dt} e^y$?

(A) e^y

(B) $e^y \frac{dy}{dt}$

(C) ye^{y-1}

(D) $ye^{y-1} \frac{dy}{dt}$

(E) Don't know.

• Solve $\frac{dy}{dt} = e^{-y}$.

(A) $y(t) = 0$

(B) $y(t) = \ln(t) + C$

(C) $y(t) = \ln(t + C)$

(D) $y(t) = e^{t+C}$

(E) Don't know.

Separable equations (Section 2.2)

• What is $\frac{d}{dt} e^y$?

(A) e^y

(B) $e^y \frac{dy}{dt}$

(C) ye^{y-1}

(D) $ye^{y-1} \frac{dy}{dt}$

(E) Don't know.

• Solve $\frac{dy}{dt} = e^{-y} t^2$.

(A) $y(t) = t^2 e^t + C$

(B) $y(t) = \frac{1}{3} t^3 + C$

(C) $y(t) = \ln \left(\frac{1}{3} t^3 \right) + C$

(D) $y(t) = \ln \left(\frac{1}{3} t^3 + C \right)$

(E) Don't know.

Separable equations (Section 2.2)

- What is $\frac{d}{dt} e^y$?

Hint: rewrite as $e^y \frac{dy}{dt} = t^2$.

(D) $y e^y \frac{dy}{dt}$

(E) Don't know.

- Solve $\frac{dy}{dt} = e^{-y} t^2$.

(A) $y(t) = t^2 e^t + C$

(B) $y(t) = \frac{1}{3} t^3 + C$

(C) $y(t) = \ln \left(\frac{1}{3} t^3 \right) + C$

(D) $y(t) = \ln \left(\frac{1}{3} t^3 + C \right)$

(E) Don't know.

Separable equations (Section 2.2)

- What is $\frac{d}{dt} e^y$?

Hint: rewrite as $e^y \frac{dy}{dt} = t^2$.

$$\frac{d}{dt} (e^y) = t^2$$

(D) $y e^y \frac{dy}{dt}$

(E) Don't know.

- Solve $\frac{dy}{dt} = e^{-y} t^2$.

(A) $y(t) = t^2 e^t + C$

(B) $y(t) = \frac{1}{3} t^3 + C$

(C) $y(t) = \ln \left(\frac{1}{3} t^3 \right) + C$

(D) $y(t) = \ln \left(\frac{1}{3} t^3 + C \right)$

(E) Don't know.

Separable equations (Section 2.2)

- What is $\frac{d}{dt} e^y$?

Hint: rewrite as $e^y \frac{dy}{dt} = t^2$.

$$\frac{d}{dt}(e^y) = t^2$$

$$e^y = \frac{1}{3}t^3 + C$$

(D) $y = \frac{1}{3}t^3 + C$

(E) Don't know.

- Solve $\frac{dy}{dt} = e^{-y}t^2$.

(A) $y(t) = t^2 e^t + C$

(B) $y(t) = \frac{1}{3}t^3 + C$

(C) $y(t) = \ln\left(\frac{1}{3}t^3\right) + C$

(D) $y(t) = \ln\left(\frac{1}{3}t^3 + C\right)$

(E) Don't know.

Separable equations (Section 2.2)

- What is $\frac{d}{dt}e^y$?

Hint: rewrite as $e^y \frac{dy}{dt} = t^2$.

$$\frac{d}{dt}(e^y) = t^2$$

$$e^y = \frac{1}{3}t^3 + C$$

(D) $y = \ln\left(\frac{1}{3}t^3 + C\right)$

(E) Don't know.

- Solve $\frac{dy}{dt} = e^{-y}t^2$.

(A) $y(t) = t^2 e^t + C$

(B) $y(t) = \frac{1}{3}t^3 + C$

(C) $y(t) = \ln\left(\frac{1}{3}t^3\right) + C$

(D) $y(t) = \ln\left(\frac{1}{3}t^3 + C\right)$

(E) Don't know.